ADAPTIVE RESOLUTION SIMULATION METHODS

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Motivation



The resolution of a simulation is chosen based on the process of interest



Large-scale properties, conformational transitions, phase ordering

Coarse-grained models





Dual resolution simulations: concurrent use of different resolutions in separate regions of the simulation domain

Example: QM/MM simulation methods A small region is treated at the quantum level, the rest with classical force fields



Dual resolutions of soft matter: atomistic and coarse-grained

Low-resolution region, where molecules are coarse-grained

High-resolution region, where the atomistic detail is kept

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Low-resolution region, where molecules are coarse-grained

High-resolution region, where the atomistic detail is kept

How are these two regions interfaced?

Interpolation of force-fields

 $\langle \bullet \rangle$



Interpolation of force-fields

AdResS - Adaptive Resolution Simulation scheme

 $\mathbf{F}_{\alpha\beta} = w(X_{\alpha})w(X_{\beta})\mathbf{F}_{\alpha\beta}^{expl} + [1 - w(X_{\alpha})w(X_{\beta})]\mathbf{F}_{\alpha\beta}^{cg}$



M. Praprotnik, L. Delle Site, and K. Kremer, J. Chem. Phys. 123, 2005

Control of the thermodynamics in the explicit region

Coarse-grained potentials usually don't match the atomistic system's virial pressure

 $\langle \bullet \rangle$

The difference can be balanced via an iteratively-refined thermodynamic force [1]

$$\mathbf{F}_{th}^{i+1}(x) = \mathbf{F}_{th}^{i}(x) - \frac{M}{\rho_0^2 \kappa_T} \nabla \rho^i(x)$$

[1] S. Fritsch, S. Poblete, C. Junghans, G. Ciccotti, L. Delle Site, and K. Kremer, Phys Rev Lett 17, vol 108, 2012 [Figures from therein]



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The explicit region behaves as an open system

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Validation and applications





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(a)





FIG. 1. Adaptive resolution simulation scheme for hydrophobic solutes, illustrated for the case of C_{2160} icosahedral fullerene.

FIG. 1: (a) The on-the-fly interchange between the atomic and coarse-grained levels of description. The middle hybrid molecule is a linear combination of fully atomistic tetrahedral molecule with an additional center of mass particle representing the coarse-grained molecule. (b) Snapshot of the hybrid atomistic/mesoscopic model at $\rho^* = 0.1$ and $T^* = 1$ (LJ units). The red molecules are the explicit atomistically resolved tetrahedral molecules, the blue molecules are the corresponding one particle coarse-grained molecules.

(b)

M. Praprotnik, L. Delle Site, K. Kremer, Phys. Rev. E 73, 2006

M. Praprotnik, L. Delle Site , K. Kremer, Annu. Rev. Phys. Chem. 59, 2008

B.P. Lambeth, Jr., C. Junghans, K. Kremer, C. Clementi, L. Delle Site, J. Chem. Phys. 133, 2010

Figure 6

(a) The on-the-fly interchange between the atomistic (*far-right molecule*) and coarse-grained (*far-left molecule*) levels of description. The middle hybrid molecule is a linear combination of a fully atomistic molecule with an additional center-of-mass particle representing the coarse-grained molecule. (b) Snapshot of the hybrid atomistic/mesoscopic model liquid with $\rho = 0.175$ and T = 1.0. The red molecules are the explicit atomistically resolved tetrahedral molecules, and the blue molecules are the corresponding one-particle coarse-grained molecules.

h



Figure 11

(*a*) On-the-fly interchange between the all-atom and coarse-grained water models. (*b*) A schematic representation of the hybrid liquid-water system.

Application of AdResS for "open-boundaries" simulations

When the correct particle fluctuations are important large simulation boxes are needed

Triglycine solvated in aqueous urea







A two-component solvent requires two thermodynamic force terms

D. Mukherji, N. F. A. van der Vegt, K. Kremer, and L. Delle Site, JCTC. 8, 375 (2012) D. Mukherji, N. F. A. van der Vegt, and K. Kremer, JCTC 8, 3536 (2012)

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Triglycine solvated in aqueous urea Example of density correction in a methanol-water mixture



D. Mukherji, N. F. A. van der Vegt, K. Kremer, and L. Delle Site, JCTC. 8, 375 (2012) D. Mukherji, N. F. A. van der Vegt, and K. Kremer, JCTC 8, 3536 (2012)

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A force-based mixing was chosen over an energy-based mixing $\mathbf{F}_{\alpha\beta} = w(X_{\alpha})w(X_{\beta})\mathbf{F}_{\alpha\beta}^{expl} + [1 - w(X_{\alpha})w(X_{\beta})]\mathbf{F}_{\alpha\beta}^{cg}$

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$$H = \mathcal{K} + V^{int} + \sum_{\alpha} \left\{ \lambda_{\alpha} V_{\alpha}^{AA} + (1 - \lambda_{\alpha}) V_{\alpha}^{CG} \right\}$$

$$V_{\alpha}^{AA} \equiv \frac{1}{2} \sum_{\substack{\beta, \beta \neq \alpha \\ \beta, \beta \neq \alpha}}^{N} \sum_{ij} V^{AA} (|\mathbf{r}_{\alpha i} - \mathbf{r}_{\beta j}|)$$
$$V_{\alpha}^{CG} \equiv \frac{1}{2} \sum_{\substack{\beta, \beta \neq \alpha \\ \beta, \beta \neq \alpha}}^{N} V^{CG} (|\mathbf{R}_{\alpha} - \mathbf{R}_{\beta}|)$$
$$\lambda_{\alpha} = \lambda (\mathbf{R}_{\alpha})$$

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$$\begin{split} V_{\alpha}^{AA} &\equiv \frac{1}{2} \sum_{\beta,\beta \neq \alpha}^{N} \sum_{ij} V^{AA} (|\mathbf{r}_{\alpha i} - \mathbf{r}_{\beta j}| \\ V_{\alpha}^{CG} &\equiv \frac{1}{2} \sum_{\beta,\beta \neq \alpha}^{N} V^{CG} (|\mathbf{R}_{\alpha} - \mathbf{R}_{\beta}|) \\ \lambda_{\alpha} &= \lambda (\mathbf{R}_{\alpha}) \end{split}$$

The total energies of the molecules are weighted by the switching function

$$H = \mathcal{K} + V^{int} + \sum_{\alpha} \left\{ \lambda_{\alpha} V_{\alpha}^{AA} + (1 - \lambda_{\alpha}) V_{\alpha}^{CG} \right\}$$

$$\mathbf{F}_{\alpha} = \mathbf{F}_{\alpha}^{int} + \sum_{\beta,\beta\neq\alpha} \left\{ \frac{\lambda_{\alpha} + \lambda_{\beta}}{2} \mathbf{F}_{\alpha|\beta}^{AA} + \left(1 - \frac{\lambda_{\alpha} + \lambda_{\beta}}{2}\right) \mathbf{F}_{\alpha|\beta}^{CG} \right\} - \left[V_{\alpha}^{AA} - V_{\alpha}^{CG} \right] \nabla_{\alpha} \lambda_{\alpha}$$

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 $\left\langle \mathbf{F}_{\alpha}^{\nabla} \right\rangle = -\left\langle \left[V_{\alpha}^{AA} - V_{\alpha}^{CG} \right] \right\rangle_{\mathbf{R}_{\alpha}} \nabla \lambda(\mathbf{R}_{\alpha})$ $\mathbf{R}_{lpha}, \lambda_{lpha}$ **CG** region **AA** region Hybrid region

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The force in the hybrid region is proportional to the difference of Helmholtz free energy between AA and CG models

Modify the Hamiltonian introducing a compensation term

N $H_{\Delta} = H - \sum \Delta H(\lambda(\mathbf{R}_{\alpha}))$ $\alpha = 1$

Modify the Hamiltonian introducing a compensation term

$$H_{\Delta} = H - \sum_{\alpha=1}^{N} \Delta H(\lambda(\mathbf{R}_{\alpha}))$$

$$\Delta H(\lambda) \equiv \frac{\Delta F(\lambda)}{N}$$

Helmholtz free energy cancels the drift force in the hybrid region

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Helmholtz free energy cancels the drift force in the hybrid region To remove the pressure imbalance between AA and CG we employ Gibbs free energy difference:

$$\Delta H(\lambda) \equiv \Delta \mu(\lambda) = \frac{\Delta F(\lambda)}{N} + \frac{\Delta p(\lambda)}{\rho^{\star}}$$

The big picture



MicroCanonical simulations

Energy-conserving simulations of a simple toy model system



Tetrahedral purely-repulsive molecules
The CG potential is NOT parametrized

on the AA system



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Energy-conserving simulations of a simple toy model system



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Tetrahedral purely-repulsive molecules
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NVT simulations

 $(\mathbf{\bullet})$

Thermostated simulation of a water system



The CG potential is NOT parametrized on the AA system

Hamiltonian of a binary mixture

$$H^{MIX} = \mathcal{K} + V^{int} + \sum_{a \in A} \left[\lambda_a V_a^{AT} + (1 - \lambda_a) V_a^{CG} \right] + \sum_{b \in B} \left[\lambda_b V_b^{AT} + (1 - \lambda_b) V_b^{CG} \right]$$

How can we control the thermodynamics of both species?

 $\langle \bullet \rangle$

$H_{\Delta}^{MIX} = H^{MIX} - \sum_{a \in A} \Delta H_A(\lambda_a) - \sum_{b \in B} \Delta H_B(\lambda_b)$

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$H_{\Delta}^{MIX} = H^{MIX} - \sum_{a \in A} \Delta H_A(\lambda_a) - \sum_{b \in B} \Delta H_B(\lambda_b)$ $\Delta H_k(\lambda) = \frac{\Delta F_k(\lambda)}{N_k} + \frac{\Delta p_k(\lambda)}{\rho_k^*}$

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All compensation terms are computed with a single Kirkwood Thermodynamic Integration The Free Energy Compensation method as a replacement for coarse-graining



The hybrid region can interface **arbitrarily different models** while preserving the equilibrium properties of the high-resolution region

A problem-specific CG interaction can be chosen at will

Accurate coarse-graining of the high-resolution system is thus not necessary

Binary mixture composed by two DIFFERENT species in EQUAL proportions



The SAME coarse-grained model is used for both





Markov The reference density is preserved



The reference density is preserved

The pairwise structure is preserved

RP, S. Fritsch, P. Español, R. Delgado-Buscalioni, K. Kremer, R. Everaers and D. Donadio, Phys. Rev. Lett. 110, 108301 (2013)

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Binary mixture composed by two EQUAL species in DIFFERENT proportions





Binary mixture composed by two EQUAL species in DIFFERENT proportions



Binary mixture in contact with an attractive wall

Different species in equal proportions
All atoms interact with the wall through a LJ potential





Binary mixture in contact witl

Different species in equal proportions
All atoms interact with the wall through a LJ potential





Take-home message

AdResS / H-AdResS: force-based or energy-based dual resolution simulation methods

 \diamond

- The force-based approach preserves Newton³ exactly, but it's not conservative (a local thermostat is needed)
- The energy-based approach is Hamiltonian, but in the hybrid region Newton³ is satisfied only on average
- Pros of having a Hamiltonian: NVE and MC possible, efficient Free Energy Compensation calculation, arbitrary CG model
- Applications in accretion processes (crystal growth, self-assembly), free energy calculations, classical/QM coupling (Path Integrals)

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Both AdResS and H-AdResS are implemented in Espresso++!!!

Acknowledgments

* Davide Donadio

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* Sebastian Fritsch

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* Rafael Delgado-Buscalioni

* Pep Español

* Ralf Everaers

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THANKYOU!