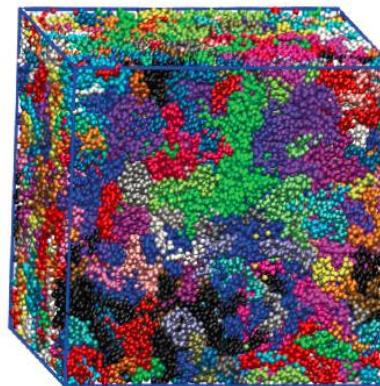
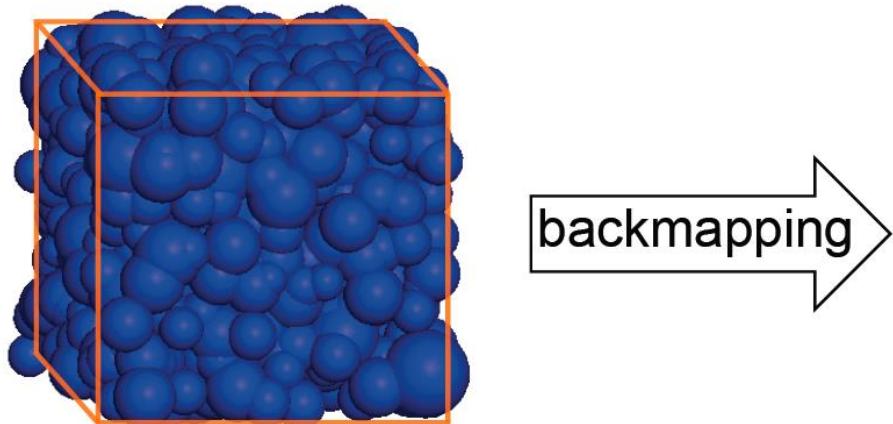


# EQUILIBRATING HIGH MOLECULAR-WEIGHT POLYMER MELTS USING HIERARCHICAL STRATEGIES

Guojie Zhang, Takahiro Ohkuma, Hsiao-Ping Hsu,  
Torsten Stuehn, Kostas Daoulas, and Kurt Kremer



THEORY  
GROUP

## OUTLINE



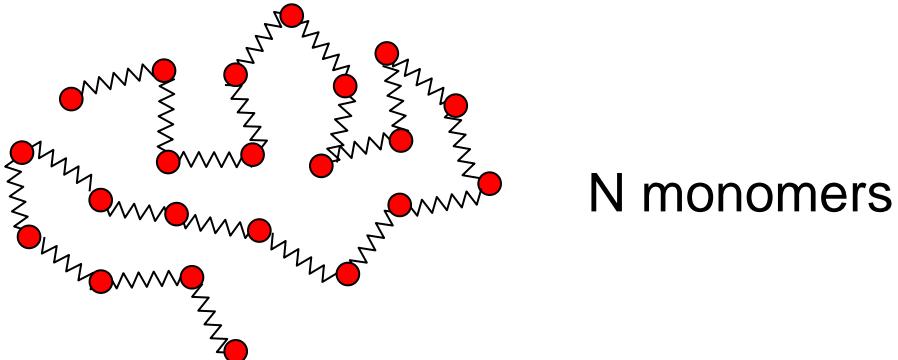
- Reminder: Rouse and reptation models. Why modeling polymer melts is challenging ?
- Hierarchical modeling of generic and chemistry-specific systems
- “Material genomic” approach to blob-based models
- Hierarchical modeling of multicomponent systems → symmetric blends
- Concluding comments



# DYNAMICS IN MELTS OF SHORT POLYMERS: ROUSE MODEL



- Originally developed for dilute polymer solution



- Assumption → solvent treated as immobile “background”

- Brownian motion of N linked beads

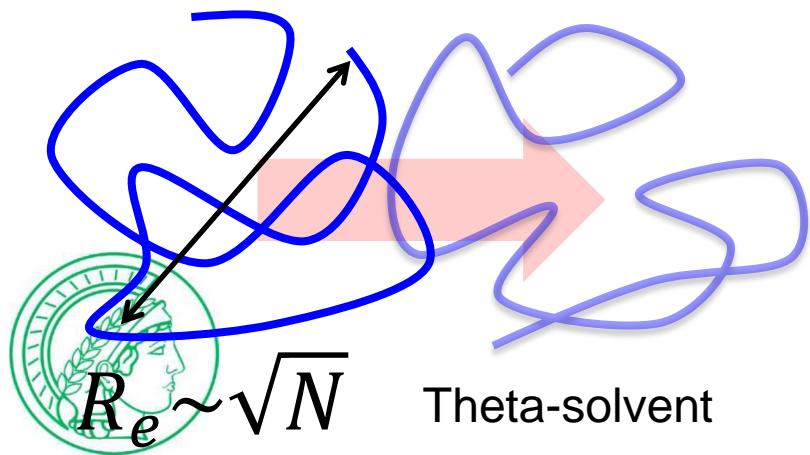
$$\zeta_R = N\zeta$$

friction coefficient of  
whole Rouse chain

$$D_R = \frac{kT}{N\zeta}$$

diffusion coefficient of  
whole Rouse chain

- Largest chain-relaxation time ~ chain must diffuse a length comparable to chain size



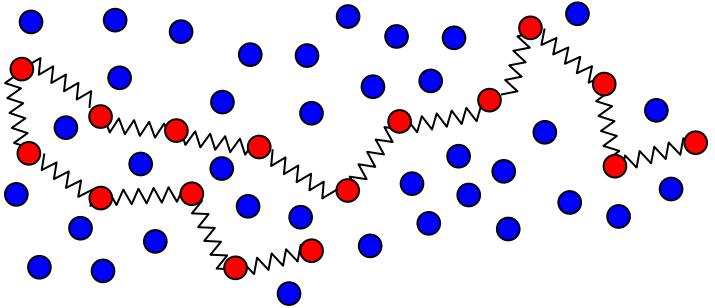
$$R_e^2 \sim D_R \tau_R \Rightarrow \tau_R \sim \frac{\zeta N^2}{kT}$$

Rouse  
time

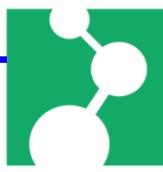
# DYNAMICS IN MELTS OF SHORT POLYMERS: ROUSE MODEL



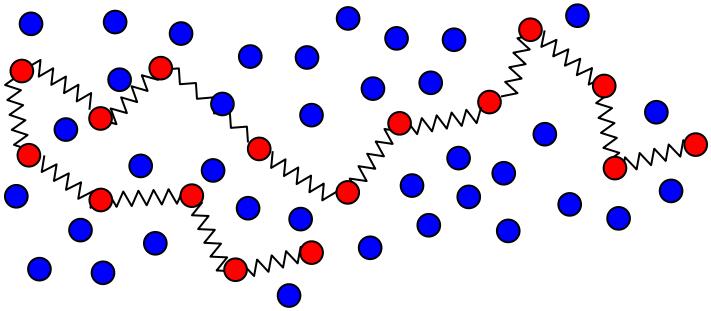
- ❑ Rouse model neglects hydrodynamic interactions →  
Long-range forces arising from motion of one particle



# DYNAMICS IN MELTS OF SHORT POLYMERS: ROUSE MODEL



- Rouse model neglects hydrodynamic interactions →  
Long-range forces arising from motion of one particle



- For dilute solutions Zimm model is appropriate
- In **melts of short polymers** hydrodynamic interactions are screened and Rouse model becomes valid

- To remember from Rouse model

$$\tau_R \sim \frac{\zeta N^2}{kT} \quad D_R = \frac{kT}{N\zeta}$$

*See also:*

Doi & Edwards, The Theory of Polymer Dynamics 1986

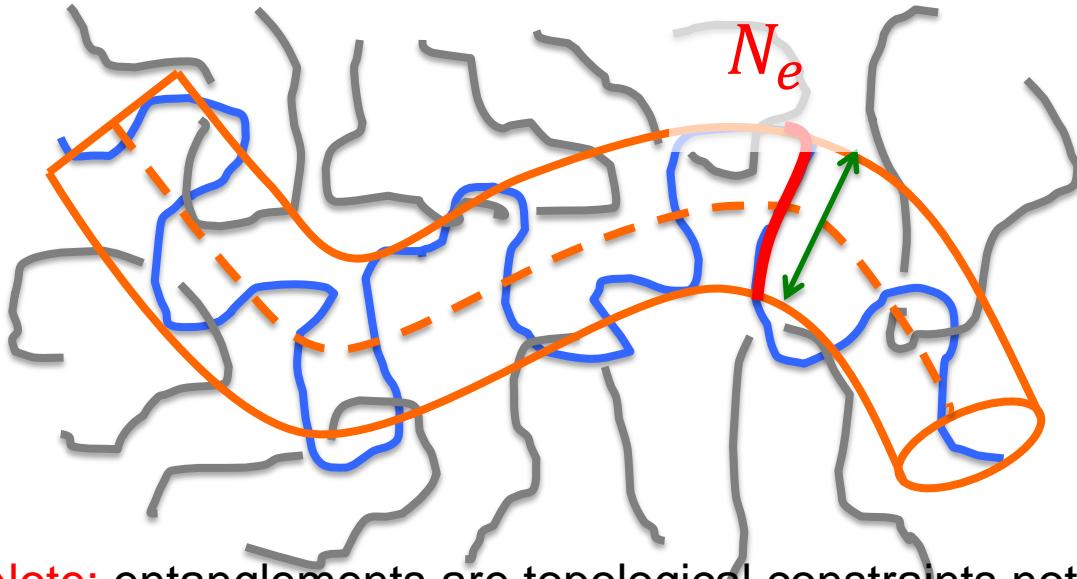
Grosberg & Khokhlov,  
Statistical Physics of Macromolecules 1997  
Rubinstein & Colby, Polymer Physics 2003



# DYNAMICS IN MELTS OF LONG POLYMERS: REPTATION MODEL



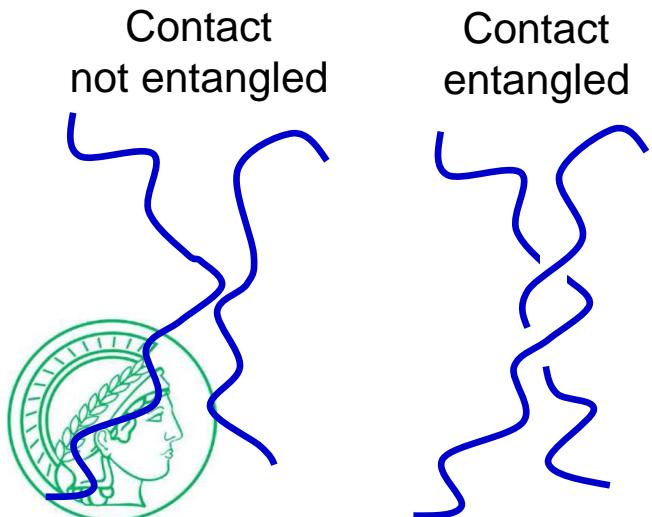
- Topological entanglements create an effective tube
- Chain motion on large length scales corresponds to 1D reptation along tube-axis



Presentation follows:

Grosberg & Khokhlov,  
Statistical Physics of  
Macromolecules 1997

- Note: entanglements are topological constraints not just monomer / monomer contacts



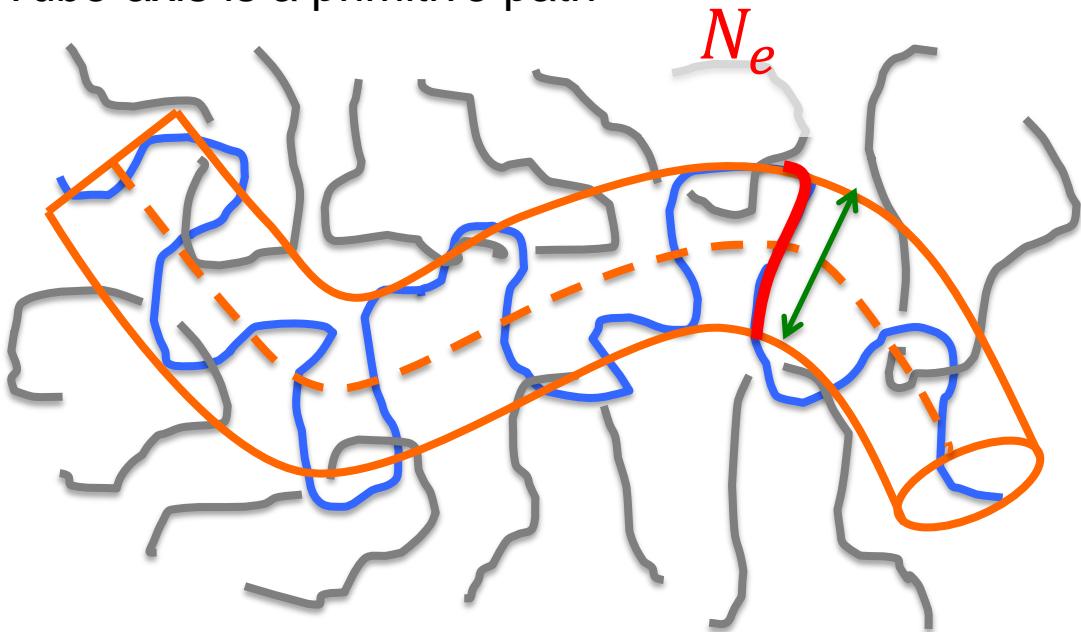
≠



# DYNAMICS IN MELTS OF LONG POLYMERS: REPTATION MODEL



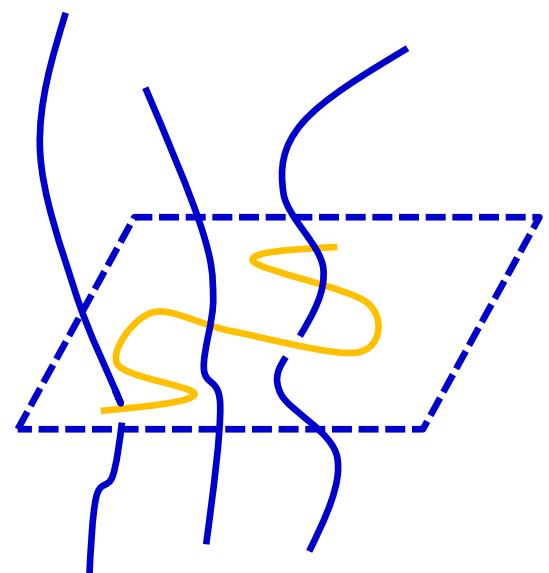
- ☐ Tube-axis is a primitive path



Tube diameter:  $d \sim \sqrt{N_e}$

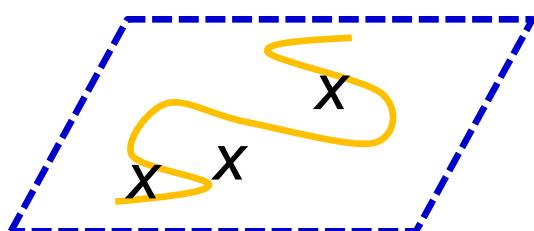
Presentation follows:

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Statistical Physics of  
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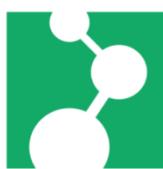


- ☐ Primitive path:

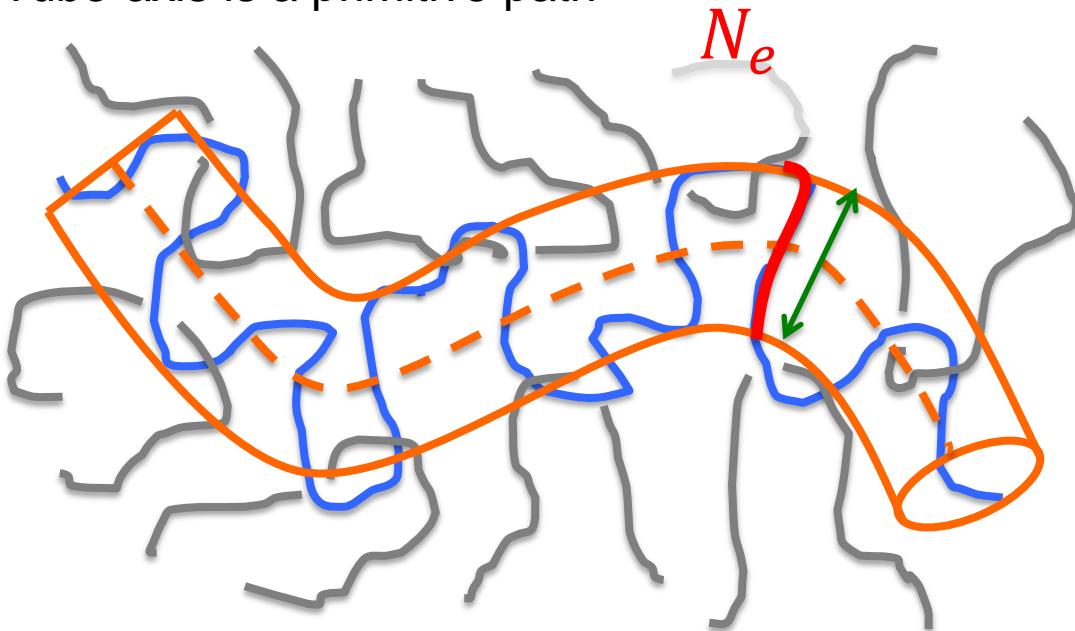
Shortest line between chain-ends which preserves the chain-topology with respect to surrounding chains



# DYNAMICS IN MELTS OF LONG POLYMERS: REPTATION MODEL



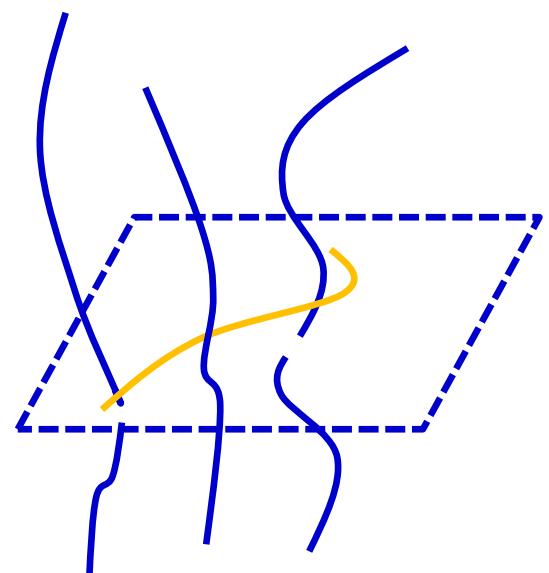
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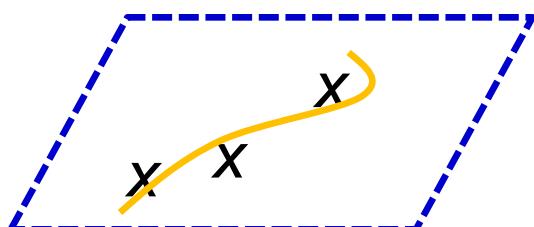
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- ☐ Primitive path:

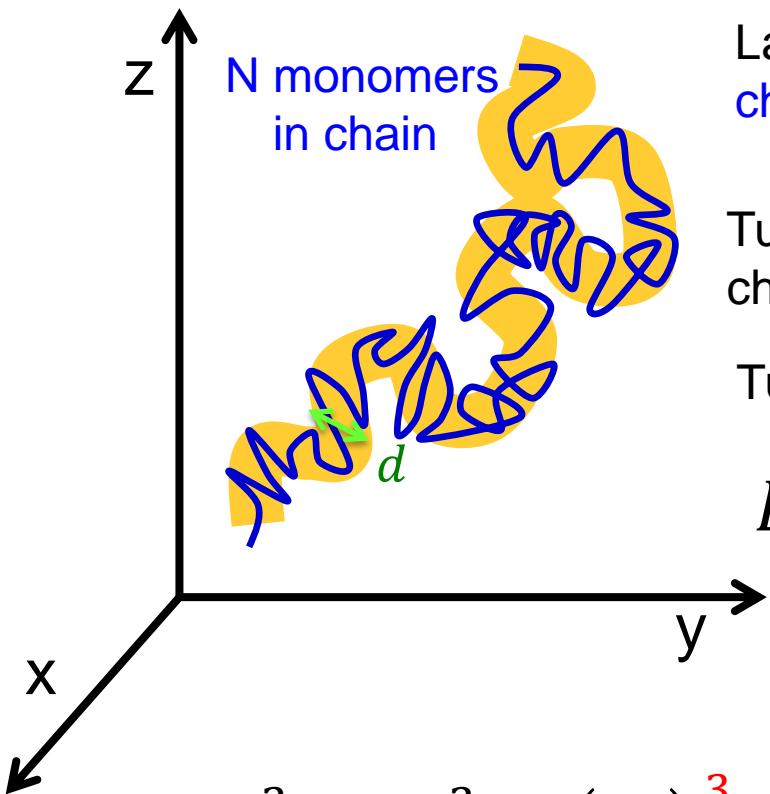
Shortest line between chain-ends which preserves the chain-topology with respect to surrounding chains



# DYNAMICS IN MELTS OF LONG POLYMERS: REPTATION MODEL



- Simple estimations of relaxation time and diffusion coefficient



Largest relaxation time → chain reptates out of the tube

Tube is a random walk characteristic scale  $d$

Tube contour length

$$L = d \frac{N}{N_e}$$

1D diffusion coefficient along tube

$$D_t = \frac{kT}{\zeta N}$$

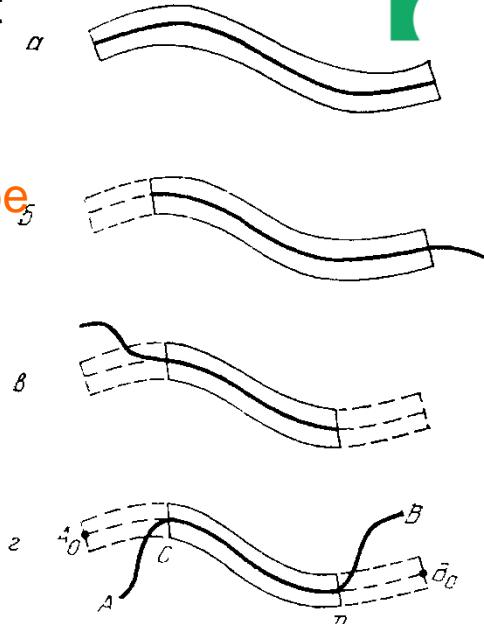
$$\tau = \frac{L^2}{D_t} = \frac{\zeta d^2 N_e}{kT} \left( \frac{N}{N_e} \right)^3 \sim \frac{\zeta N_e^2}{kT} \left( \frac{N}{N_e} \right)^3$$

Rouse time of entanglement strand

$$\tau_e \sim \frac{\zeta N_e^2}{kT}$$

3D diffusion coefficient

$$D = \frac{\langle R^2 \rangle}{t} = \frac{1}{\tau N_e} \frac{N}{d^2} = \frac{N_e}{N^2} \frac{kT}{\zeta}$$



# STUDYING HIGH-MOLECULAR POLYMER MELTS IS CHALLENGING AND IMPORTANT



- Equilibrating melts of long polymers described with microscopic detail is **challenging**:

Largest relaxation time:  $\tau \sim \tau_e \left( \frac{N}{N_e} \right)^3$

Chain diffusion:  $D = \frac{N_e kT}{N^2 \zeta}$

- Modeling high-molecular weight polymers is crucial for **industry** where  $\frac{N}{N_e} \sim 100$

Example:

Processing requires detailed understanding of polymer dynamics and rheology

Classical and modern applications,  
e.g. printing polymer inks with useful optical and electronic properties

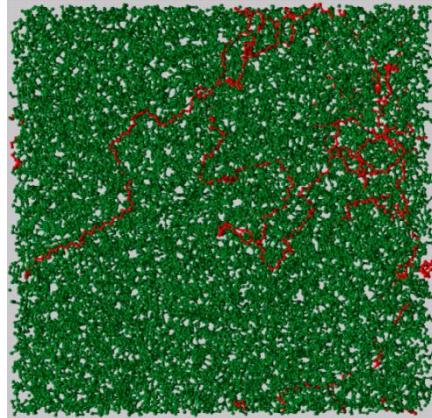


# STRATEGIES FOR EQUILIBRATING LONG POLYMER MELTS



## Single-scale techniques:

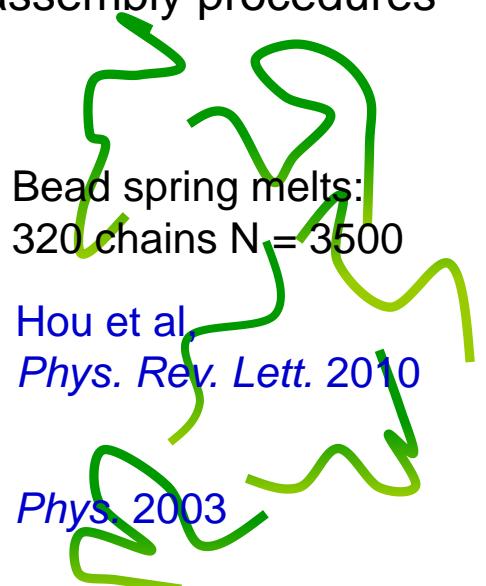
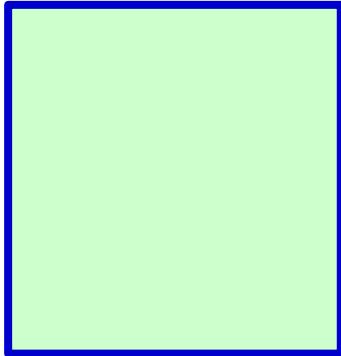
- Re-bridging Monte Carlo moves



PE melts:  
32 chains, C6000  
Uhlherr et al,  
*Europhys. Lett.* 2002

Pant & Theodorou, *Macromolecules* 1995

- Configuration assembly procedures



## Multiscale techniques:



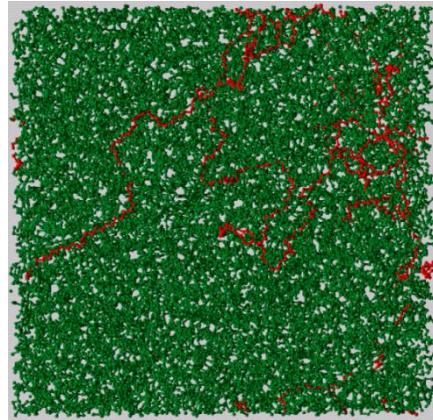
Auhl et al, *J. Chem. Phys.* 2003

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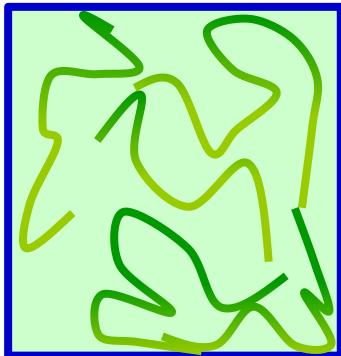
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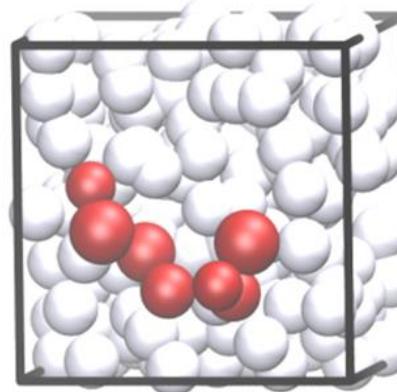
- Configuration assembly procedures



Bead spring melts:  
320 chains N = 3500  
Hou et al,  
*Phys. Rev. Lett.* 2010

Auhl et al, *J. Chem. Phys.* 2003

## Multiscale techniques:



blob model

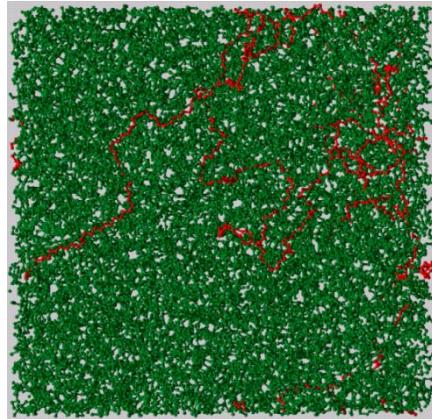
- Opportunities:

# STRATEGIES FOR EQUILIBRATING LONG POLYMER MELTS



## Single-scale techniques:

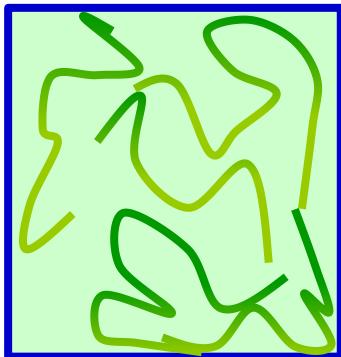
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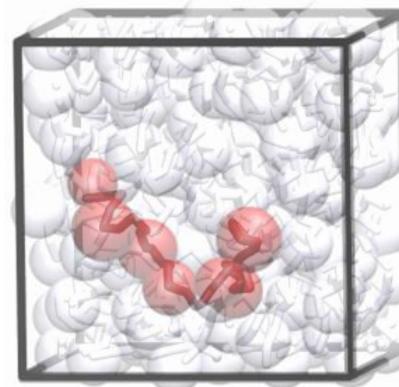
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*Phys. Rev. Lett.* 2010

Auhl et al, *J. Chem. Phys.* 2003

## Multiscale techniques:



reinsert details

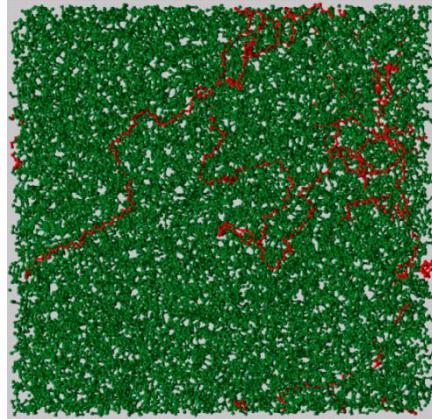
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# STRATEGIES FOR EQUILIBRATING LONG POLYMER MELTS



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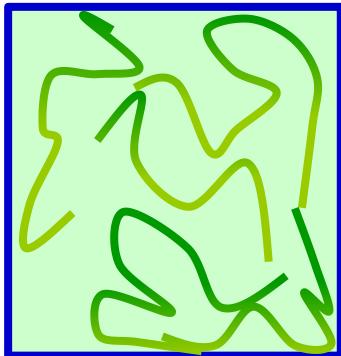
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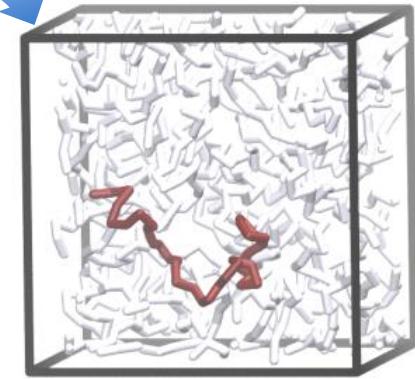
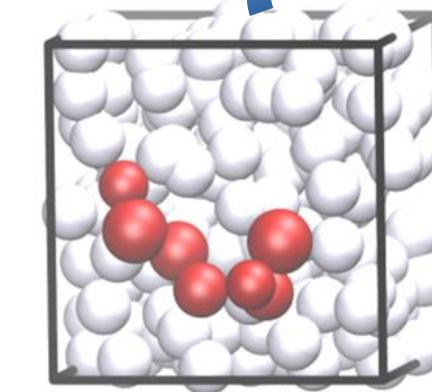
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Auhl et al, *J. Chem. Phys.* 2003

## Multiscale techniques:



microscopic description

## • Opportunities:

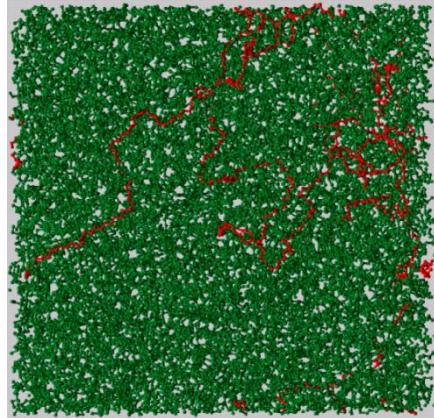
- Equilibrate samples of unprecedented size / chain length

# STRATEGIES FOR EQUILIBRATING LONG POLYMER MELTS



## □ Single-scale techniques:

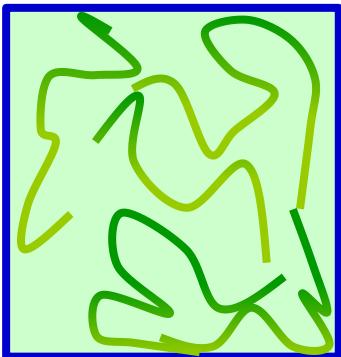
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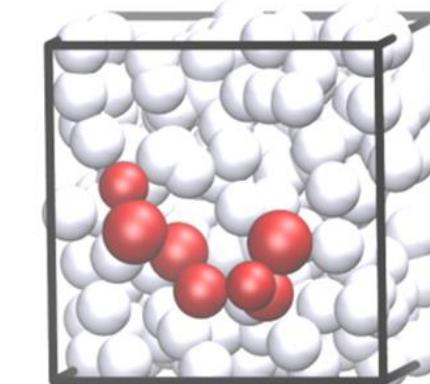
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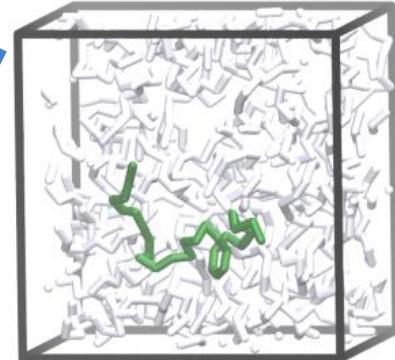
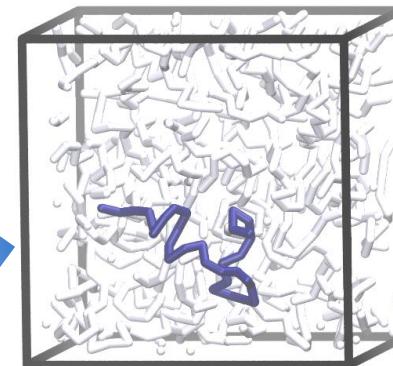
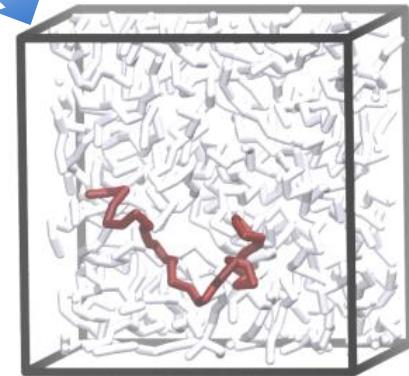
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Hou et al,  
*Phys. Rev. Lett.* 2010

Auhl et al, *J. Chem. Phys.* 2003

## □ Multiscale techniques:



universal blob model



chemically diverse materials

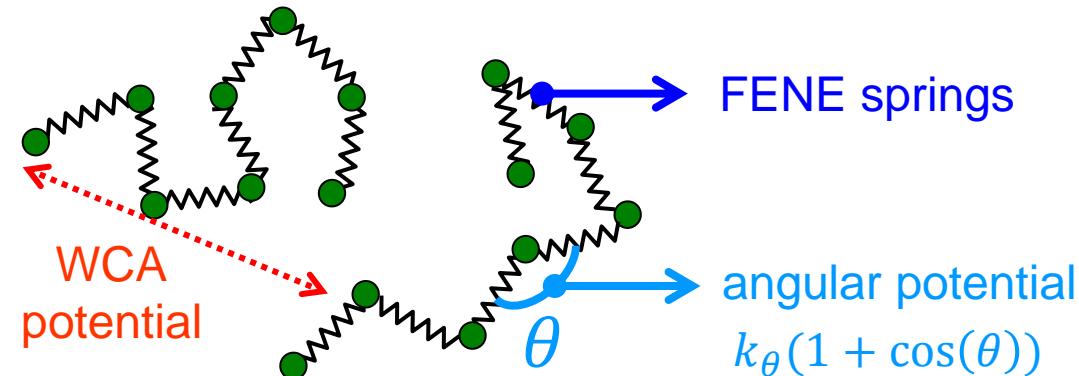
## • Opportunities:

- Equilibrate samples of unprecedented size / chain length
- Benefit from **universality**: “materials genomic” strategies

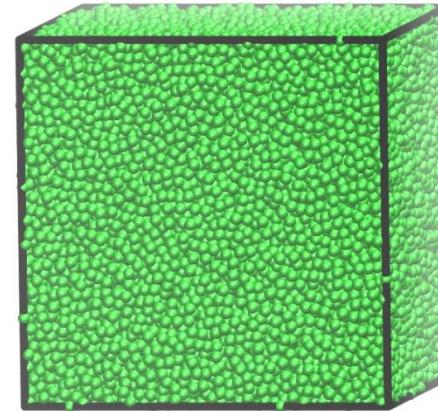
# MICROSCOPIC DESCRIPTIONS OF MELTS



## □ Generic:



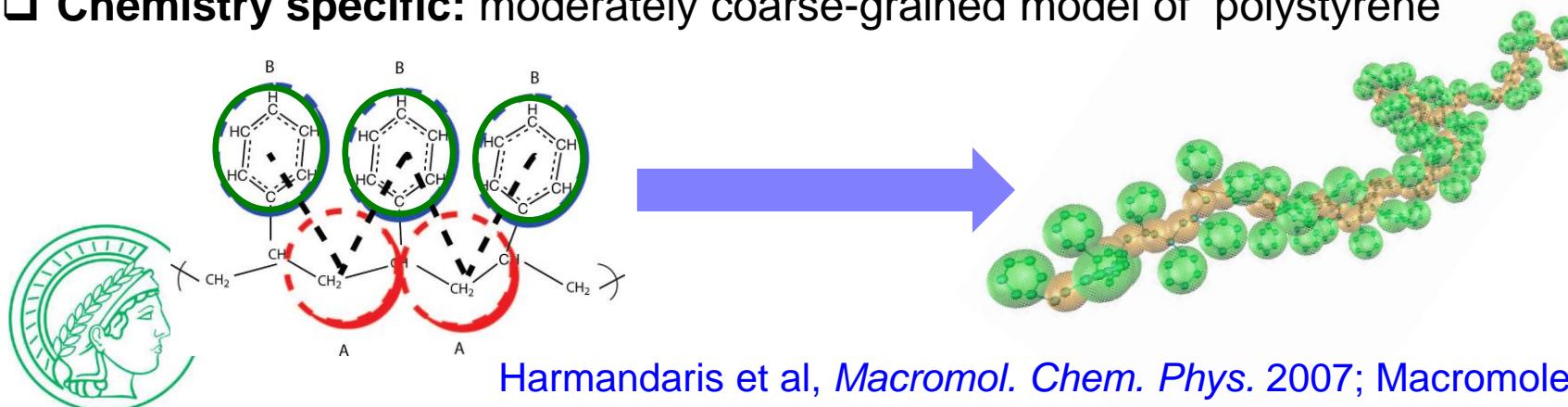
Kremer & Grest, *J. Chem. Phys.* 1990



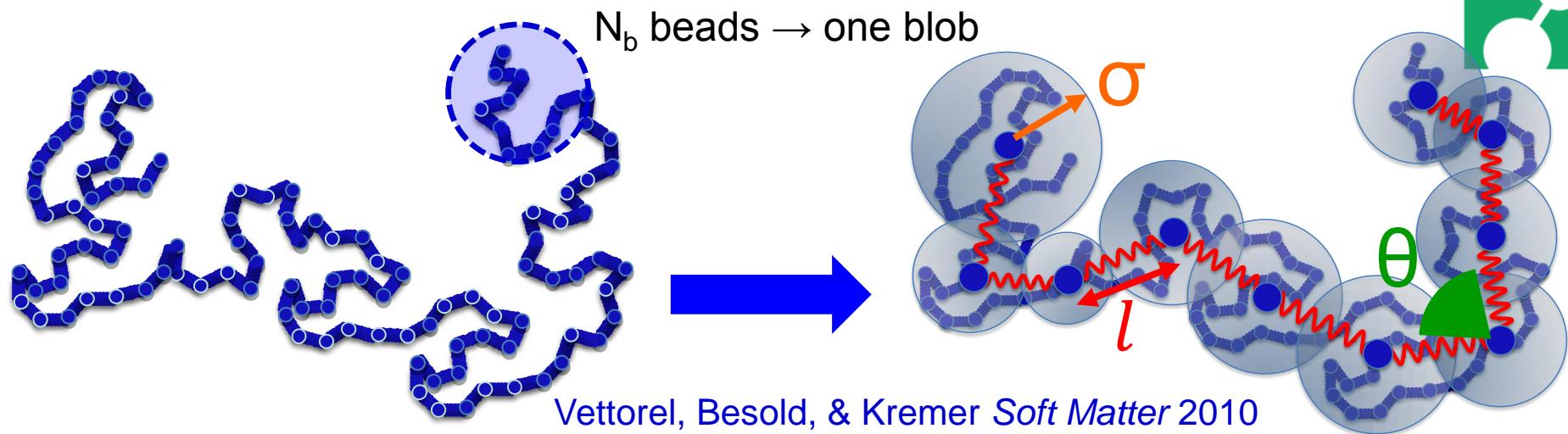
standard monomer density  
 $\sigma_0^3 \rho = 0.85$

- Model represents key features of real melts:
  - Strong covalent bonds, hard excluded volume, high density
- Tool for understanding fundamentals of polymer physics, **especially rheology**

## □ Chemistry specific: moderately coarse-grained model of polystyrene



# MAPPING MICROSCOPIC MODELS ON BLOB REPRESENTATIONS



Blob size:



$$U_{sp} = a_1 \frac{N_b^2}{\sigma^3} + a_2 \frac{\sigma^2}{N_b}$$

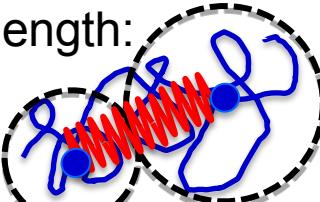
$$\left(\frac{N_b}{\sigma^3}\right)^2 \sigma^3$$

repulsive excluded volume interaction

$$\frac{\sigma^2}{N_b}$$

entropic cost of stretching the sub-chain

"Bond" length:



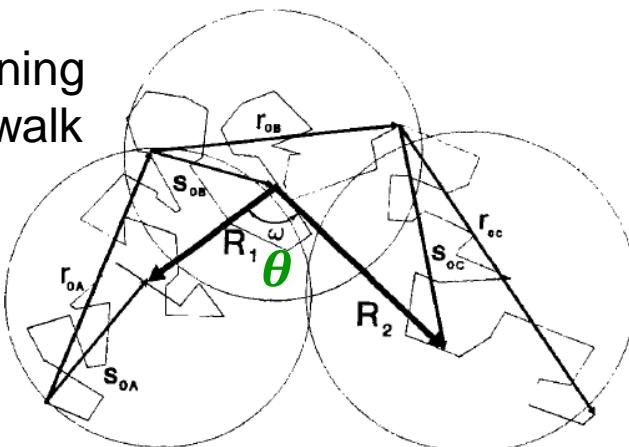
$$U_{bond} = \frac{k_{bond} l^2}{2}$$

coarse-graining a random walk

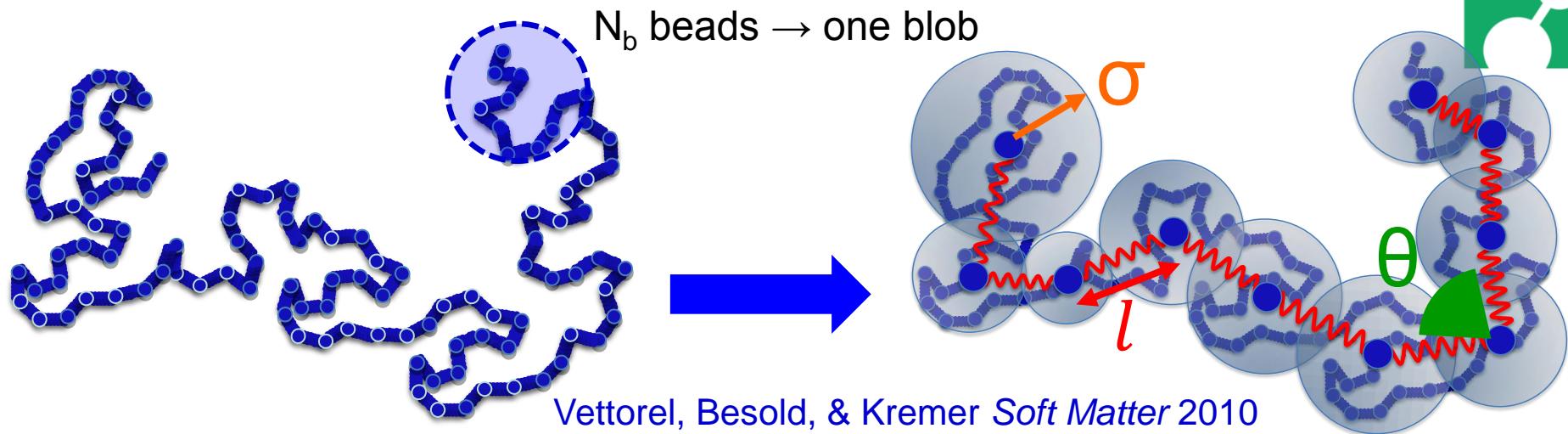
Angular correlation:

$$U_{ang} = k_\theta (1 + \cos(\theta))$$

Laso et al, *J. Chem. Phys.* 1991



# MAPPING MICROSCOPIC MODELS ON BLOB REPRESENTATIONS

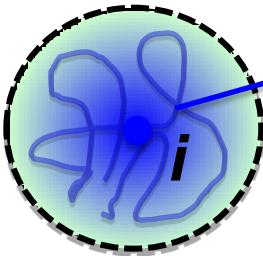


Blob size:



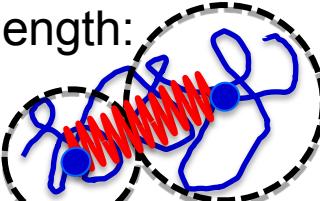
$$U_{sp} = a_1 \frac{N_b^2}{\sigma^3} + a_2 \frac{\sigma^2}{N_b}$$

Each blob assigned:



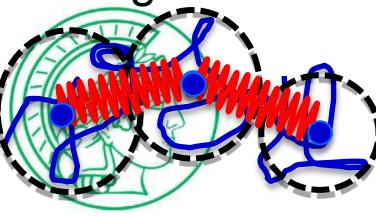
Gaussian density  
cloud  $\rho_i(\mathbf{r})$  of variance  $\sigma$

"Bond" length:



$$U_{bond} = \frac{k_{bond} l^2}{2}$$

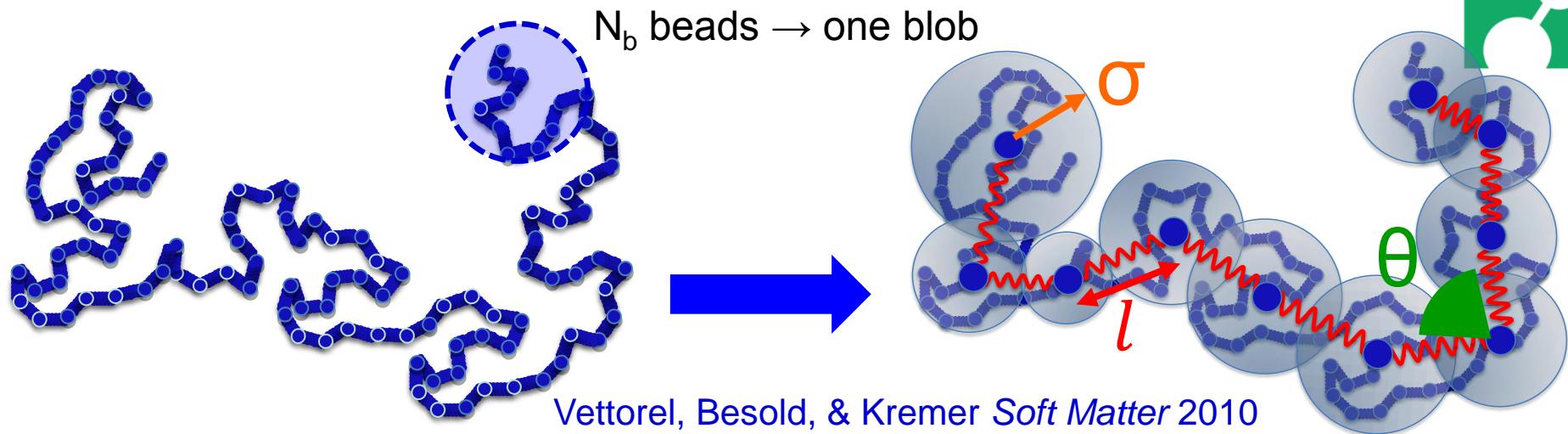
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# MAPPING MICROSCOPIC MODELS ON BLOB REPRESENTATIONS

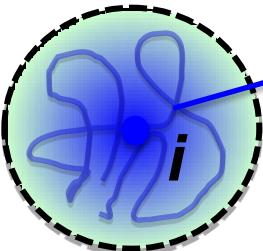


Blob size:



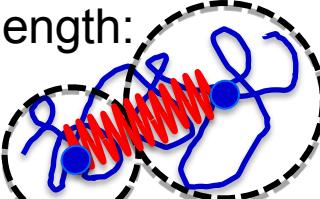
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Each blob assigned:



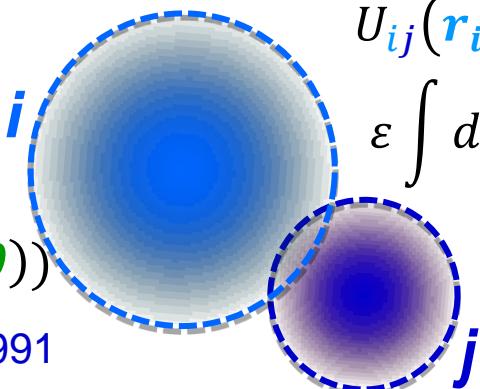
Gaussian density  
cloud  $\rho_i(\mathbf{r})$  of variance  $\sigma$

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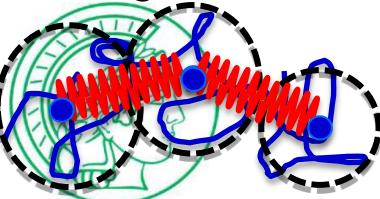
$$U_{bond} = \frac{k_{bond} l^2}{2}$$

Repulsion of two blobs:



$$U_{ij}(\mathbf{r}_i - \mathbf{r}_j) = \varepsilon \int d\mathbf{r} \rho_i(\mathbf{r}_i - \mathbf{r}) \rho_j(\mathbf{r}_j - \mathbf{r})$$

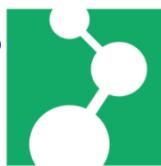
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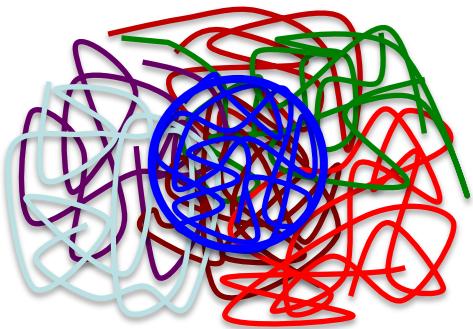
# EFFICIENT MONTE CARLO METHOD FOR BLOB-BASED MODELS



□ Blob-based models can be considered with standard techniques

- Monte Carlo using:  $U_{sp}$ ,  $U_{bond}$ ,  $U_{ang}$ , and  $U_{ij}$

However: Higher molecular weights → more “drastic” coarse-graining → larger  $N_b$



- Number of interacting soft spheres increases

$$\sqrt{N} = \frac{n_{subchains}}{V} R_{chains}^3 \sim \rho_o \sqrt{N_b}$$

→ more interacting neighbors → less efficiency !!!

□ Rewriting non-bonded interactions as a functional of collective variables allows for an efficient simulation scheme **without neighbor-lists**

- Collective variables:

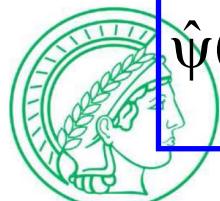
$$\hat{\phi}(\mathbf{r}) = \sum_{i=1}^{all \text{ spheres}} \rho_i(\mathbf{r})$$
$$\hat{\psi}(\mathbf{r}) = \sqrt{\sum_{i=1}^{all \text{ spheres}} \rho_i^2(\mathbf{r})}$$

- Non-bonded interactions:

$$H_{nb} = \frac{1}{2} \sum_{i=1}^{all \text{ spheres}} \sum_{j=1}^{all \text{ spheres}} U_{ij}(\mathbf{r}_i - \mathbf{r}_j)$$

Equivalent to the functional:

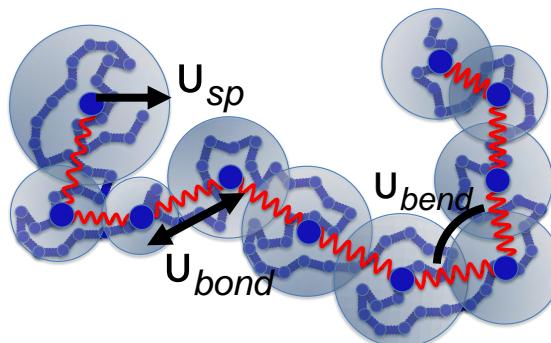
$$H_{nb} = \frac{\varepsilon}{2} \int [\hat{\phi}^2(\mathbf{r}) - \hat{\psi}^2(\mathbf{r})] d\mathbf{r}$$



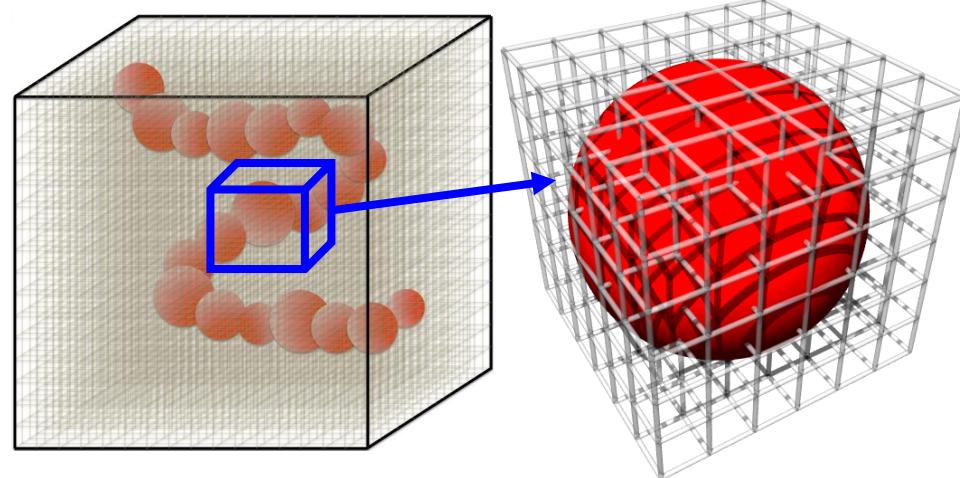
# EFFICIENT MONTE CARLO METHOD FOR BLOB-BASED MODELS



- Bonded interactions:  
use explicit potentials



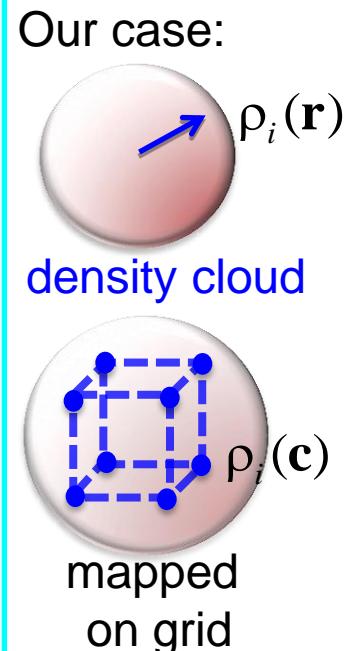
- Non-bonded interactions:
  - Introduce high-resolution mesh



- Map the Gaussian density cloud of each sphere on the grid-nodes
- Density distribution of configuration calculated:

$$\hat{\phi}(\mathbf{c}) = \sum_{i=1}^{all \text{ } spheres} \rho_i(\mathbf{c})$$

$$\hat{\psi}(\mathbf{c}) = \sqrt{\sum_{i=1}^{all \text{ } spheres} \rho_i^2(\mathbf{c})}$$



Typical PM:  
*Hockney & Eastwood Computer Simulation Using Particles IOP 1988*



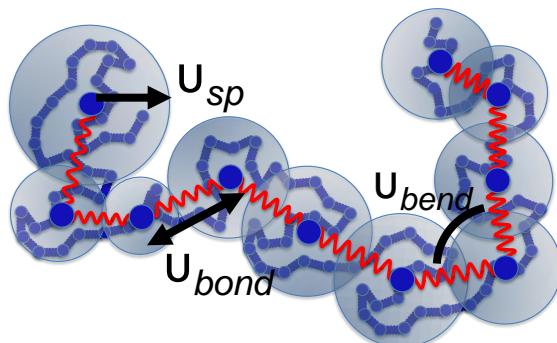
- Non-bonded energy:

$$H_{nb} = \frac{\epsilon}{2} \sum_{c=1}^{ncells} [\hat{\phi}^2(\mathbf{c}) - \hat{\psi}^2(\mathbf{c})] \Delta L^3$$

# EFFICIENT MONTE CARLO METHOD FOR BLOB-BASED MODELS

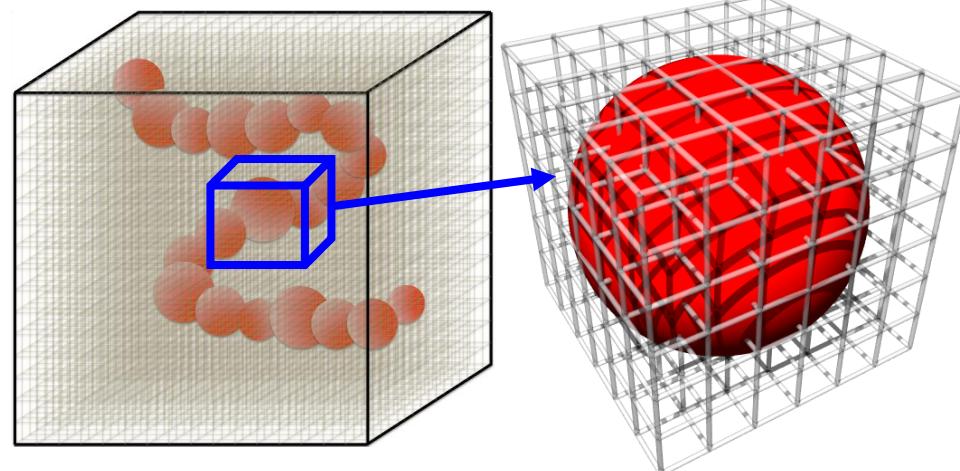


- Bonded interactions:  
use explicit potentials



Energy  
changes obtained  
from density changes

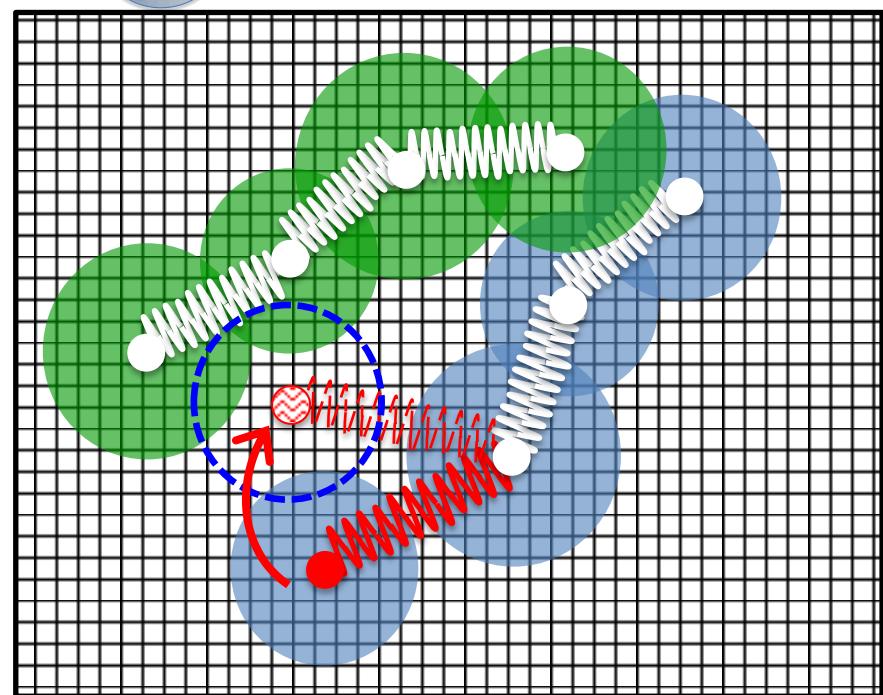
- Non-bonded interactions:
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- Map the Gaussian density cloud of each sphere on the grid-nodes
- Density distribution of configuration calculated:

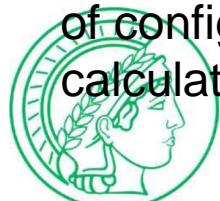
$$\hat{\phi}(\mathbf{c}) = \sum_{i=1}^{\text{all spheres}} \rho_i(\mathbf{c})$$

$$\hat{\psi}(\mathbf{c}) = \sqrt{\sum_{i=1}^{\text{all spheres}} \rho_i^2(\mathbf{c})}$$

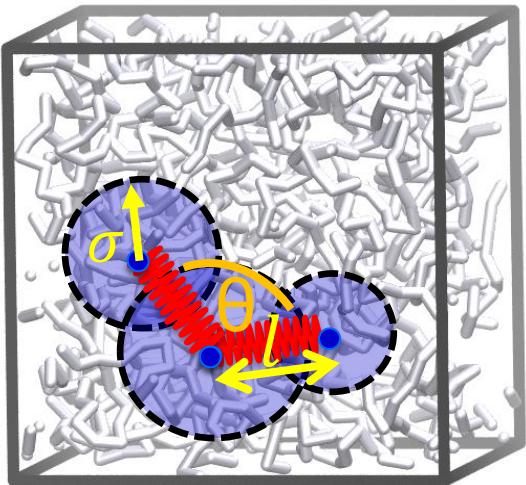


- Non-bonded energy:

$$H_{nb} = \frac{\epsilon}{2} \sum_{c=1}^{ncells} [\hat{\phi}^2(\mathbf{c}) - \hat{\psi}^2(\mathbf{c})] \Delta L^3$$

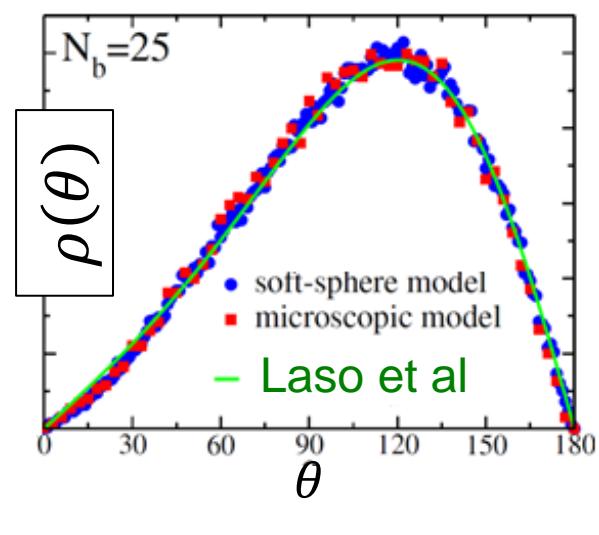
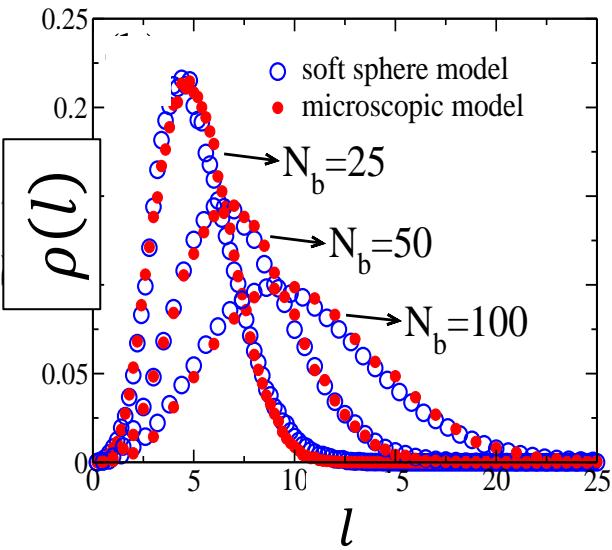
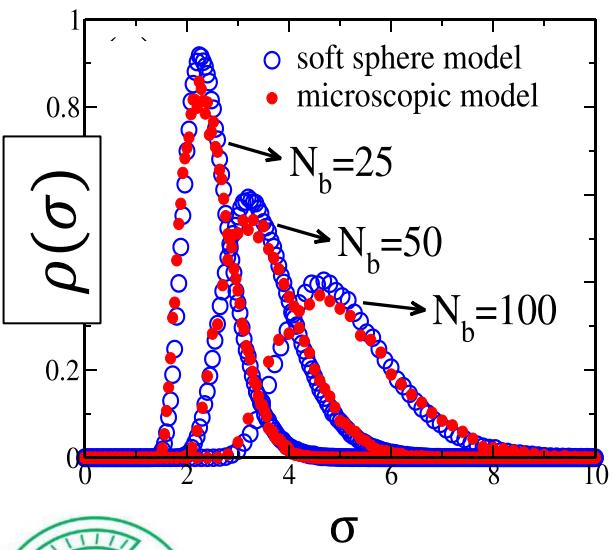


# PARAMETERIZATION OF BLOB-BASED MODEL



- Parameters tuned to reproduce **local** blob properties in **reference** samples described with the microscopic model
- Examples:
  - Distributions:  $\rho(\sigma)$ ,  $\rho(l)$ ,  $\rho(\theta)$
  - Pair-correlation-function for blob centers,  $g(r)$

- Performance of blob-based model for **generic** melt:

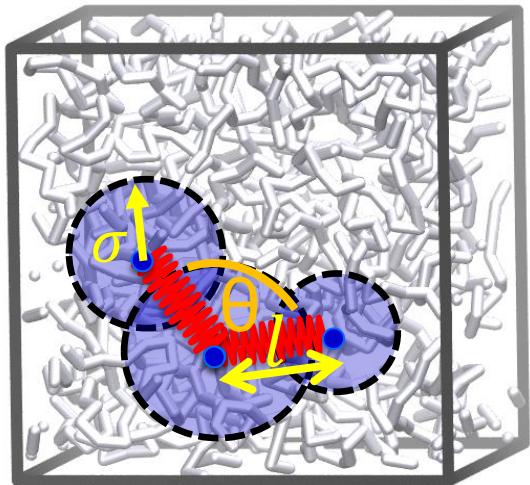


Zhang, Moreira, Stuehn, Daoulas, & Kremer ACS Macro Lett. 2014

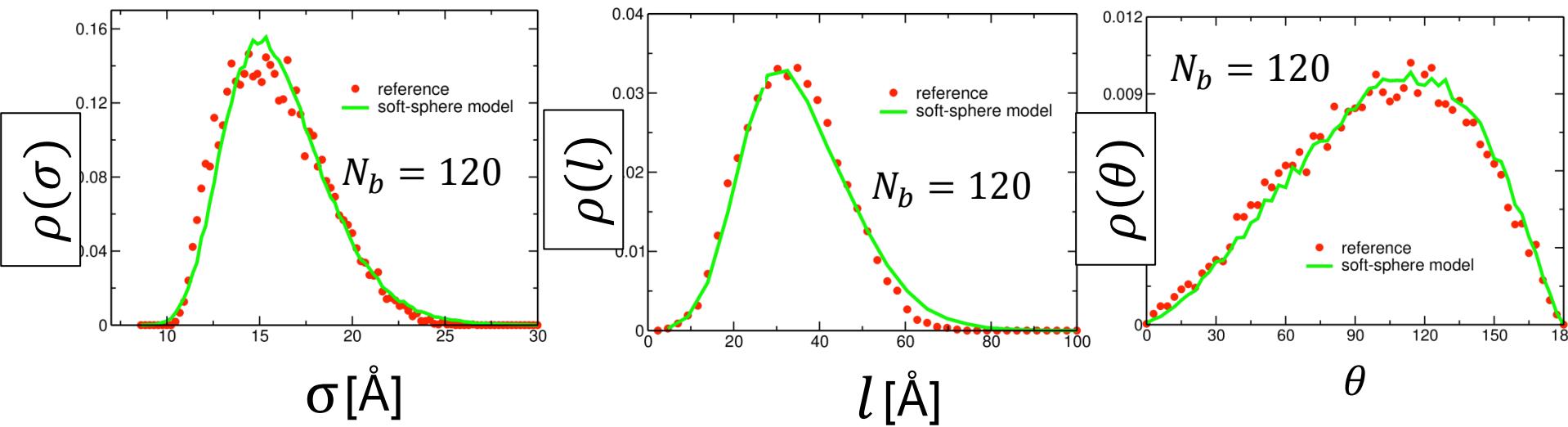
Zhang, Stuehn, Daoulas, & Kremer J. Chem. Phys. 2015



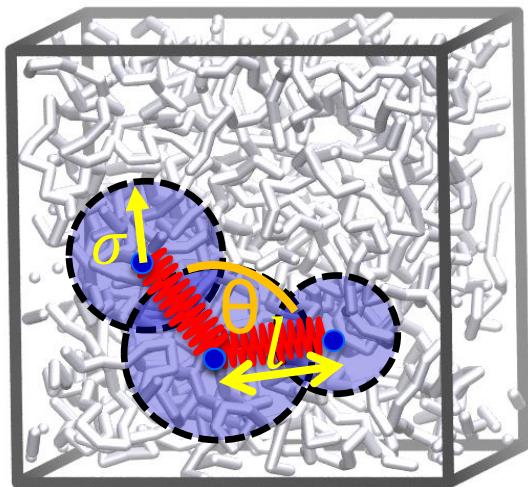
# PARAMETERIZATION OF BLOB-BASED MODEL



- Parameters tuned to reproduce **local** blob properties in **reference** samples described with the microscopic model
- Examples:
  - Distributions:  $\rho(\sigma)$ ,  $\rho(l)$ ,  $\rho(\theta)$
  - Pair-correlation-function for blob centers,  $g(r)$
- Performance of blob-based model for **polystyrene** melt:

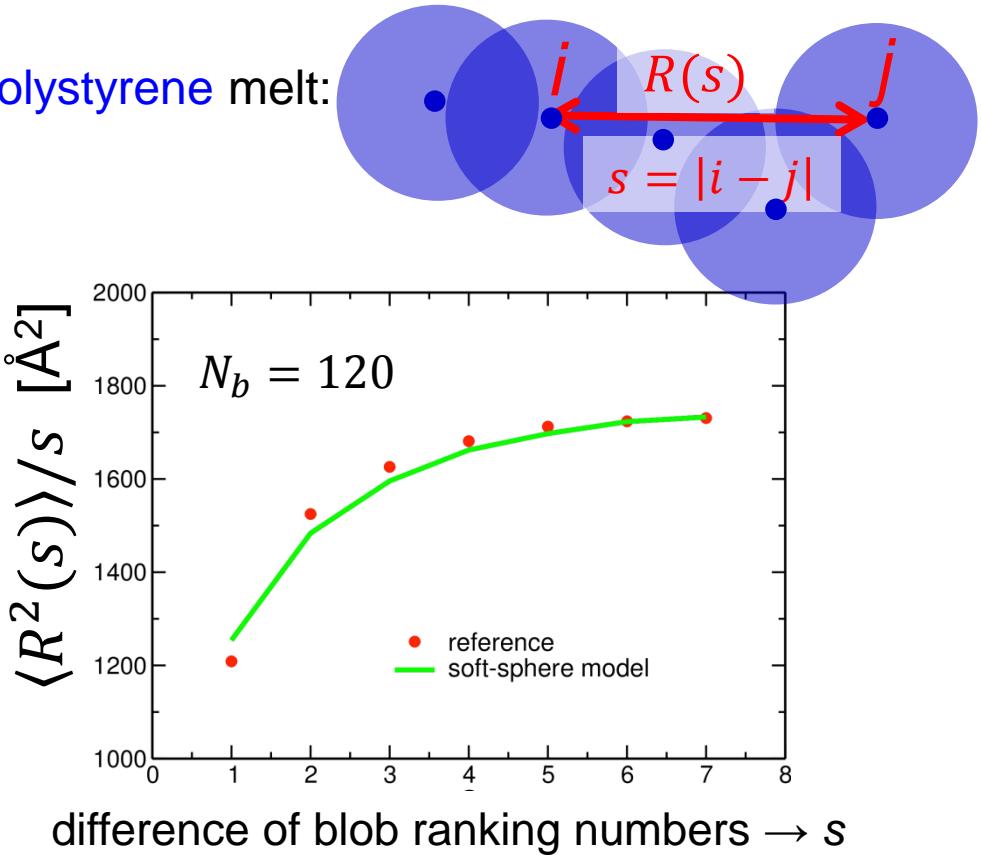
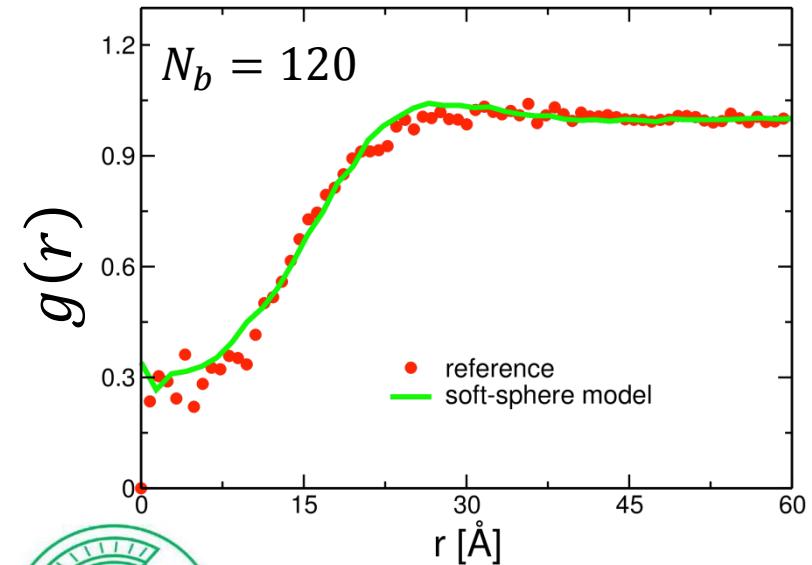


# BOTTOM-UP PARAMETERIZATION OF BLOB-BASED MODEL



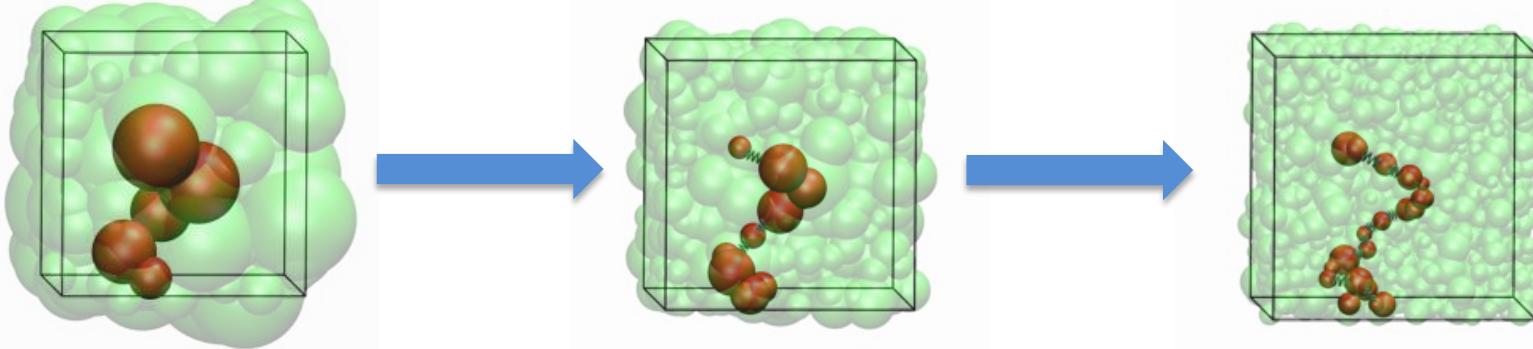
- Parameters tuned to reproduce **local** blob properties in **reference** samples described with the microscopic model
- Examples:
  - Distributions:  $\rho(\sigma)$ ,  $\rho(l)$ ,  $\rho(\theta)$
  - Pair-correlation-function for blob centers,  $g(r)$

- Performance of blob-based model for **polystyrene** melt:



# I. HIERARCHICAL BACK-MAPPING STRATEGY: FINE-GRAINING

Zhang, Moreira, Stuehn, Daoulas, & Kremer ACS Macro Lett. 2014



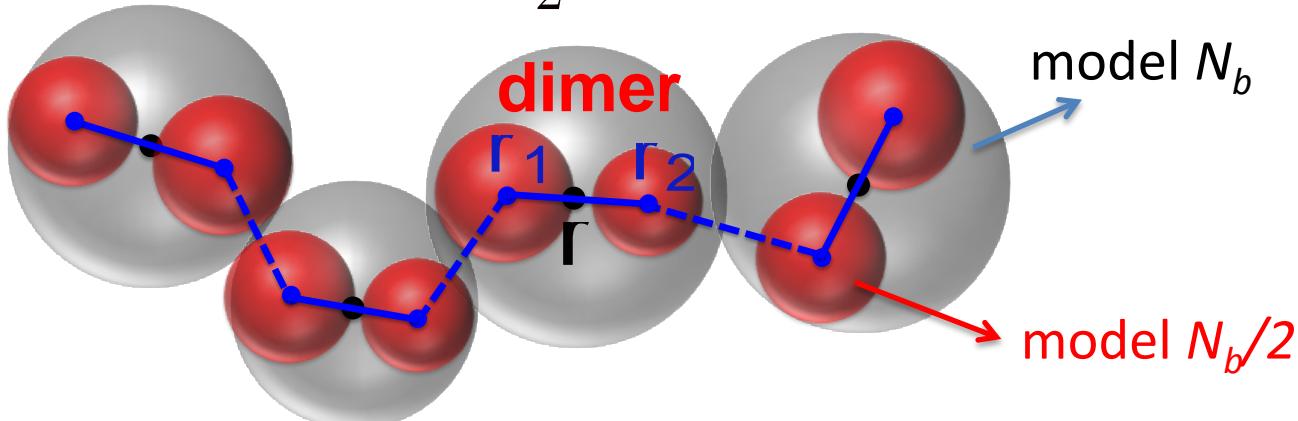
- Starting configuration equilibrated “from scratch”  
1 blob  $\rightarrow N_b$  beads

- Double resolution  
1 blob  $\rightarrow \frac{N_b}{2}$  beads

- Double resolution  
1 blob  $\rightarrow \frac{N_b}{4}$  beads

- Fine-graining concept:

$$\mathbf{r} = \frac{1}{2}(\mathbf{r}_1 + \mathbf{r}_2)$$



→ Relaxation time of smaller blobs is short  $\sim$  Rouse time of dimer

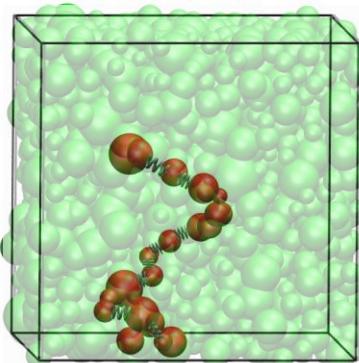


## II. HIERARCHICAL BACK-MAPPING STRATEGY: REINSERTION

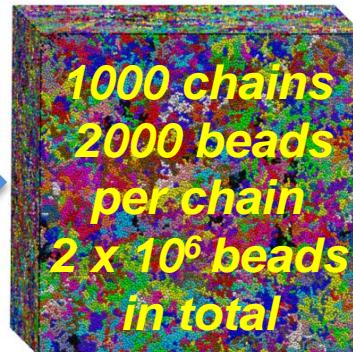
Zhang, Moreira, Stuehn, Daoulas, & Kremer ACS Macro Lett. 2014



small blobs,  
e.g., 1 blob: 25 beads

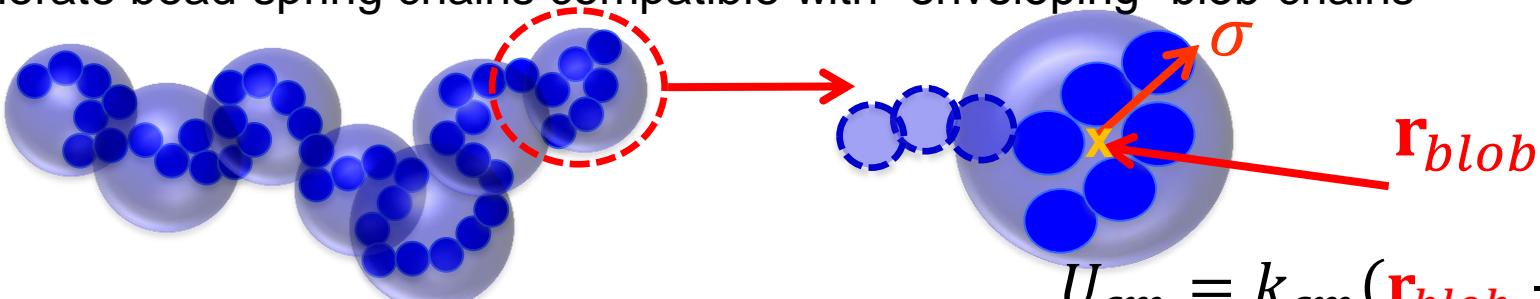


???



underlying  
microscopic  
configuration

- Generate bead-spring chains compatible with “enveloping” blob-chains

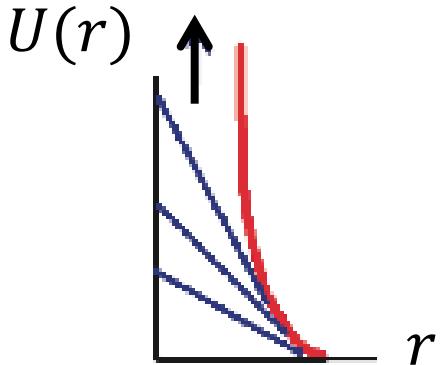
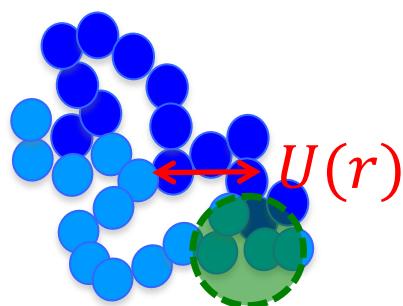


- Each sub-chain subjected to pseudopotentials:
- No intrachain correlations
- No intermolecular correlations

$$U_{cm} = k_{cm} (\mathbf{r}_{blob} - \mathbf{R}_{cm})^2$$
$$U_g = k_g (\sigma - R_g^2)^2$$

- Introduce slowly excluded volume removing monomer overlaps

Auhl et al. J. Chem. Phys. 2003

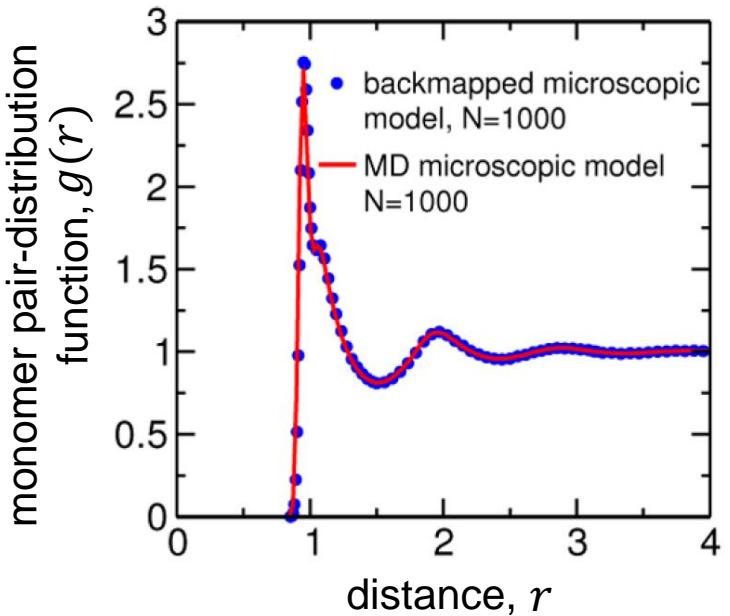


# VERIFYING EQUILIBRATION OF MELTS OF LONG POLYMERS

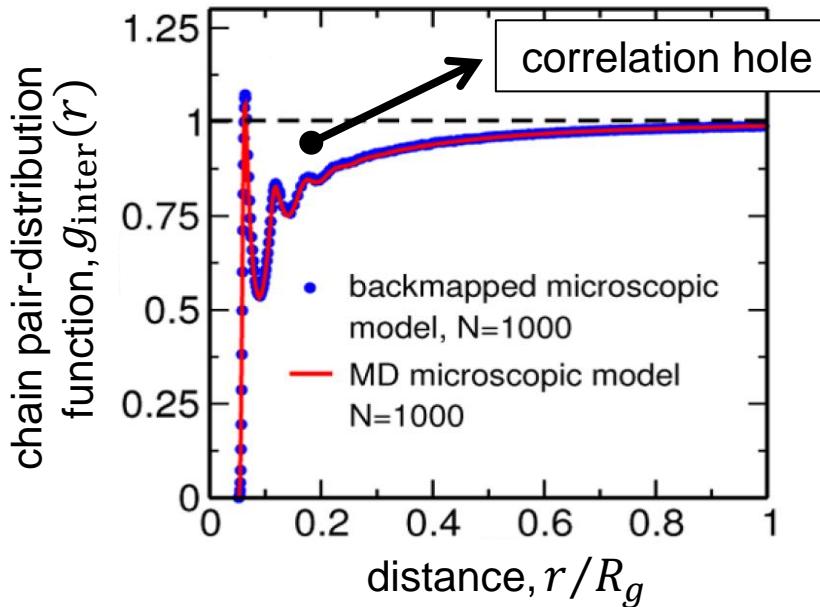


- Local liquid structure:

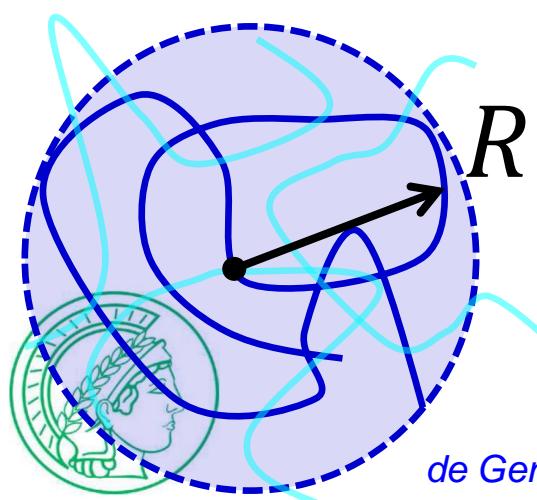
Generic melt:



- Long-wavelength liquid structure:



- Correlation hole → “packing” of polymer molecules



Due to connectivity monomers of same chain are close by →

Liquid has fixed density → monomers of other chains expelled

$$g_{\text{inter}}(\text{small } r) \sim \frac{(n-1)N}{R^3 \text{ bulk density}} = 1 - \frac{N}{R^3 \text{ bulk density}}$$

$$\frac{R^3 \text{ bulk density}}{N} \equiv \sqrt{N}$$

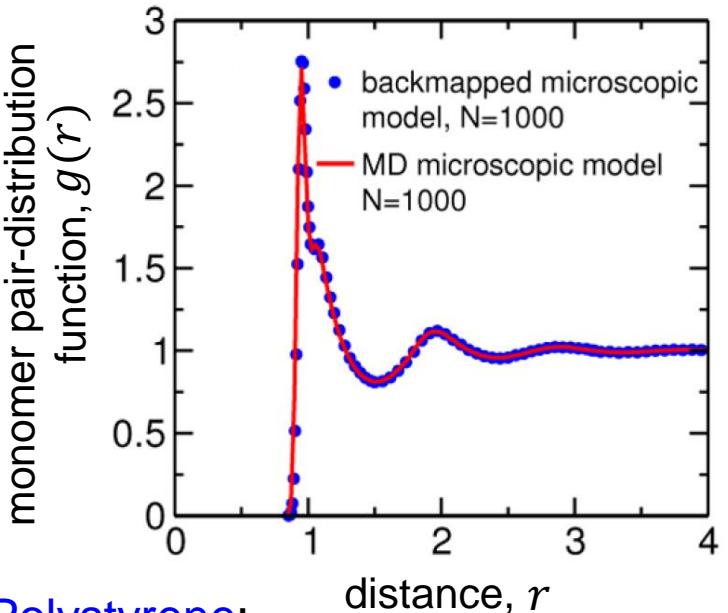
$$g_{\text{inter}}(\text{small } r) \sim 1 - \frac{1}{\sqrt{N}}$$

# VERIFYING EQUILIBRATION OF MELTS OF LONG POLYMERS



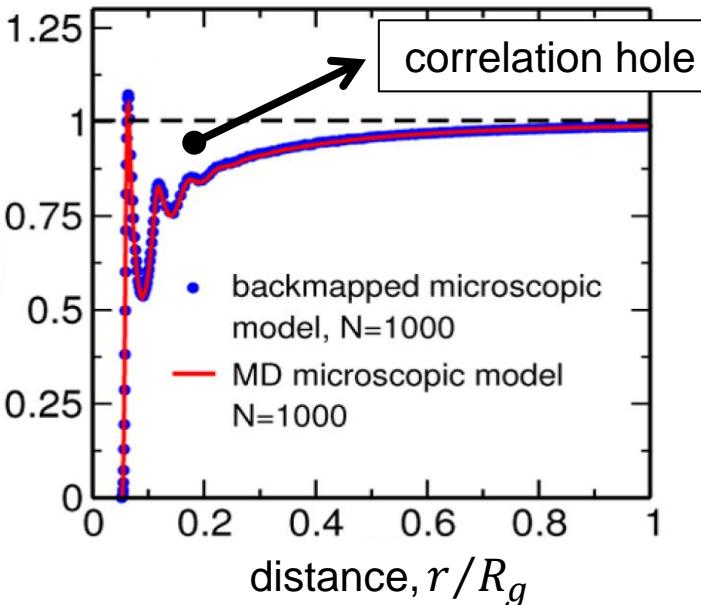
Local liquid structure:

Generic melt:

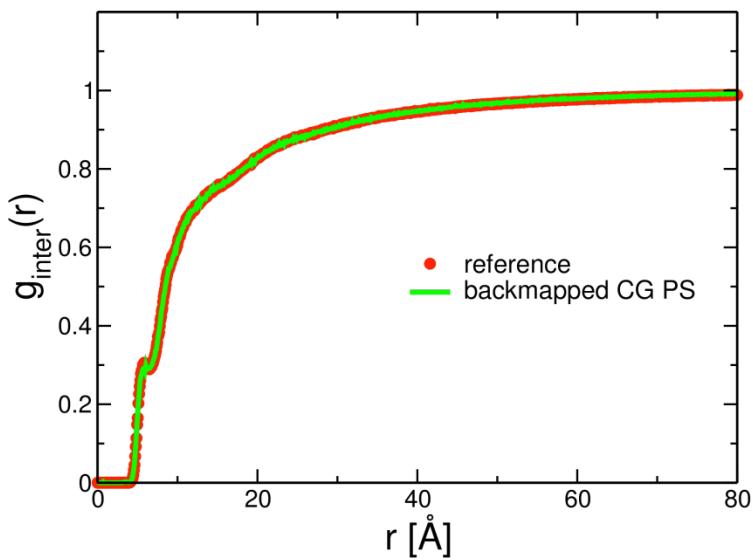
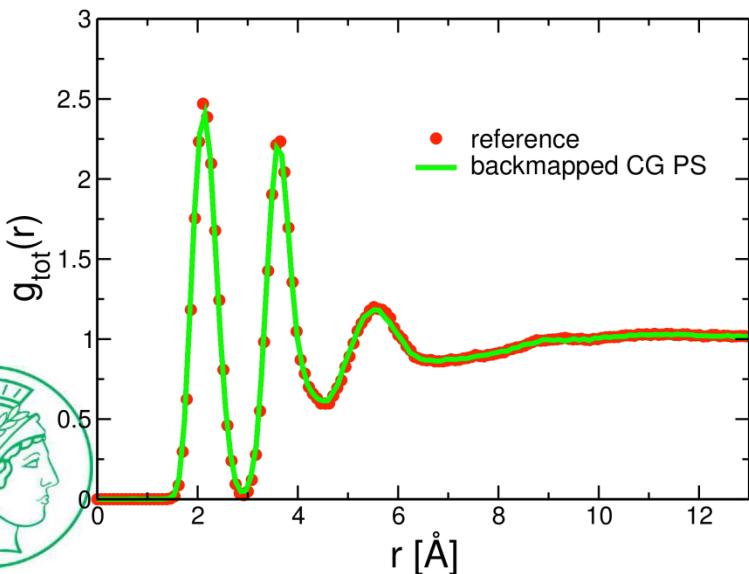


Long-wavelength liquid structure:

chain pair-distribution function,  $g_{\text{inter}}(r)$



Polystyrene:

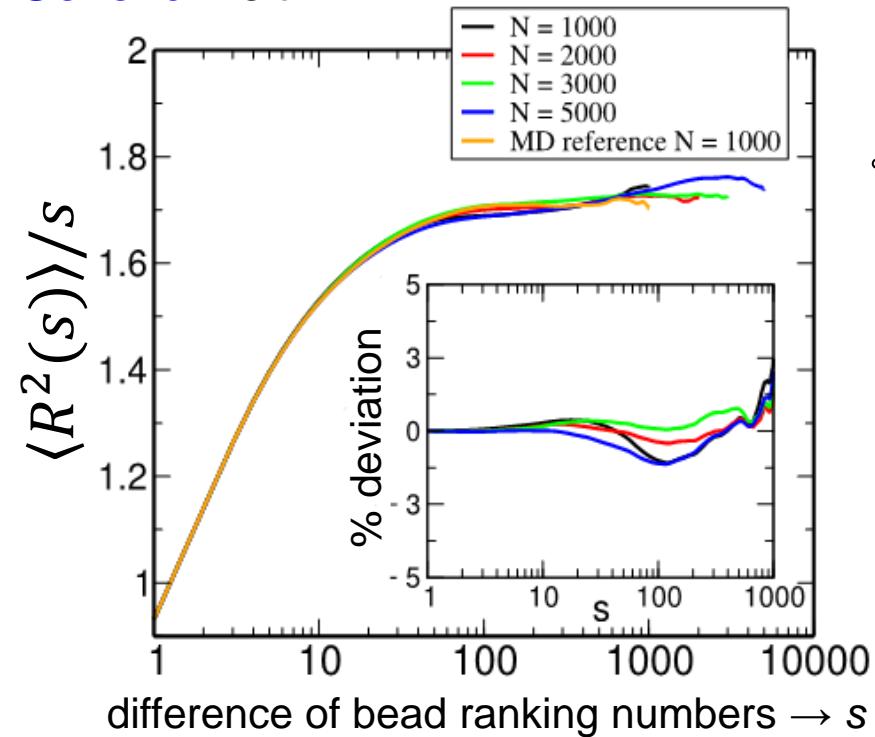


# VERIFYING EQUILIBRATION OF MELTS OF LONG POLYMERS

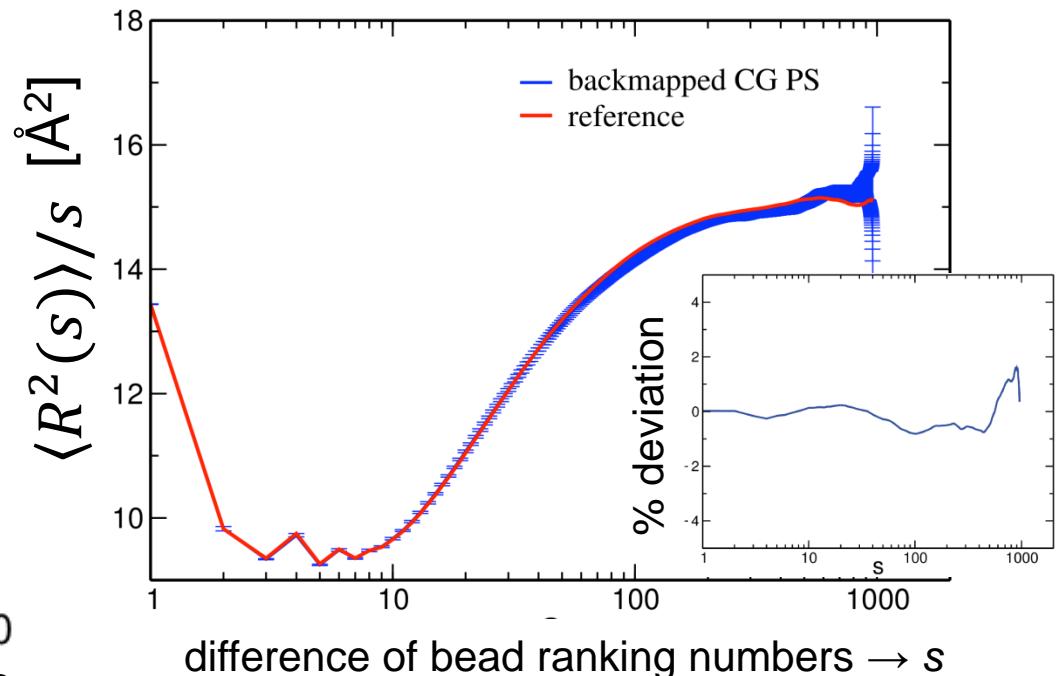


- ☐ Chain conformations:

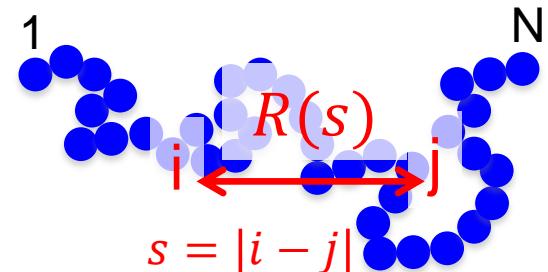
Generic melt:



Polystyrene:

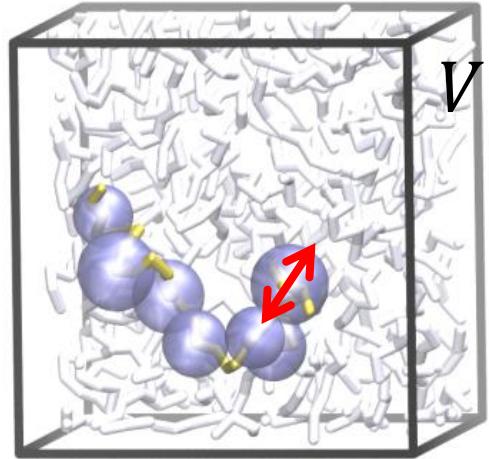


- ☐ Internal distance plots highlight excellent equilibration
- ☐ The method equilibrates samples with more than 1000 chains and N = 5000



For generic model representative computation time ~ 6 days on 32 processors  
 For polystyrene model, complexity raises computation time by an order of magnitude

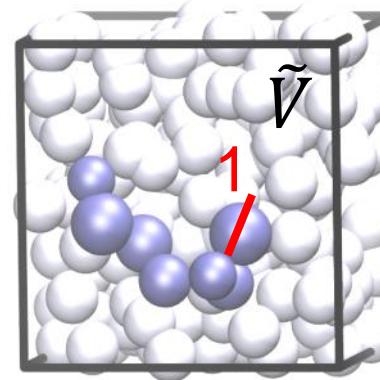
# UNIVERSAL BLOB-BASED REPRESENTATION OF MELTS



coarse  
graining  
scale  
 $\Delta L$

renormalization

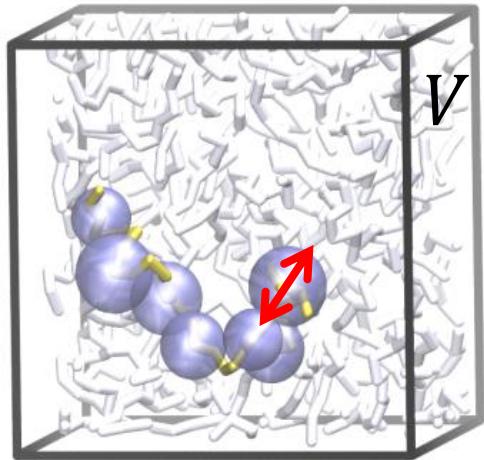
$$\mathbf{r}/\Delta L$$



$N_{CG}$  blobs in a chain



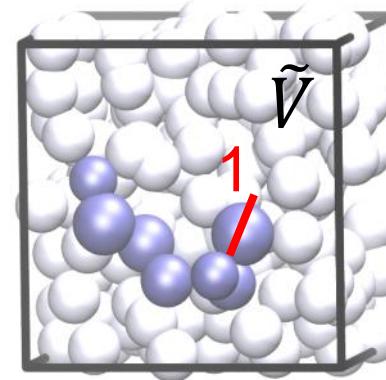
# UNIVERSAL BLOB-BASED REPRESENTATION OF MELTS



renormalization

$$\mathbf{r}/\Delta L$$

coarse  
graining  
scale  
 $\Delta L$



$N_{CG}$  blobs in a chain

□ Different melts map on the same renormalized blob representation when:

A) For each melt  $\Delta L$  chosen so that chains have  $N_{CG}$  blobs

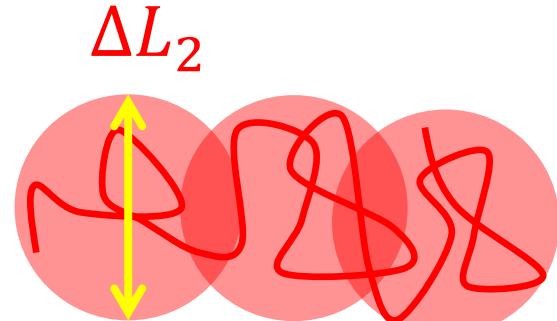
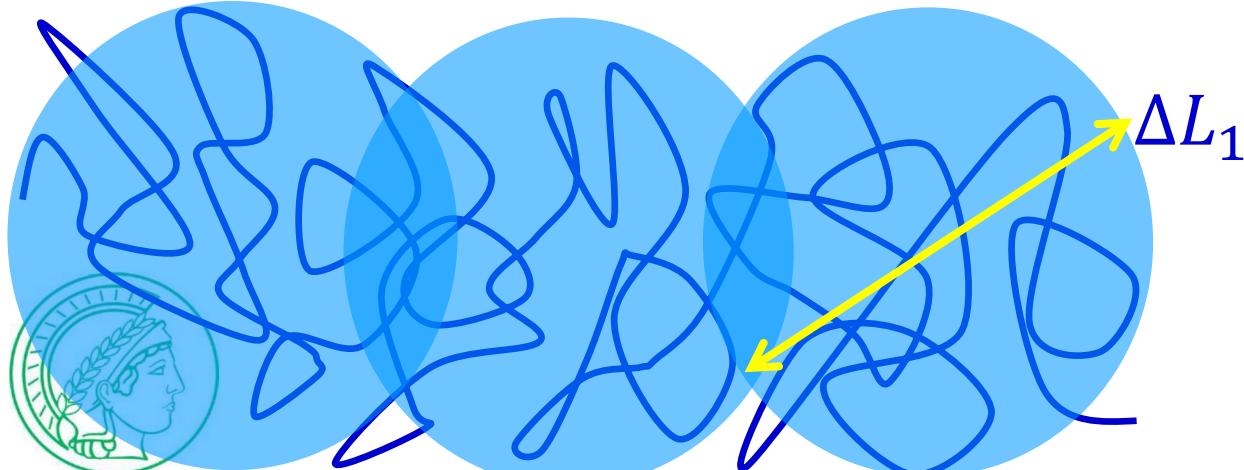
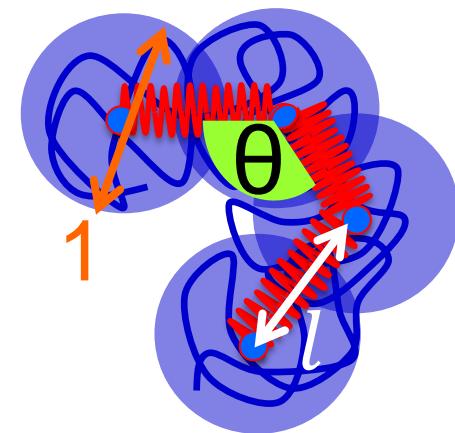
universal  
distributions  
 $\rho(\theta)$     $\rho(l)$



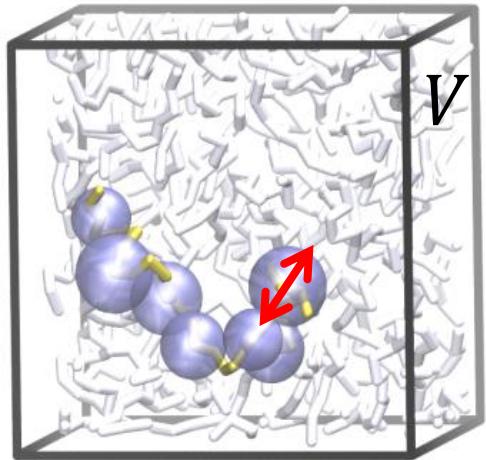
same  
 $N_{CG}$

= same  
conformations

Laso et al, *J. Chem. Phys.* 1991



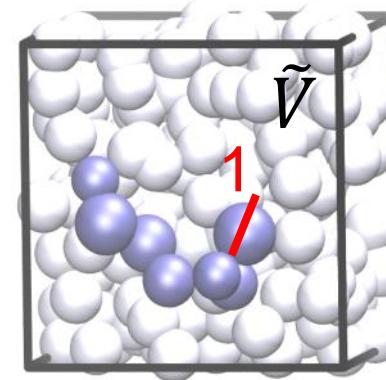
# UNIVERSAL BLOB-BASED REPRESENTATION OF MELTS



renormalization

$$\mathbf{r}/\Delta L$$

coarse  
graining  
scale  
 $\Delta L$



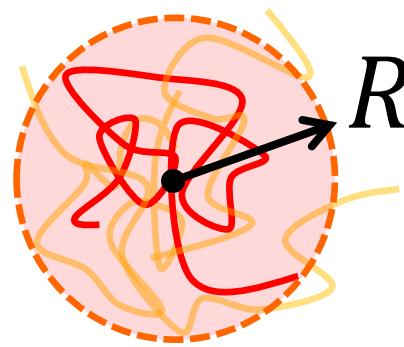
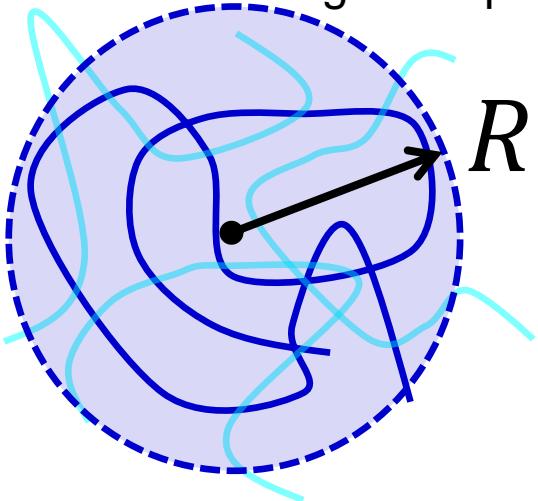
$N_{CG}$  blobs in a chain

□ Different melts map on the same renormalized blob representation when:

B) Melts have the same invariant degree of polymerization  $\bar{N}$

$$\sqrt{\bar{N}} = nR^3/V$$

quantifies  
chain overlap



same liquid structure

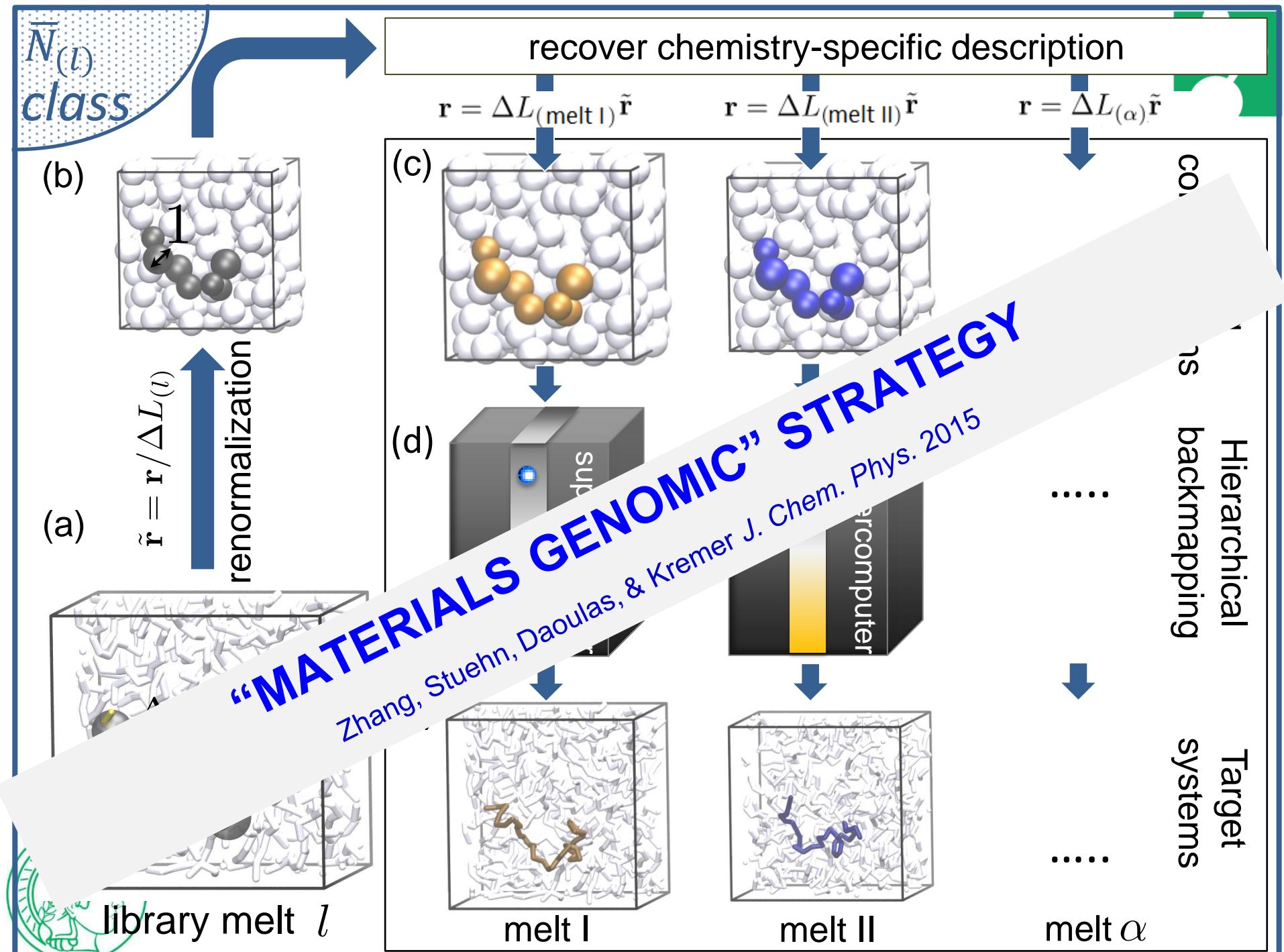


$$N_{CG} \Rightarrow$$

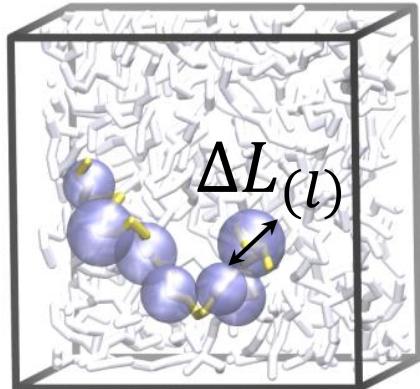
blobs have  
the same

$$\bar{N}_b \Rightarrow$$

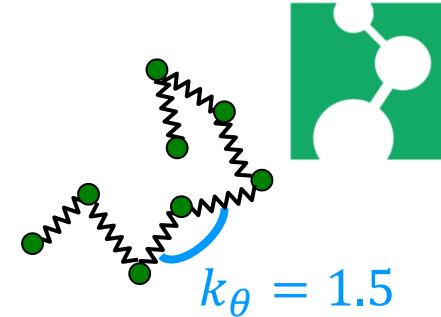
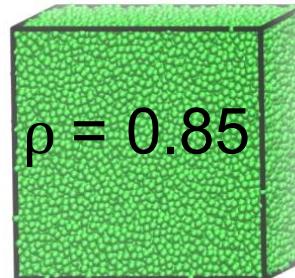
$$g_{CG}(\tilde{r}) = 1 - \frac{1}{\sqrt{\bar{N}_b}} X_o(\tilde{r}, N_{CG})$$



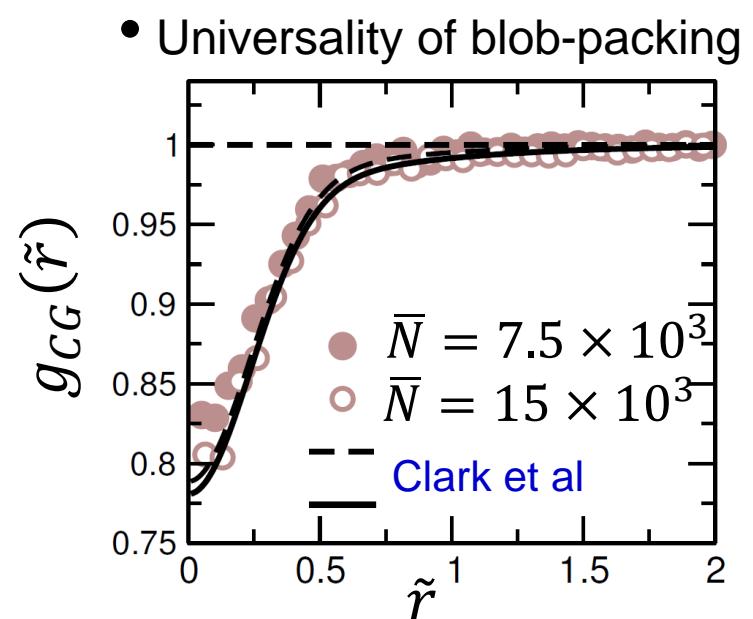
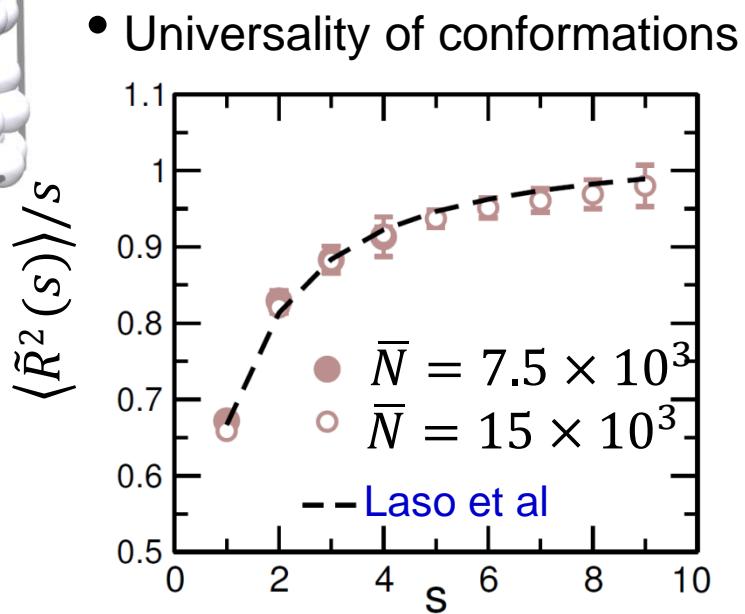
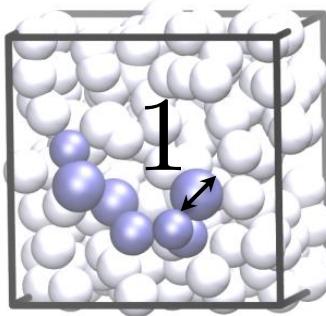
# PROOF-OF-PRINCIPLE



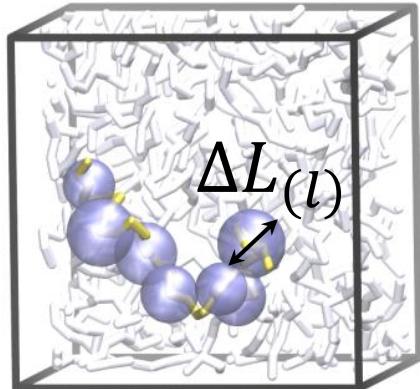
- All library melts →  
Same “chemical” substance  
 $\bar{N} = 7.5 \times 10^3$   
 $\bar{N} = 15 \times 10^3$



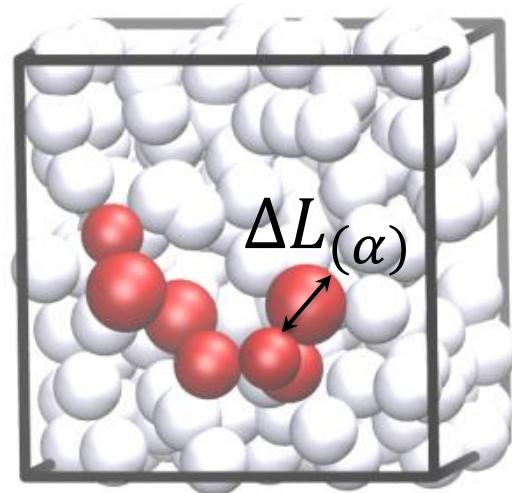
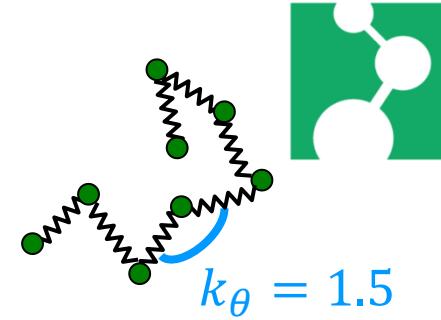
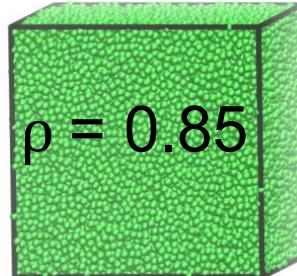
- Universal blob-based description exists:



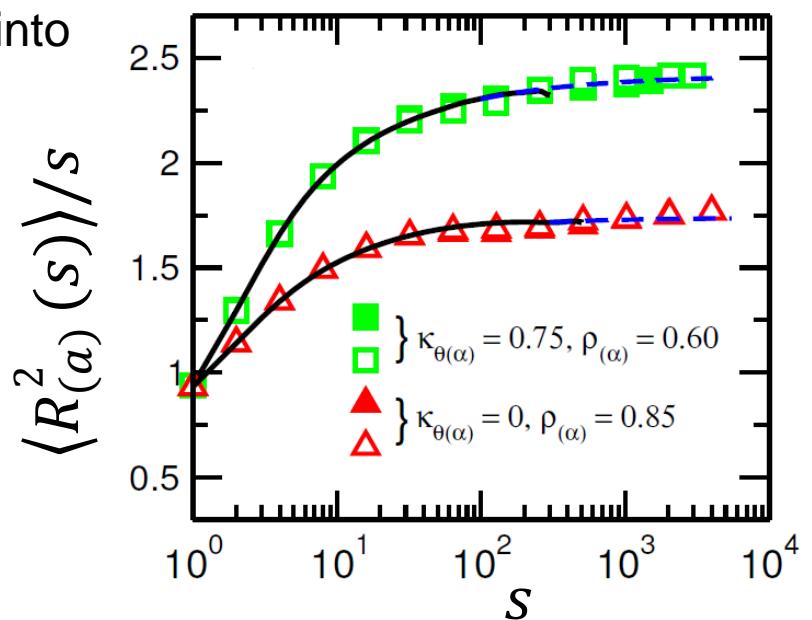
# PROOF-OF-PRINCIPLE



- All library melts →  
Same “chemical” substance  
 $\bar{N} = 7.5 \times 10^3$   
 $\bar{N} = 15 \times 10^3$



- Convert library melts into  
“different” materials:



# EQUILIBRATED SAMPLES ARE STARTING-POINT FOR COMPUTATIONAL RHEOLOGICAL “EXPERIMENTS”

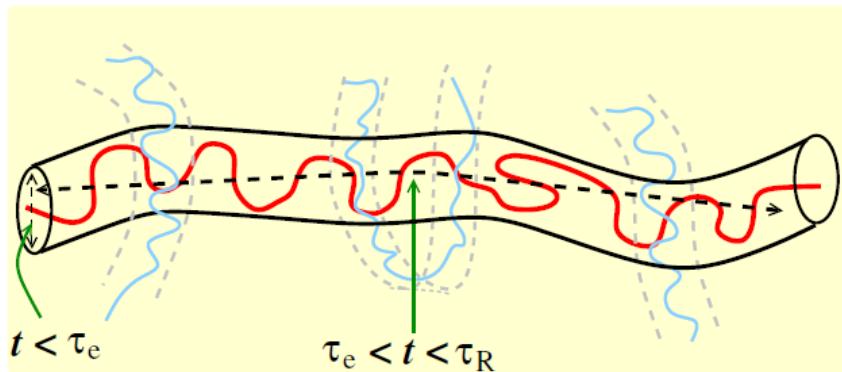


□ Simple illustration:

Equilibrium chain dynamics in highly entangled regime

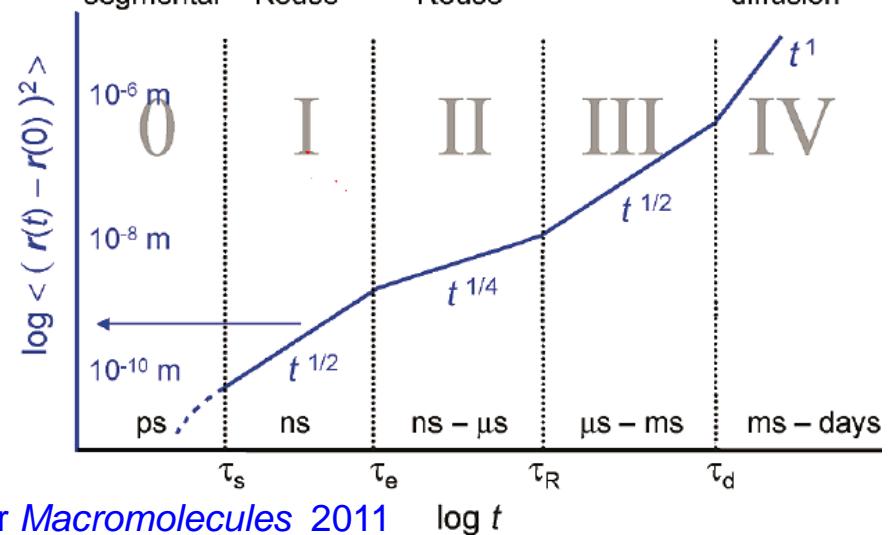
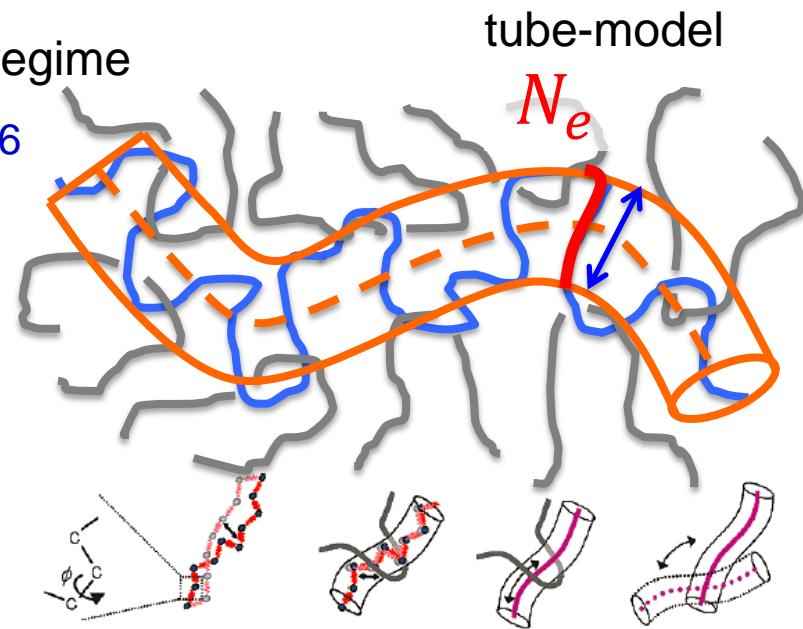
Doi & Edwards, *The Theory of Polymer Dynamics* 1986

Example: mean square monomer displacement



$$g_1(t) \sim \begin{cases} t^{1/2} & \text{for } t \leq \tau_e \\ t^{1/4} & \text{for } \tau_e \leq t \leq \tau_R \\ t^{1/2} & \text{for } \tau_R \leq t \leq \tau_d \\ t & \text{for } \tau_d \leq t \end{cases}$$

Rubinstein & Colby, *Polymer Physics* 2003



Adapted from: Chávez & Saalwächter *Macromolecules* 2011



# EQUILIBRATED SAMPLES ARE STARTING-POINT FOR COMPUTATIONAL RHEOLOGICAL “EXPERIMENTS”

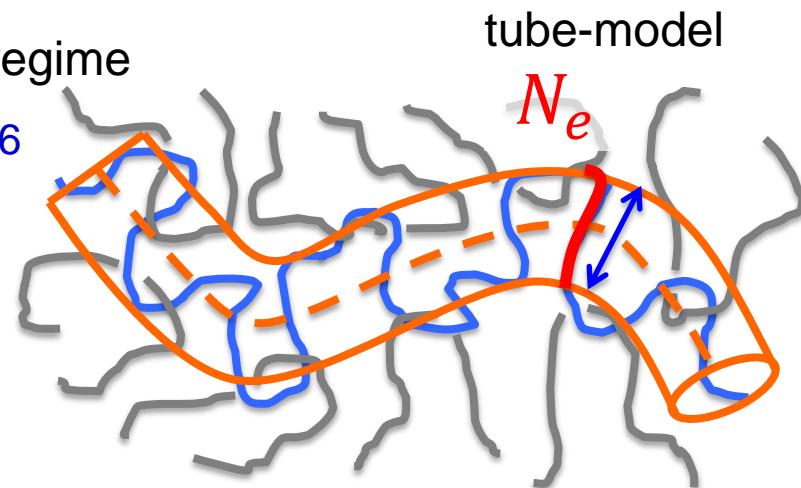
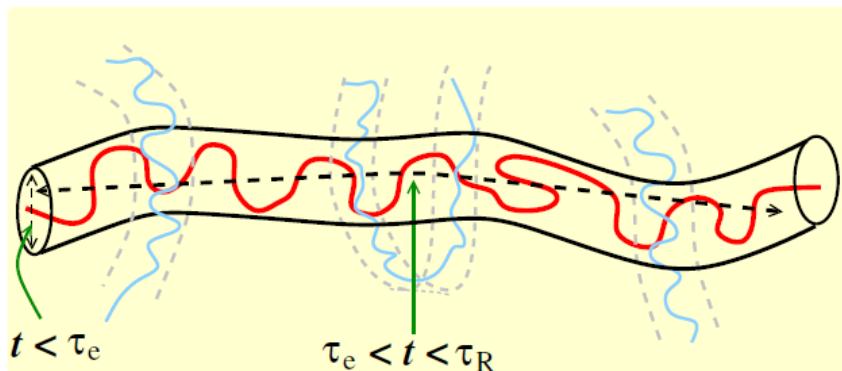


□ Simple illustration:

Equilibrium chain dynamics in highly entangled regime

Doi & Edwards, *The Theory of Polymer Dynamics* 1986

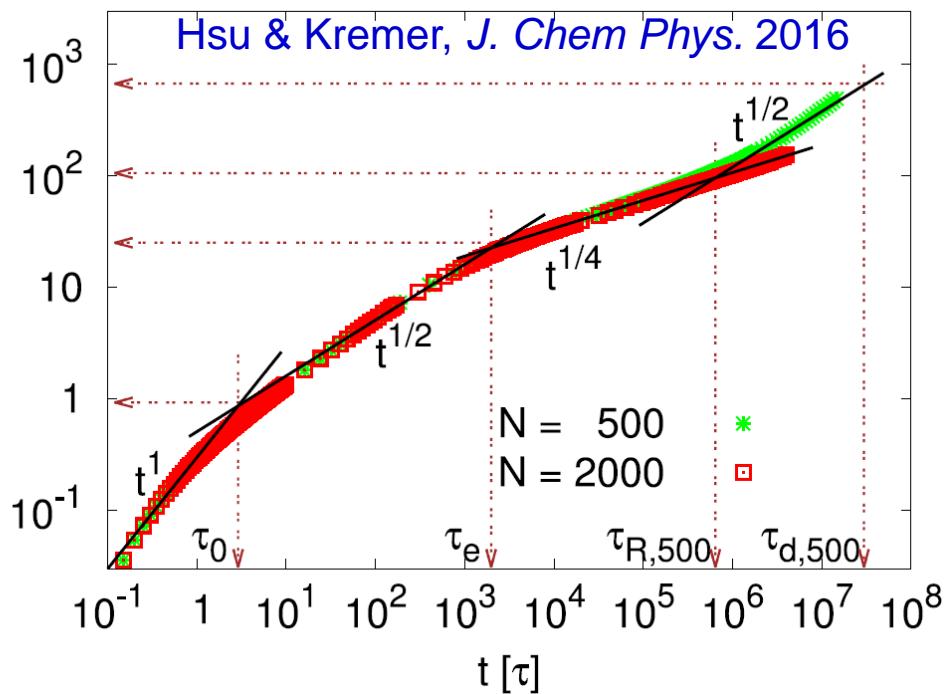
Example: mean square monomer displacement



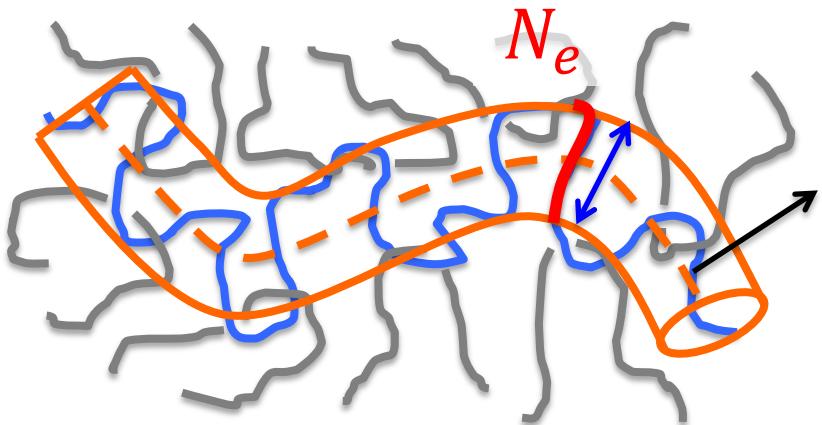
$$g_1(t) \sim \begin{cases} t^{1/2} & \text{for } t \leq \tau_e \\ t^{1/4} & \text{for } \tau_e \leq t \leq \tau_R \\ t^{1/2} & \text{for } \tau_R \leq t \leq \tau_d \\ t & \text{for } \tau_d \leq t \end{cases}$$



Rubinstein & Colby, *Polymer Physics* 2003



# TOPOLOGICAL ANALYSIS: PRIMITIVE PATH



## Primitive path (PP)

*Shortest path between endpoints of original chain into which its contour can be contracted without crossing any obstacle*

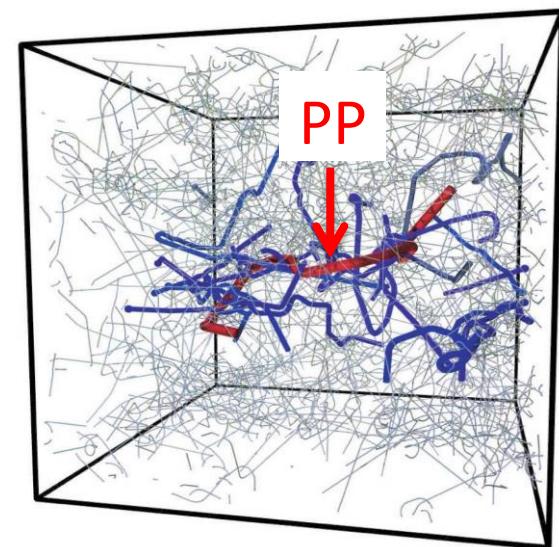
$N_e$  is defined as the number of monomers in a **Kuhn segment** of Primitive Path.

$$N_e = a_{pp} / b_{pp}$$

$$a_{pp} = \langle R^2 \rangle / L_{pp} \quad b_{pp} = L_{pp} / N$$

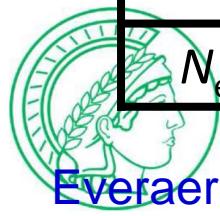
Kuhn length of PP      bond length of PP

bead-spring model,  $k_\theta=1.5$



- Fixing the chain ends, pull all chains till they are taut
- Inter-chain excluded-volume interactions are retained, while intrachain excluded-volume interactions are disabled

$N$	1000	2000	3000
$N_{e,PPA}$	$29 \pm 2$	$28 \pm 1$	$29 \pm 1$

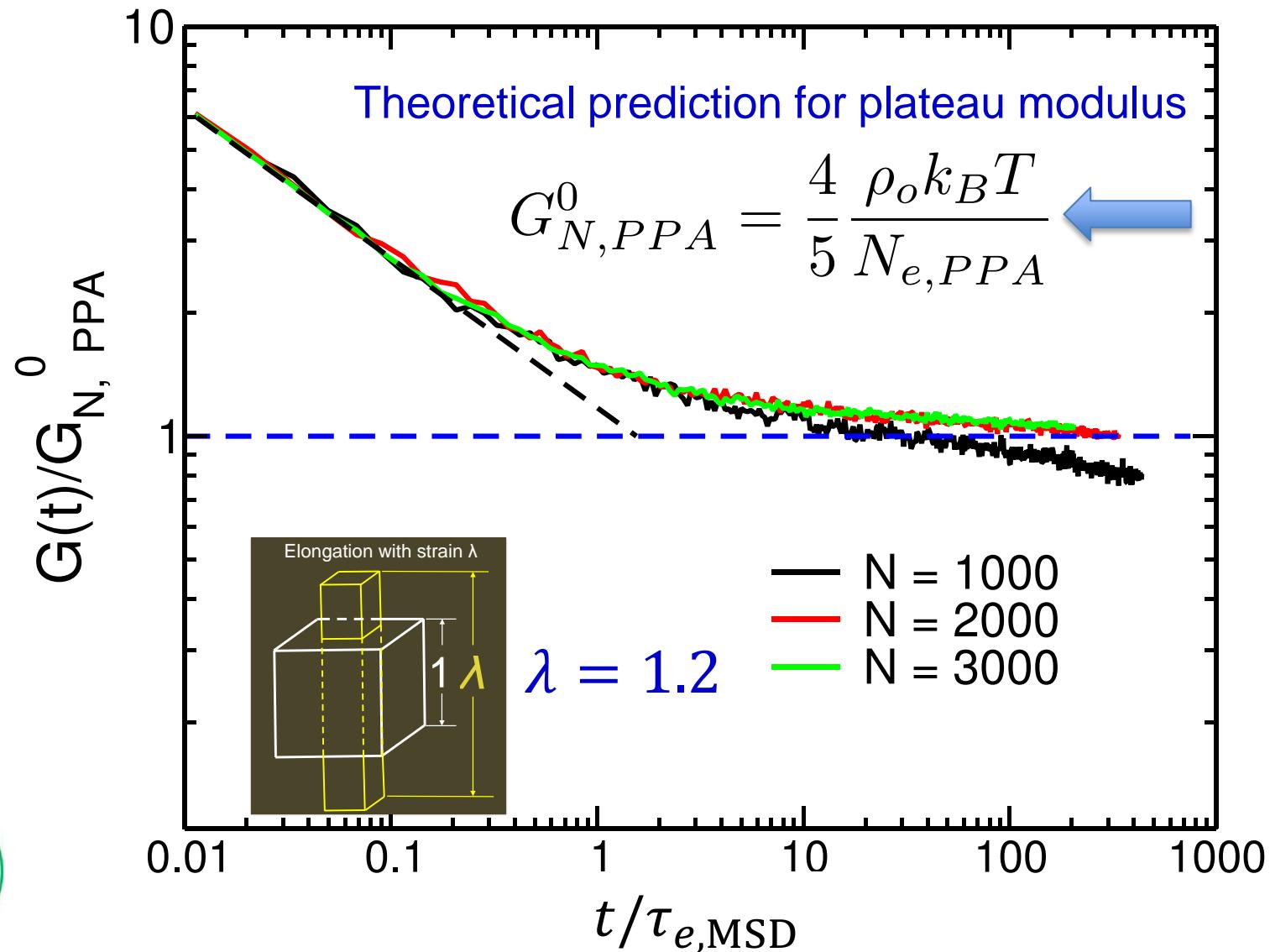


# PREDICTING THE PLATEAU MODULUS



## Rheological experiments

Example: stress relaxation modulus after step elongation



# SUMMARY



- A hierarchical scheme for equilibrating high molecular weight polymer melts was presented. Creating very large samples with chains  $\sim 100 N_e$  long is now feasible
- The scheme is applicable to generic and chemically specific microscopic models
- Hierarchical modeling was combined with universality concepts:
  - Long-wavelength structure of a single melt can be back-mapped onto “chemically” different homopolymer melts with the same  $\bar{N}$
  - Perspectives for materials genomic libraries: for different classes long-wavelength structure can be stored in a few configurations of a single material
  - Modelling blends
- Parameterization of blob models requires medium-sized “brute force” MD simulations
  - Can one benefit from other strategies, e.g. integral-equation-state theories?

## CPU time:



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NIC