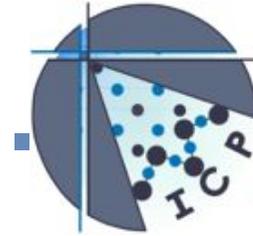




University of Stuttgart
Germany



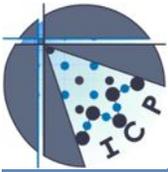
INSTITUTE FOR
COMPUTATIONAL
PHYSICS

Two Simple Microscopic Models for Ferroelectrics: A Simulation Approach

R. Weeber¹, S.S. Kantorovich^{1,2}, C. Holm¹

1) Institut für Computerphysik, Universität Stuttgart, Germany

2) Sapienza Univ. of Rome, Piazzale A. Moro 2, 00185, Rome, Italy



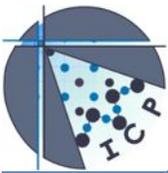
Overview: Talk has 2 Parts

R. Weeber, S. Kantorovich, C.H.

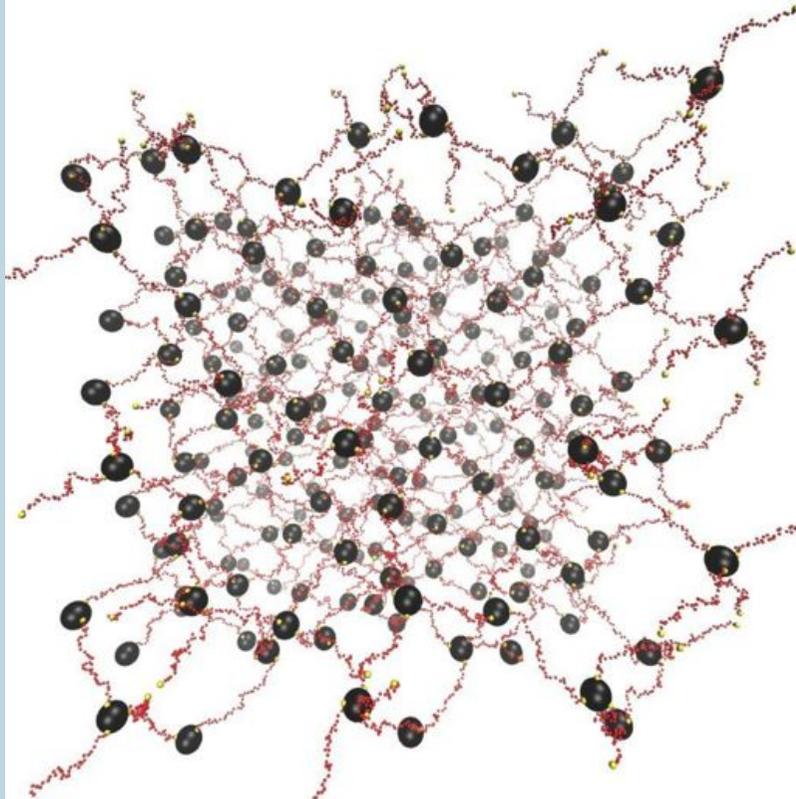
- Magnetic Gels

M. Klingikt, R. Weeber, S. Kantorovich, J.Cerda, C.H.

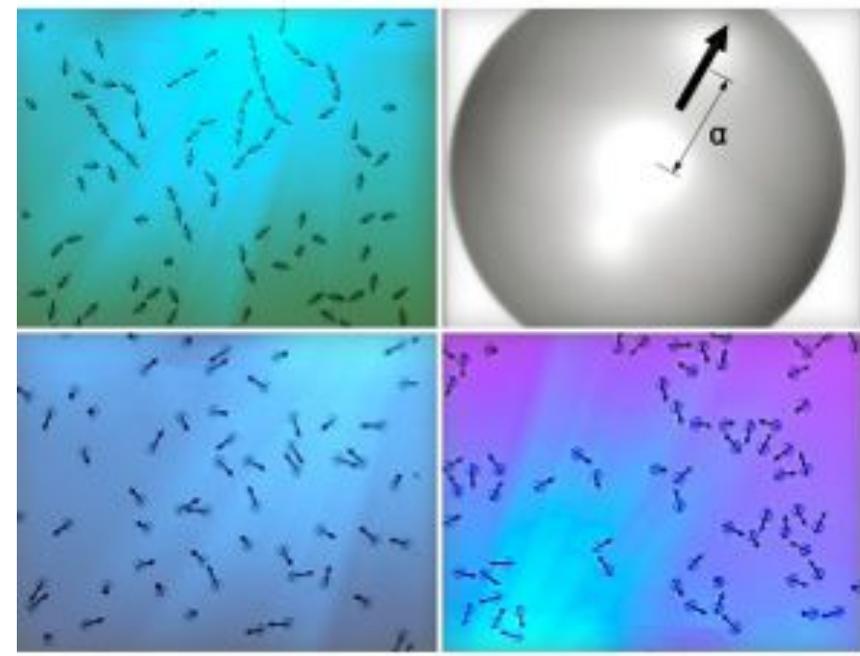
- Shifted Dipolar Particles



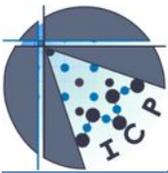
How to Tune Soft Magnetic Matter?



We can make the carrier fluid more complex
=> Magnetic gels

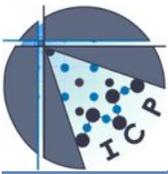


We can make the magnetic nanoparticles more complex
=> Shifted Dipolar colloids



Outline 1: Magnetic Gels

- What are ferrogels
- How can they deform in a magnetic field
- Model building (trying to follow reality):
- Some simulational details
- Model 1: deformation due to chaining
- Model 2: deformation due to torque transmission
- Summary

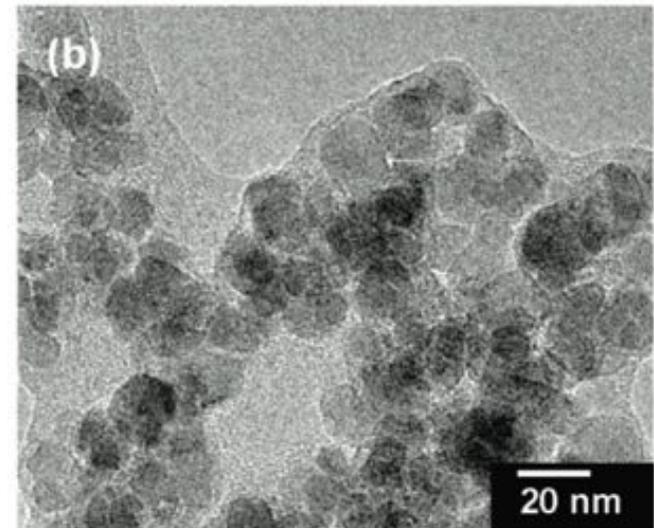
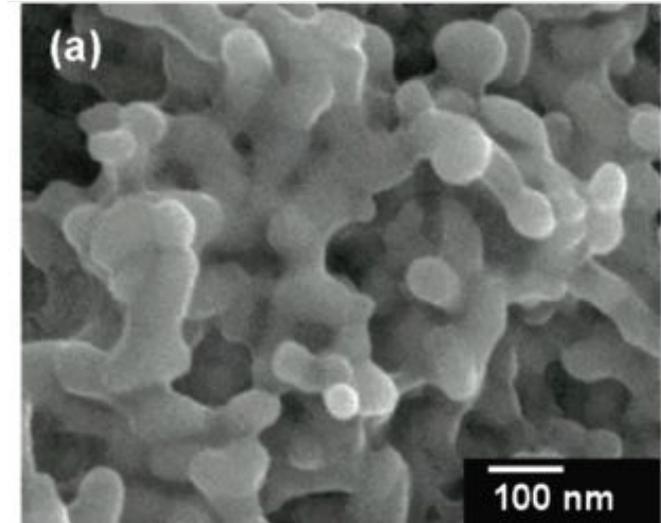


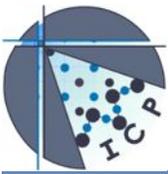
What are magnetic gels

- Magnetic nanoparticles embedded in a hydrogel
- Combination of elastic and magnetic properties

Applications:

- Drug delivery systems
- Actuators
- Artificial muscles



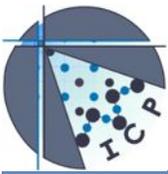


Hydrogels

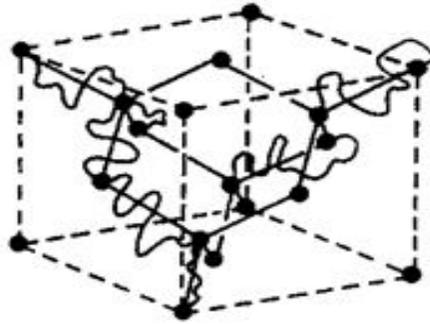
- A polymer network immersed in water
- Can react to chemical and physical environment
- Used in contact lenses, diapers, drug delivery systems

Water cleanage,
Templating via
microgels

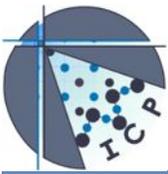




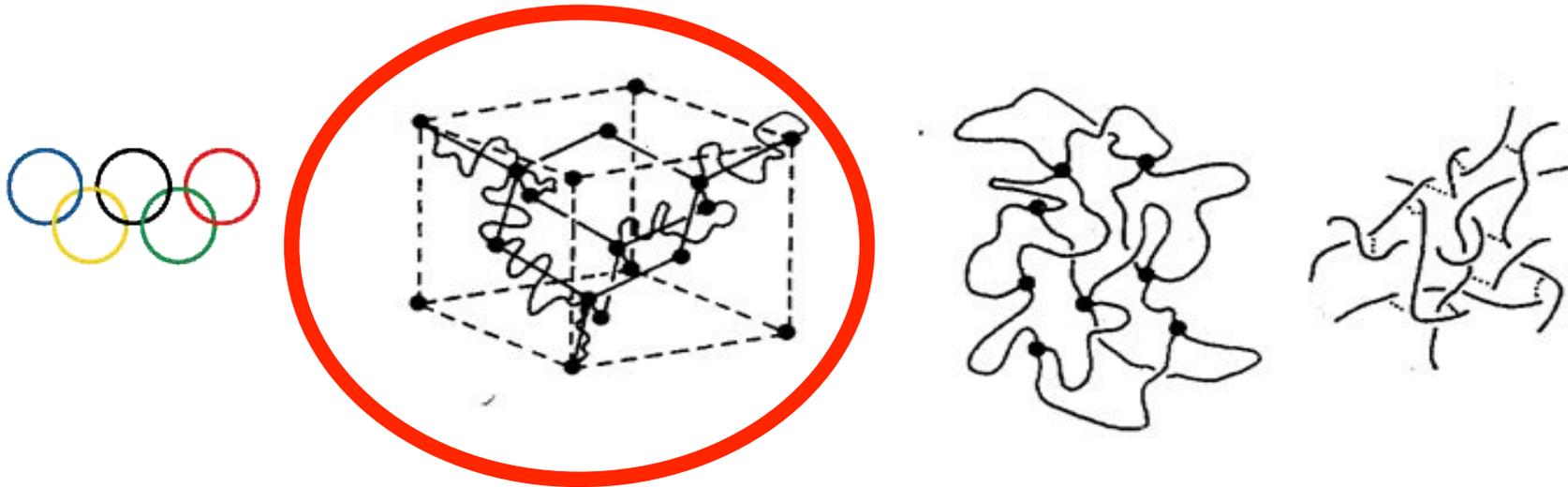
Model Networks



- Olympic gels
- Lattice Networks
- Endlinked melts
- Crosslinked melts

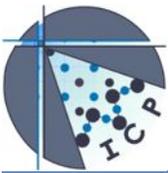


Model Networks



- Olympic gels
- Lattice Networks
- Endlinked melts
- Crosslinked melts

Control over network
architecture



Ferrogel Model Network

Model 1:

An f^{th} fraction of bead carries a magnetic moment

Model 2:

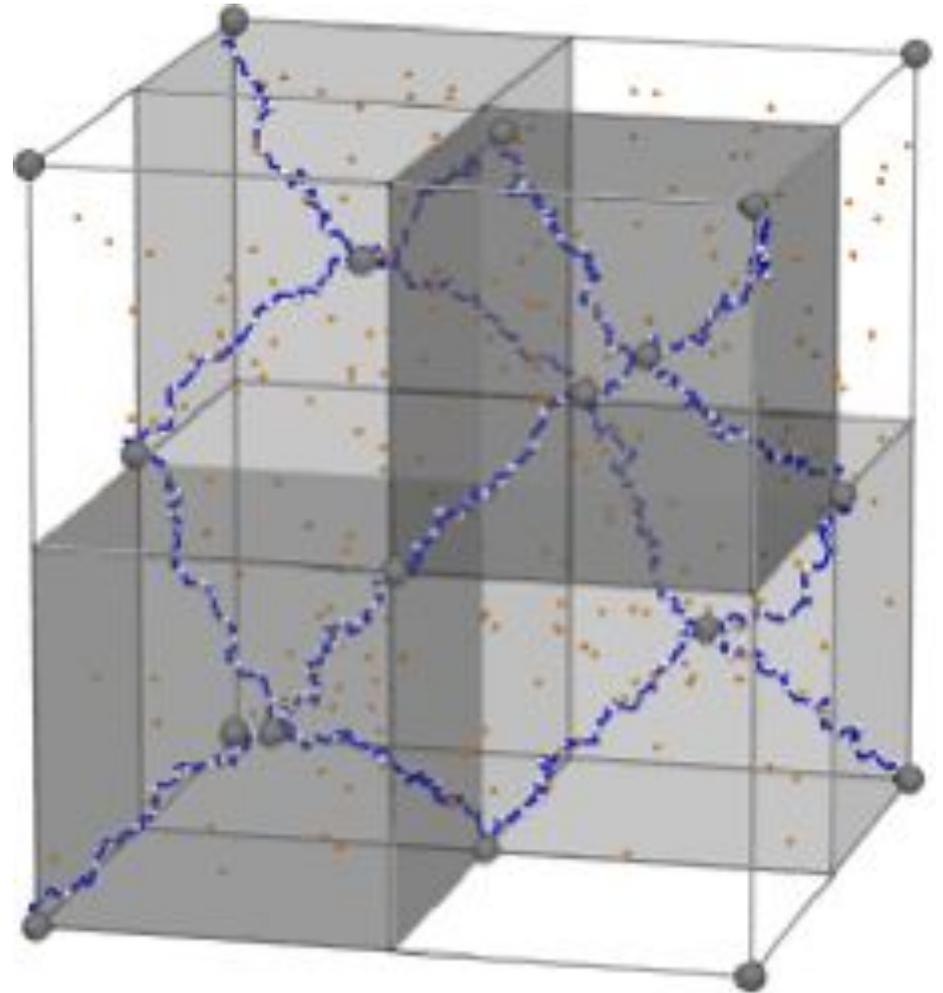
Only the network nodes carry a magnetic moment

Parameters:

- dipolar interaction strength
- Chain lengths
- Number of magnetic particles

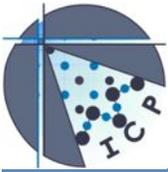
Observables:

- chain's end-to-end distance $\langle R_E^2 \rangle$
- dipole alignment
- magnetization in a field
- elastic constants



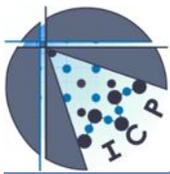
diamond-like topology

Coarse grained representation of a gel

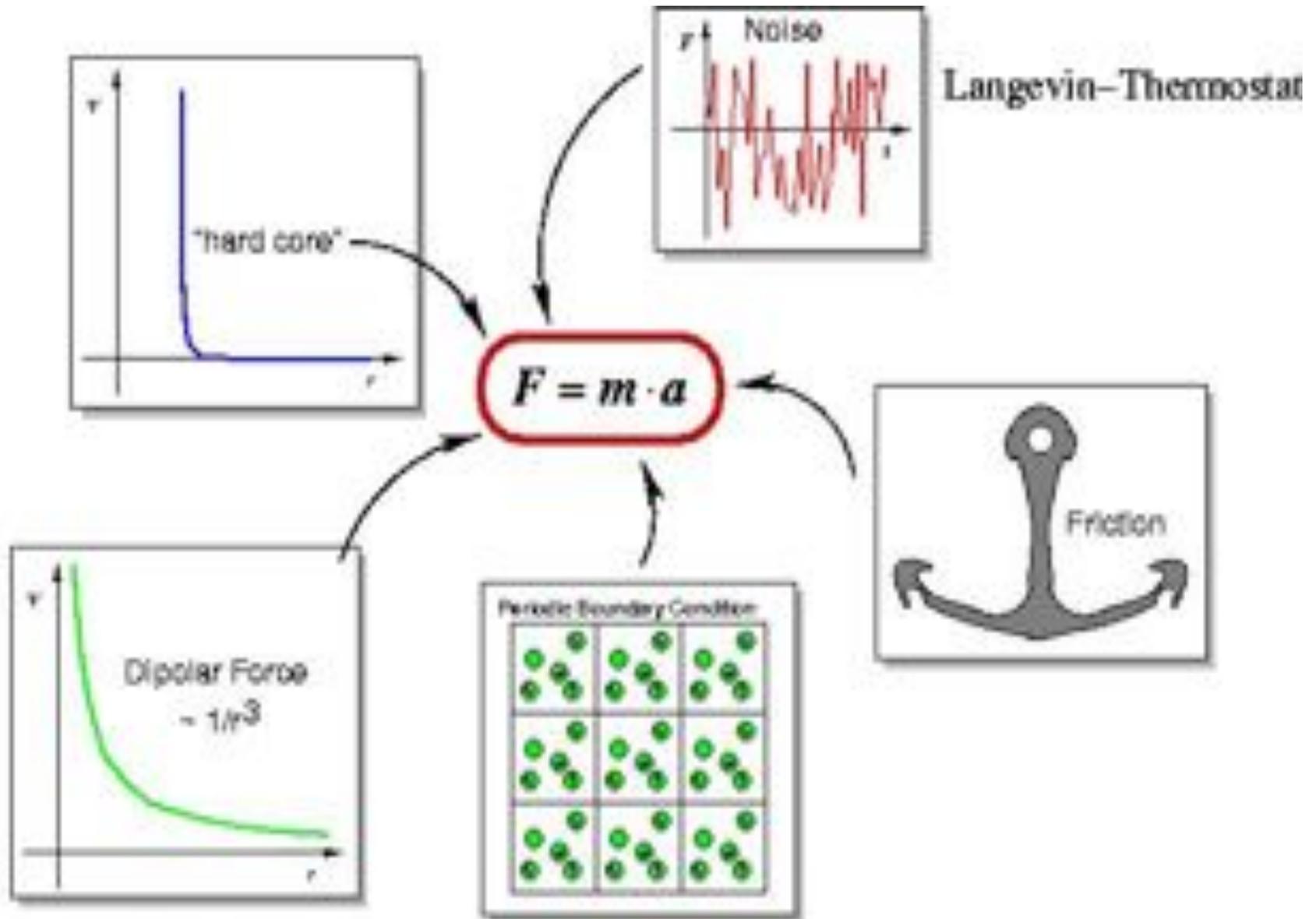


How can Ferrogels deform?

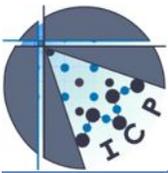
- In a field gradient:
magnetic particles move and deform the matrix
- In a homogeneous field:
 - 1) **(Model 1)** particles align to form clusters (chains)
 - 2) **(Model 2)** The rotation of the dipolar particle (Brownian relaxation) transmits torques onto the matrix



Principle of Molecular Dynamics



Dipolar P3M plus DLC



Langevin Dynamics Equ. of Motion

$$\mathcal{M}_i \dot{\mathbf{v}}_i = \mathbf{F}_i - \Gamma_T \mathbf{v}_i + \boldsymbol{\xi}_i^T,$$

$$\mathbf{I}_i \cdot \dot{\boldsymbol{\omega}}_i = \boldsymbol{\tau}_i - \Gamma_R \boldsymbol{\omega}_i + \boldsymbol{\xi}_i^R,$$

Random forces with zero first moment

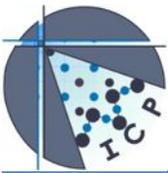
$$\langle \xi_{i\alpha}^T(t) \rangle = 0,$$

Dissipation-Fluctuation theorem

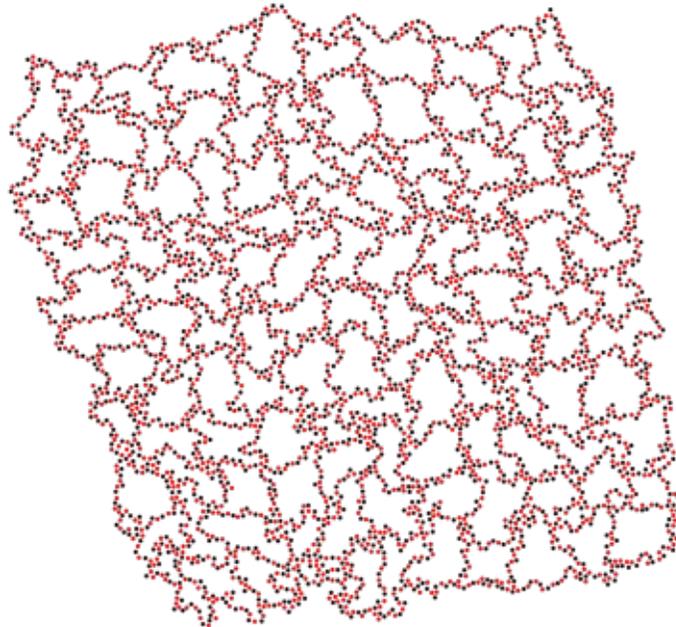
$$\langle \xi_{i\alpha}^R(t) \rangle = 0,$$

$$\langle \boldsymbol{\xi}_{i\alpha}^T(t) \cdot \boldsymbol{\xi}_{j\beta}^T(t') \rangle = 6kT\Gamma_T \delta_{ij} \delta_{\alpha\beta} \delta(t-t'),$$

$$\langle \boldsymbol{\xi}_{i\alpha}^R(t) \cdot \boldsymbol{\xi}_{j\beta}^R(t') \rangle = 6kT\Gamma_R \delta_{ij} \delta_{\alpha\beta} \delta(t-t')$$



Model 1 (2D)



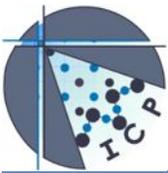
- magnetic particles
- non-magnetic particles

Diamond lattice, 15 particles per chain, $f=1/2$

Harmonic bonds between beads

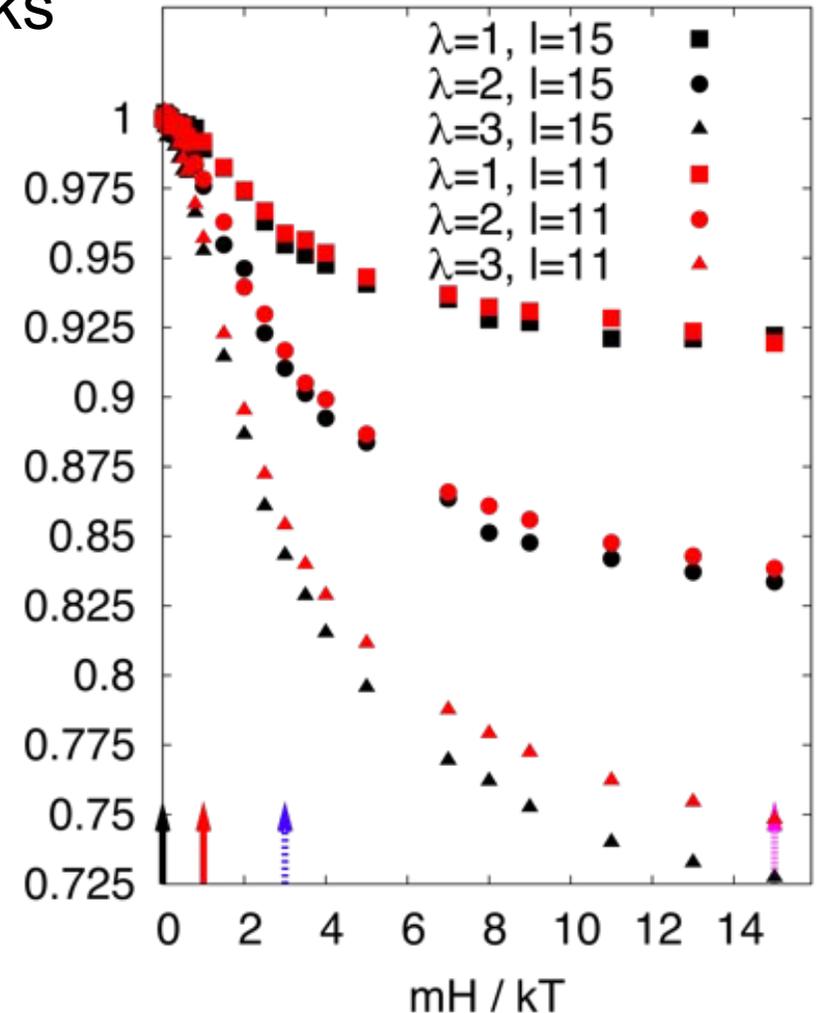
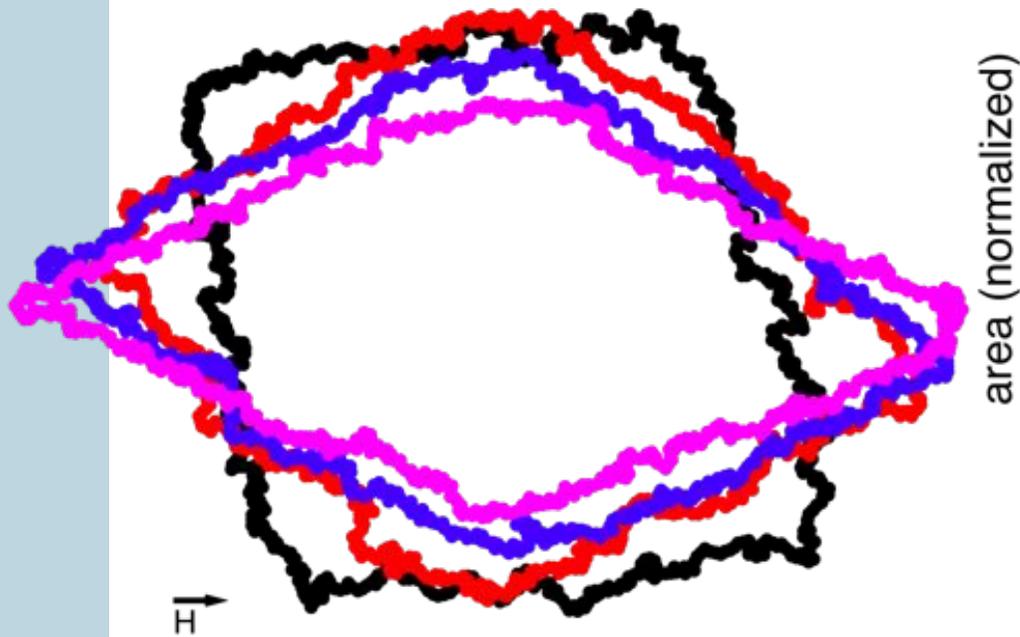
Simulated with MD, using direct sum for dipolar interaction

Open boundary, area not fixed



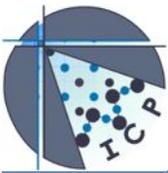
Model 1 in Magnetic Field

In a magnetic field the gel shrinks

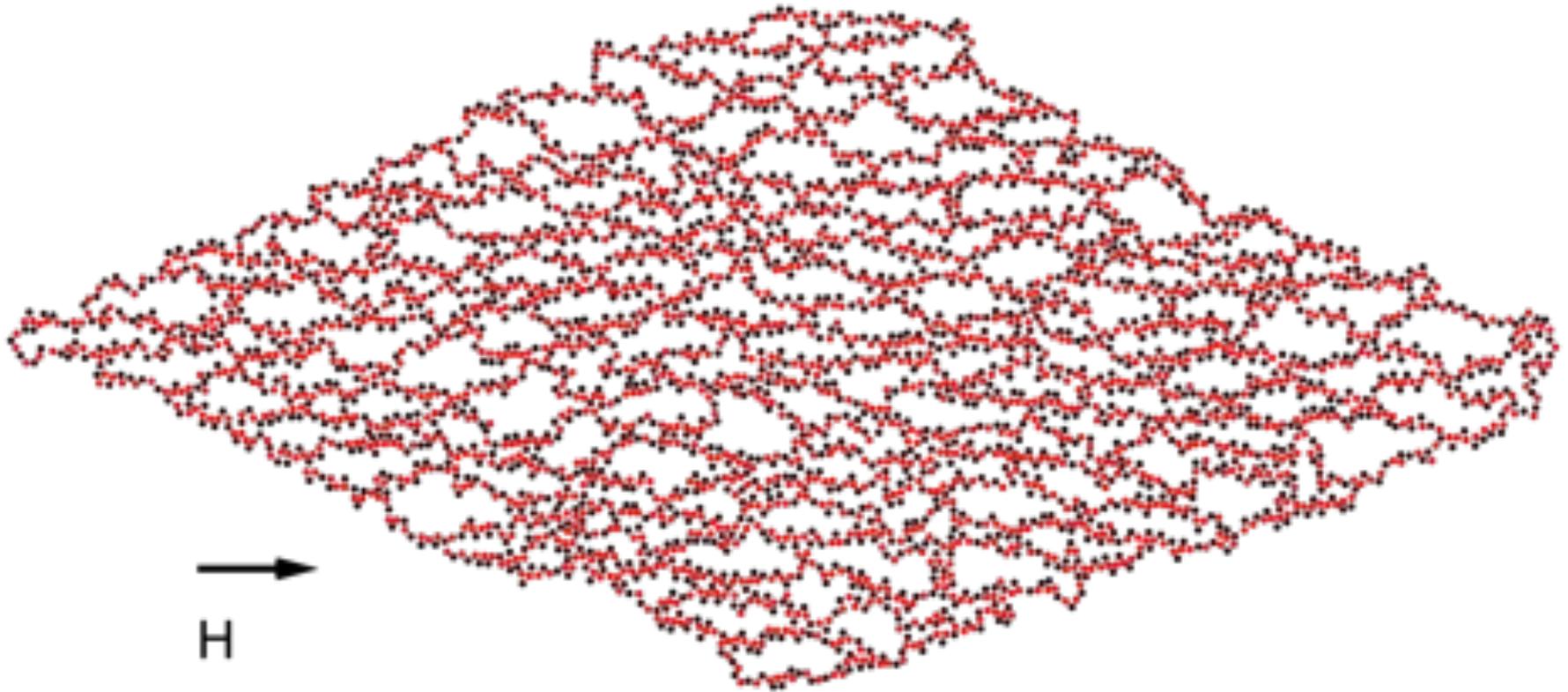


- Elongation parallel to \mathbf{H}
- Shrinking perpendicular to \mathbf{H}

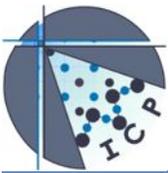
The longer the chain, the more the gel shrinks



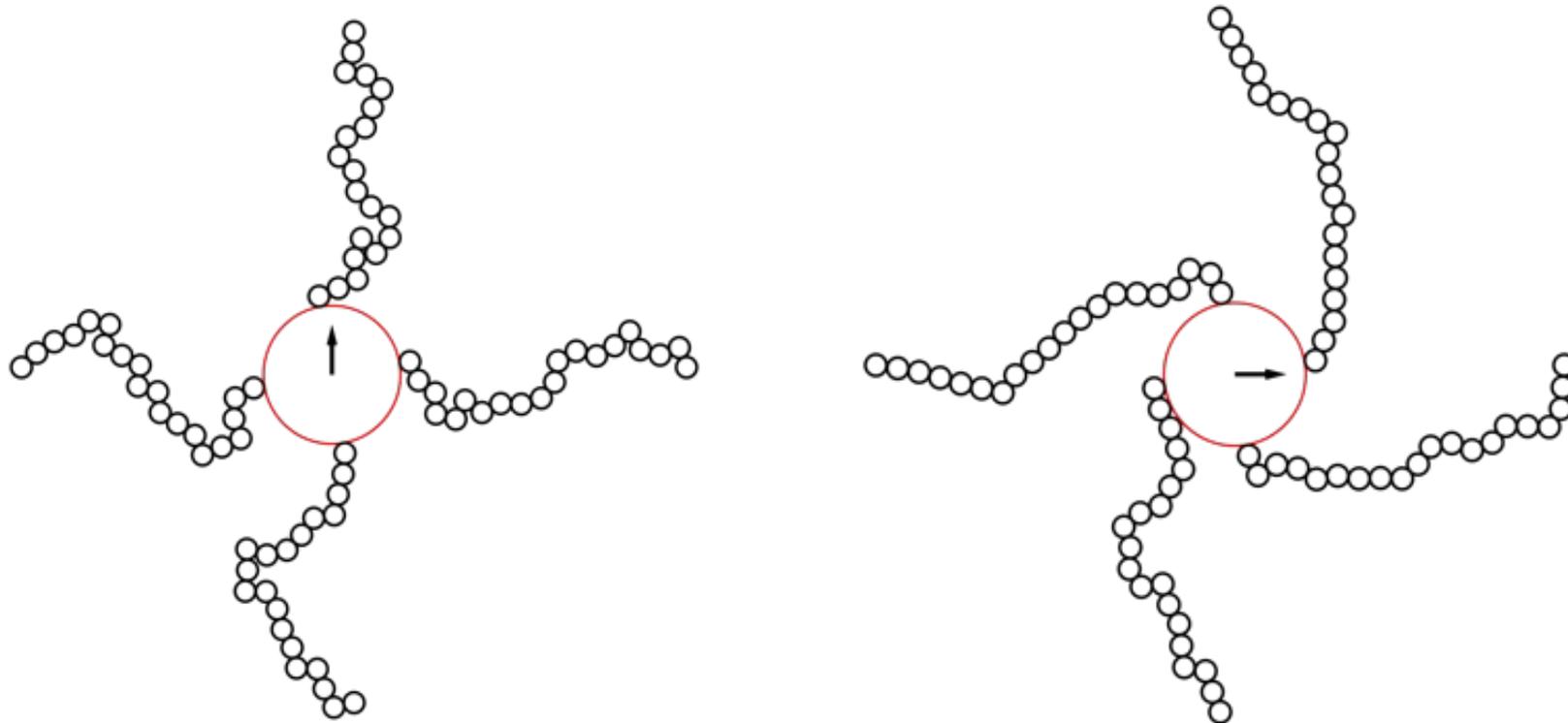
Reason for Shrinkage



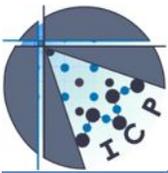
- Non-magnetic particles are pushed out of the chain
- Chains bend to align along the magnetic field lines



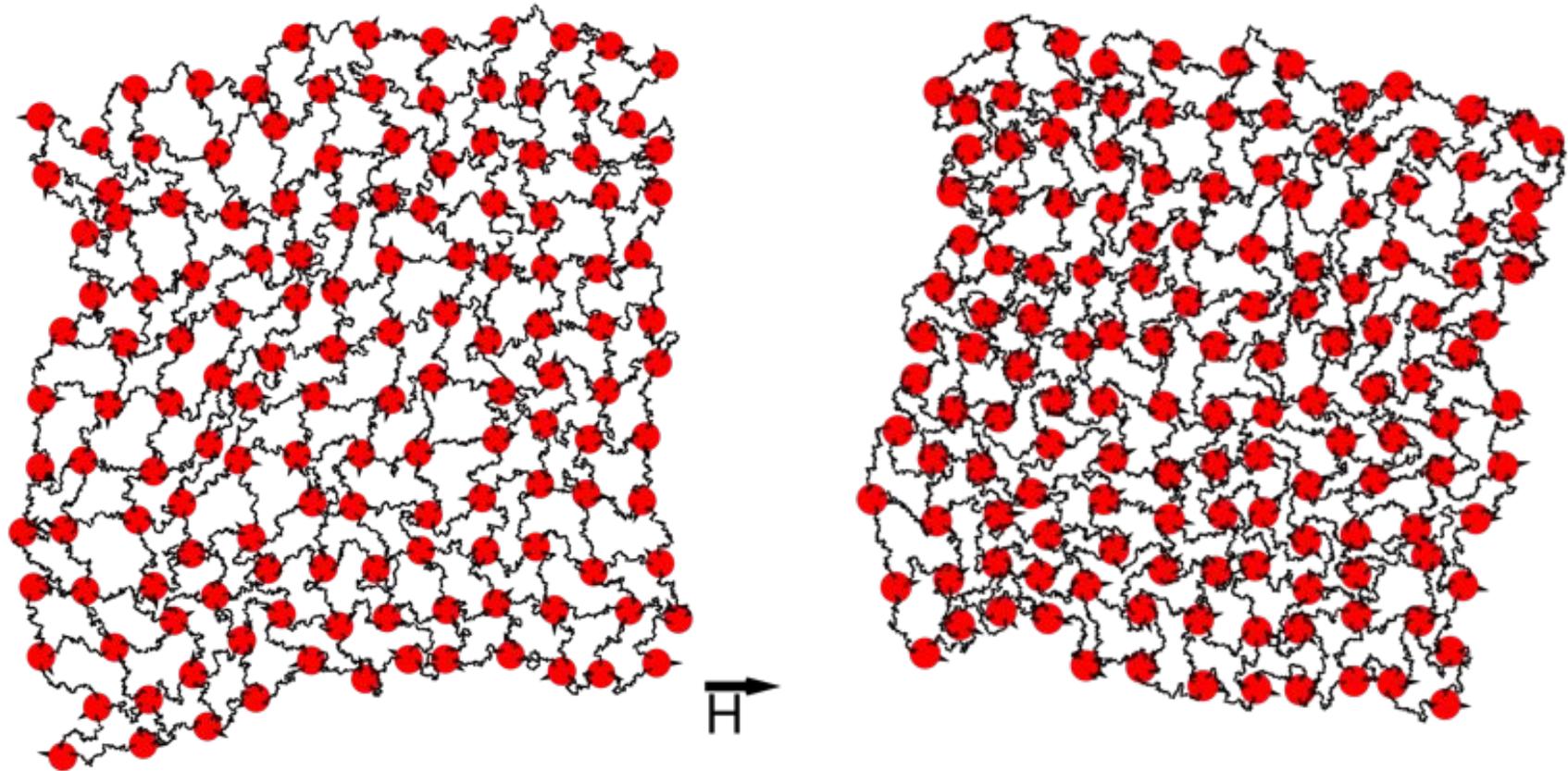
Model 2: Magnetic Crosslinkers



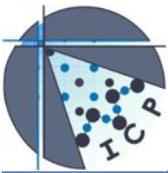
- Polymer network cross-linked with magnetic particles
- Polymers are attached to specific binding sites on the magnetic nanoparticle
- Only the node particle reacts to the field, no internode DD
- inspired by work of A. Schmidt (Köln)



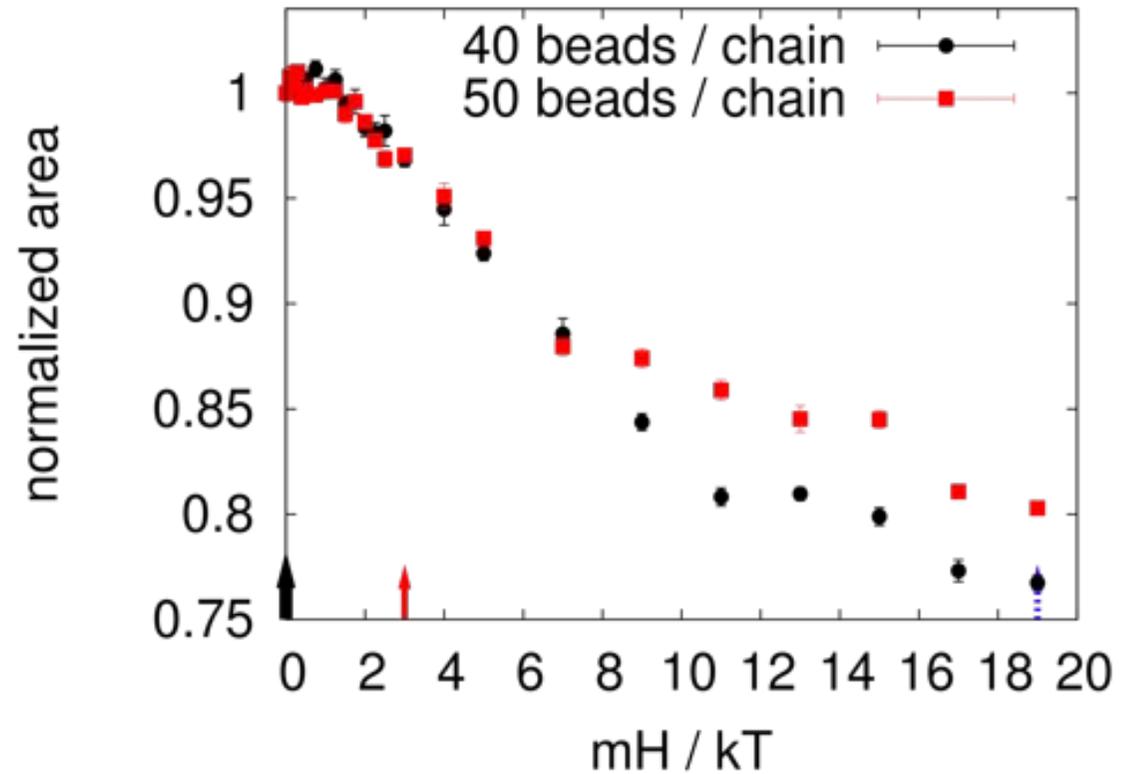
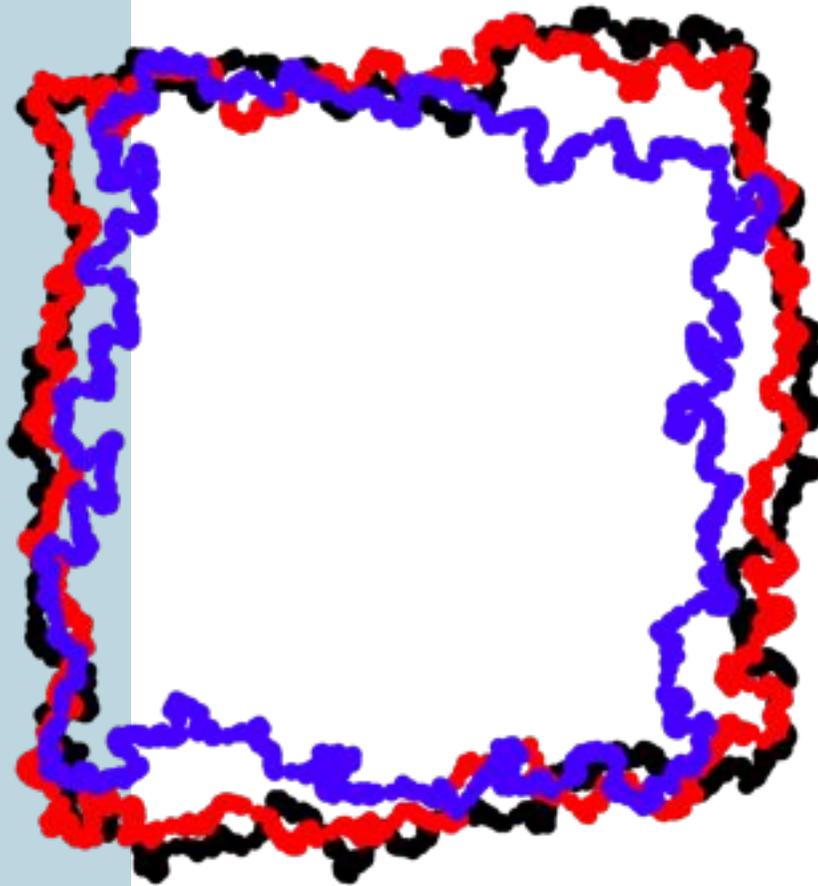
Model 2 in 2D



In a magnetic field the chains roll up
around the aligning magnetic particles
=> The gel shrinks

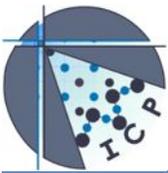


Shrinking Mechanism

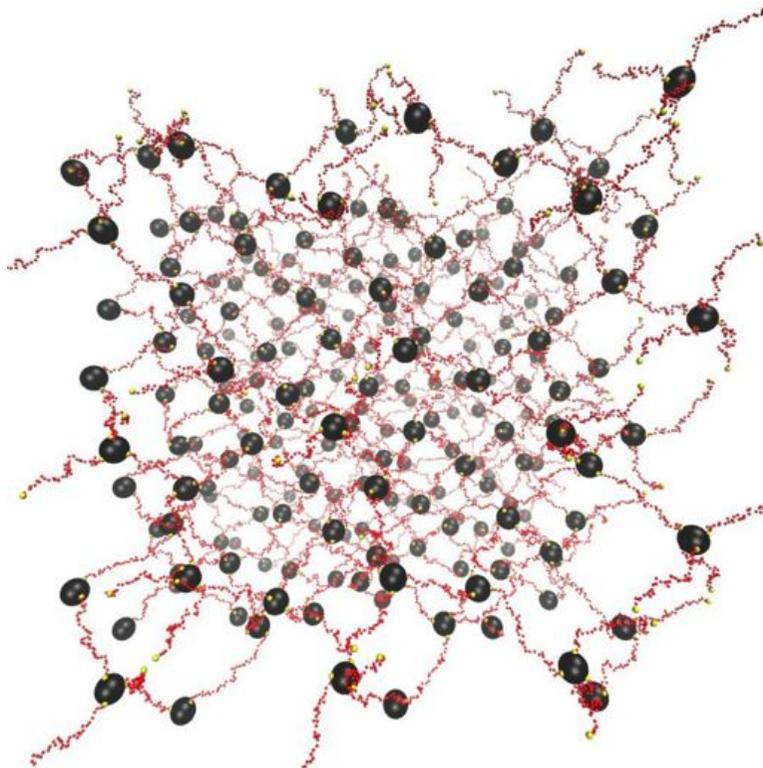


The shorter the chain, the more the gel shrinks

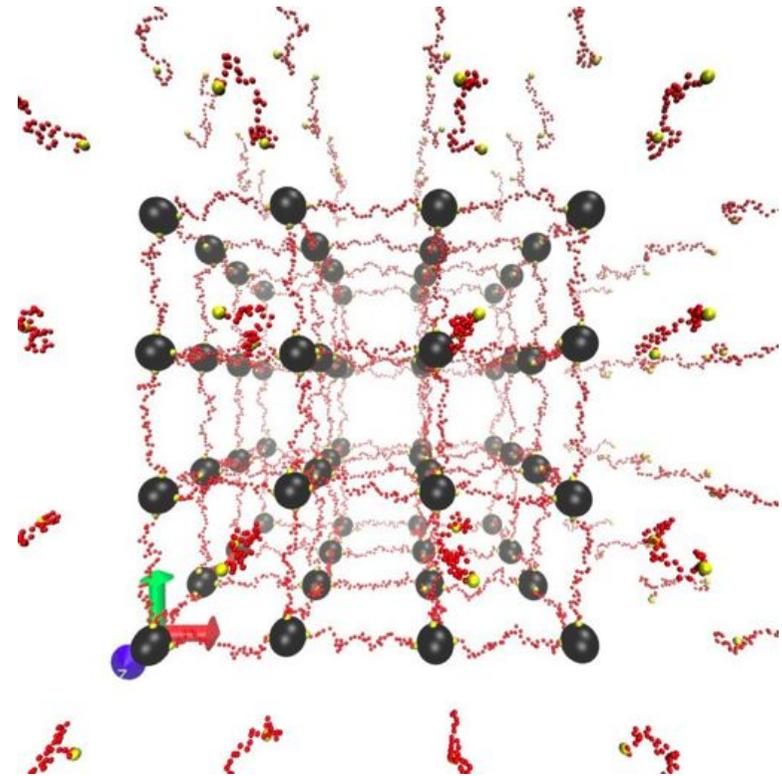
The stress on all chains attached to a magnetic particle is the same
=> The gel shrinks isotropically



Model 2 in 3D

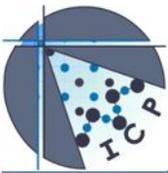


Diamond $N_c=4$

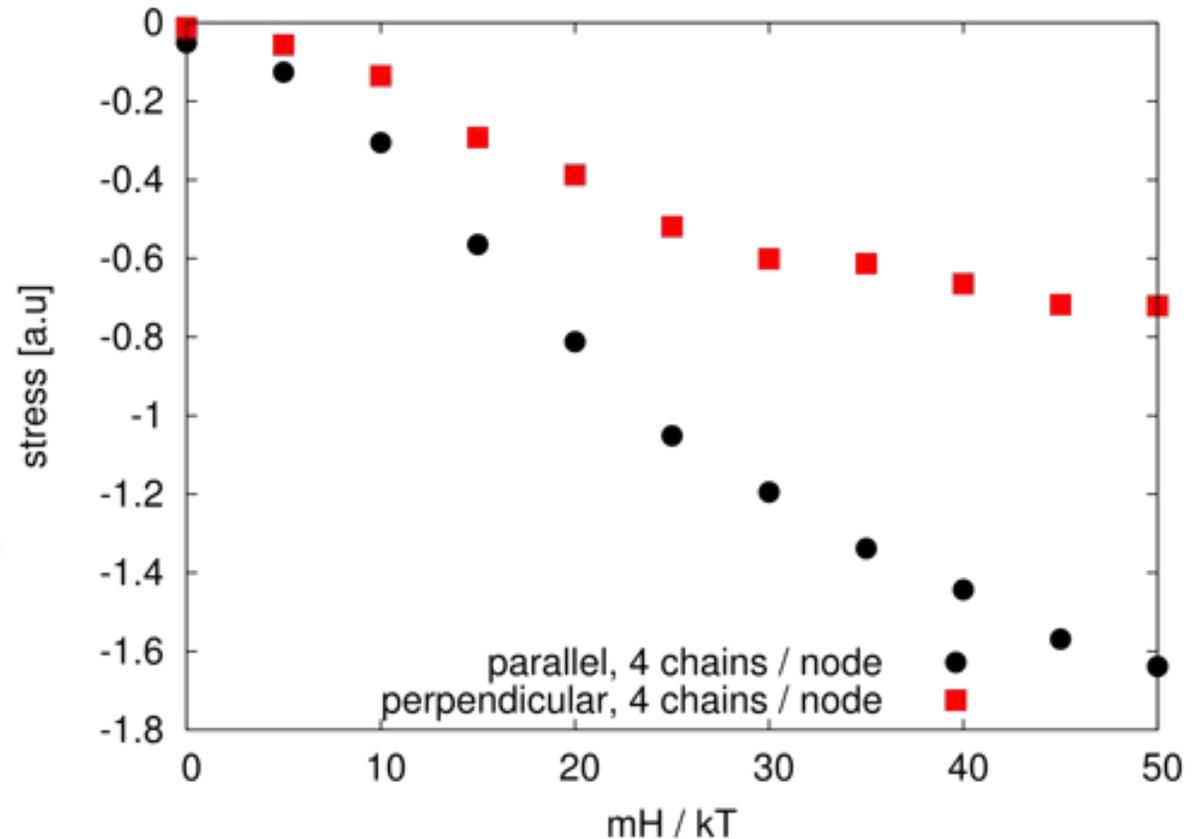
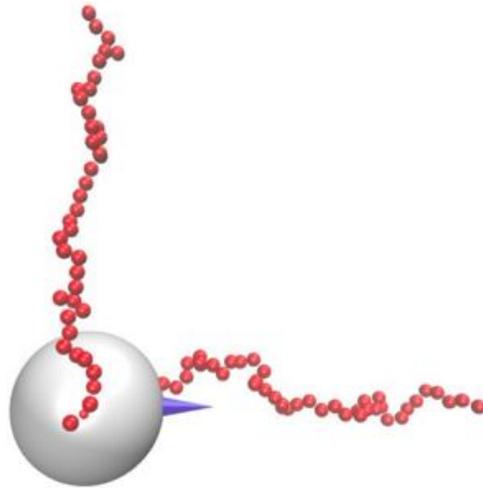


Simple cubic $N_c=6$

- Chains attached to surface of magnetic nanoparticle
- Simulation initially in NVT ensemble
- Volume iteratively changed to reach $P=0$ equilibrium state

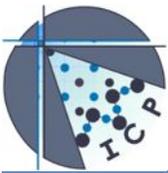


Influence of Magnetic Field

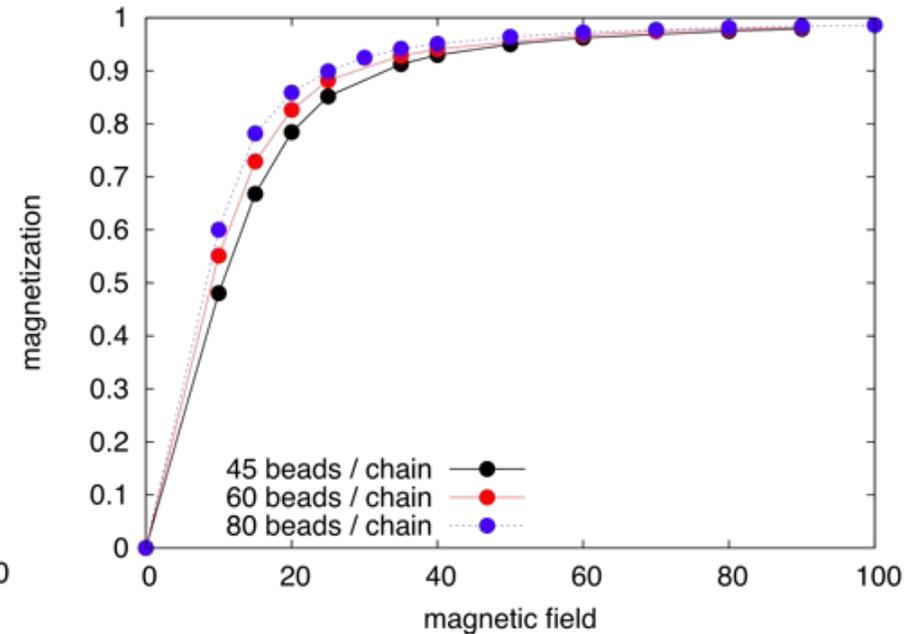
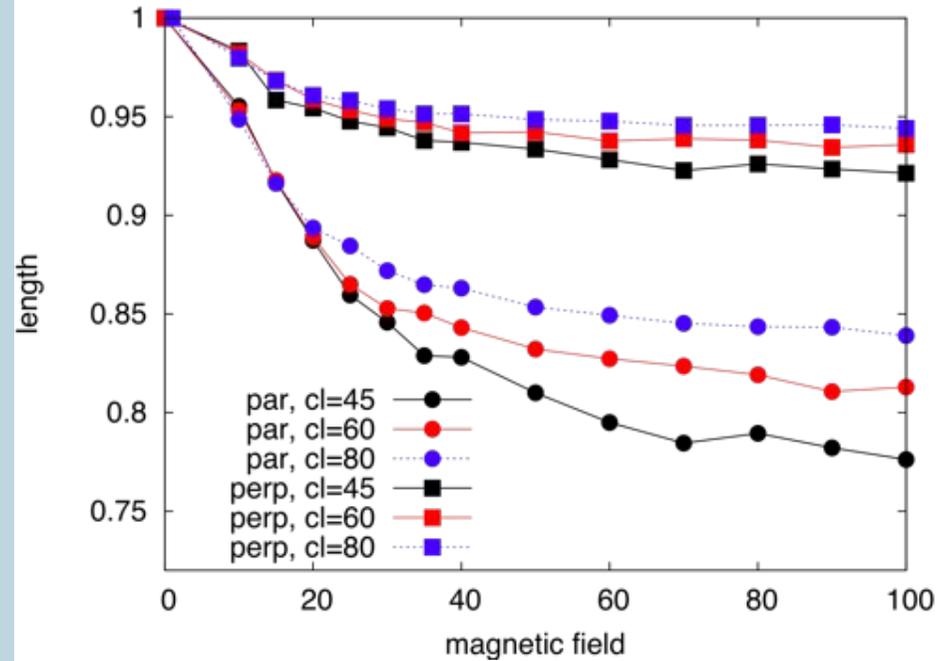


- Rotation around the field axis is possible
- Rotation around the other axis is hindered by the field

- Volume kept constant
- Higher stress in field direction, more contraction along this direction



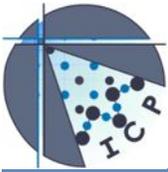
Shape Change and Magnetization



The gel shrinks stronger in field direction

A very strong field is required to magnetize the sample

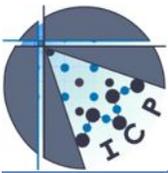
Again shorter chains show stronger contraction



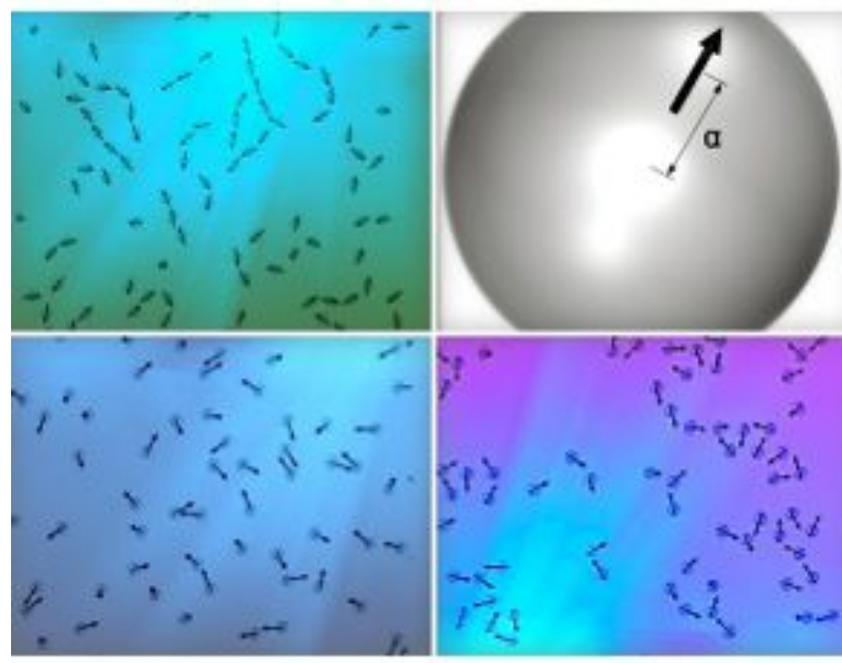
Summary Magnetic Gels

- Gels can contract in homogeneous fields due to 2 mechanisms
 - Chaining of dipolar particles in close distance
 - Transmitting the induced torque due to induced field alignments of the magnetic nodal particles that act as crosslinkers for the polymer strands
 - Differences in 2 and 3 dimensions (more d.o.f)

R Weeber S. Kantorovich and C. Holm, *Soft Matter* in press (2012)

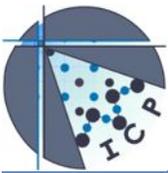


Part 2: Shifted Dipolar Particles

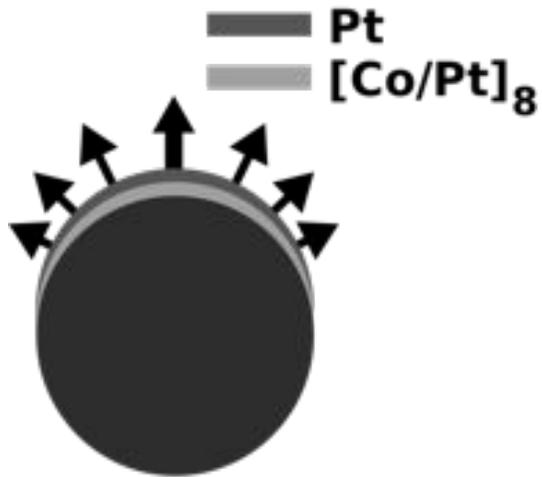


Use of Novel MNP for increasing Complexity

First we discuss only q2D geometries!

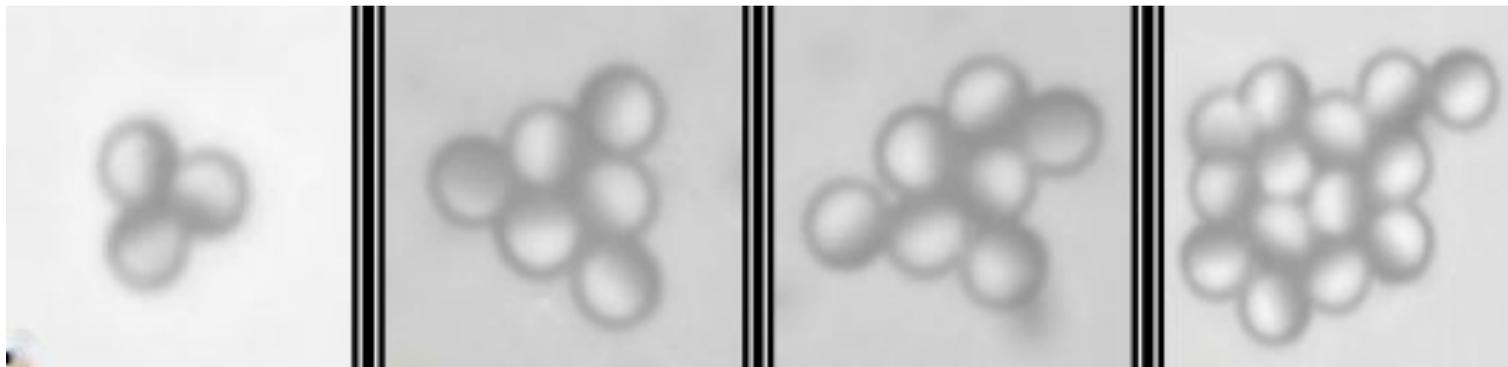
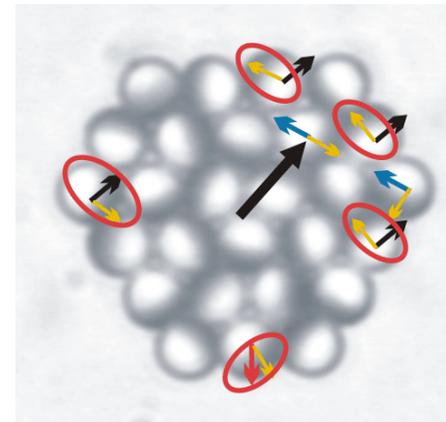
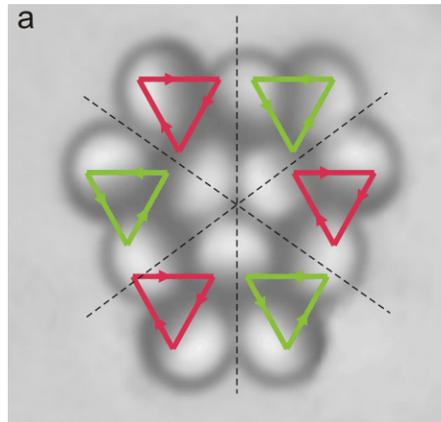
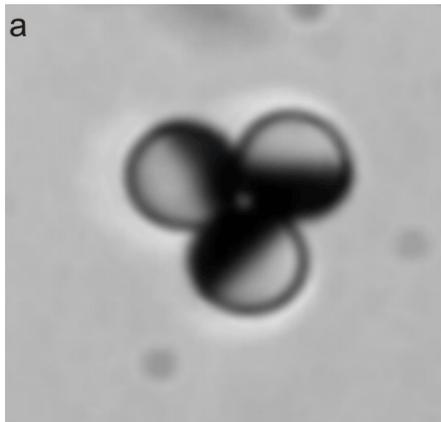


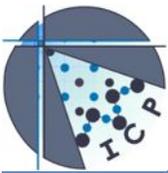
Inspiration from Experiments



L. Barabaran et al., *PRE* 77, 031407 (2008)

Barabaran et al. observe very stable „magic clusters“ with 3, 12, (27) particles

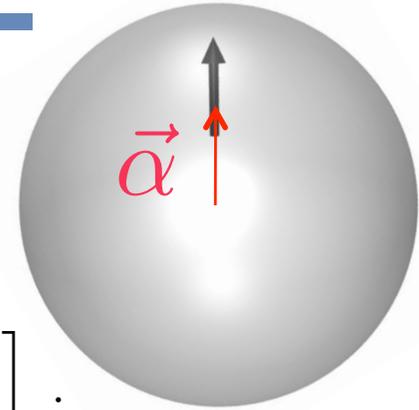




Shifted Dipol Model

Steric Interaction (WCA)
plus dipolar

$$\alpha = \frac{|\vec{\alpha}|}{R}$$



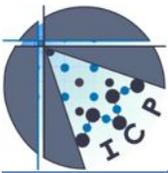
$$U_{dd}(\mathbf{m}_i, \mathbf{m}_j, \mathbf{r}_{ij}) = -\frac{\mu_0}{4\pi} \left[3 \frac{(\mathbf{m}_i \cdot \mathbf{r}_{ij})(\mathbf{m}_j \cdot \mathbf{r}_{ij})}{r^5} - \frac{(\mathbf{m}_i \cdot \mathbf{m}_j)}{r^3} \right].$$

$$\mathbf{r}_{ij} = \mathbf{r}_i - \mathbf{r}_j, \quad r = |\mathbf{r}_{ij}|$$

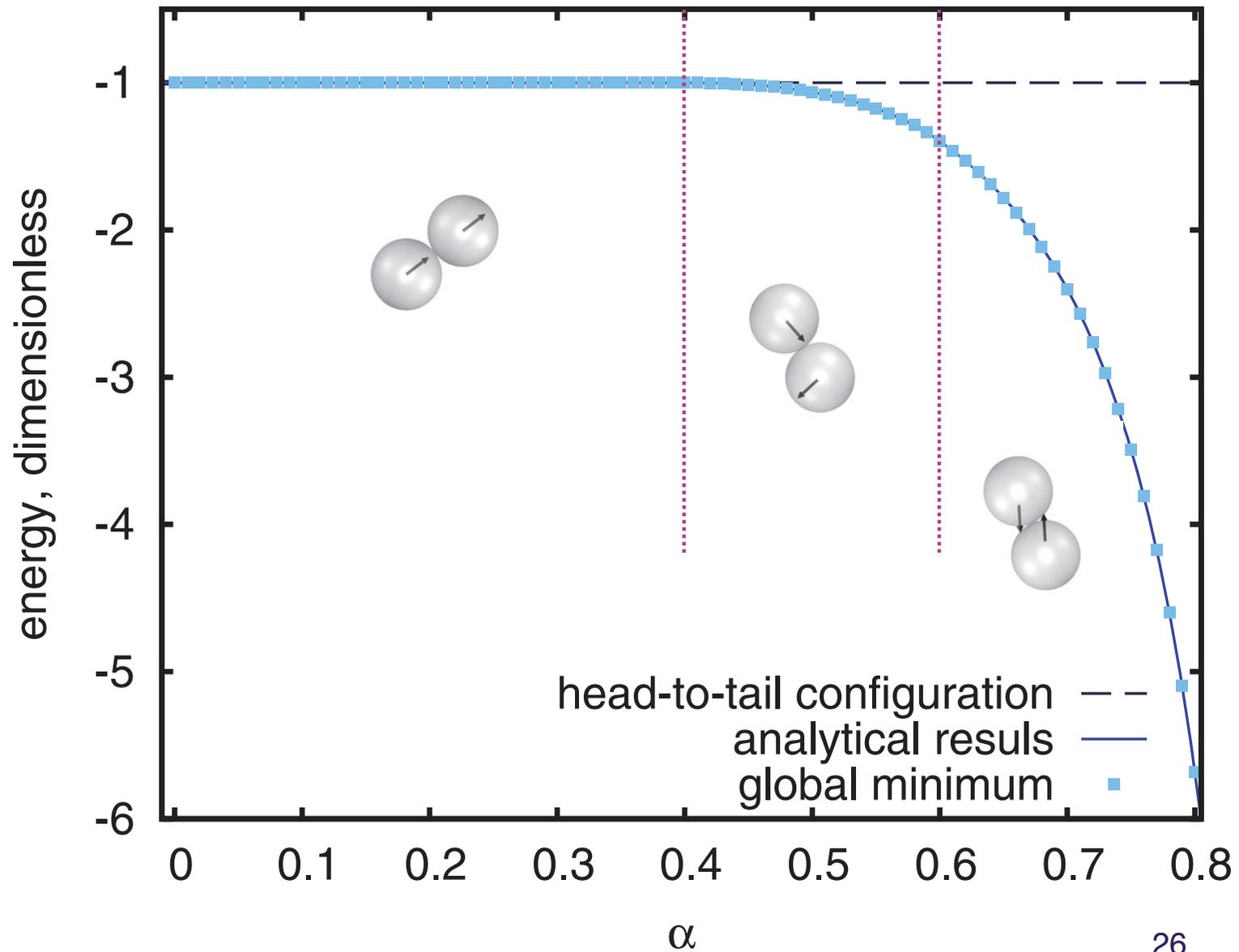
$$\lambda = \frac{\mu_0 |\mathbf{m}|^2}{4\pi k_B T d^3} \quad \lambda^* = \gamma(\alpha) \cdot \lambda$$

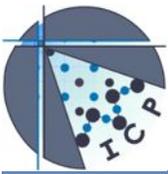
$$\gamma(\alpha) = \frac{U_{gs}(0)}{U_{gs}(\alpha)}$$

α	$\gamma(\alpha)$
0	1
0.4	0.9999
0.5	0.9396
0.6	0.7163
0.7	0.4164
0.8	0.1761



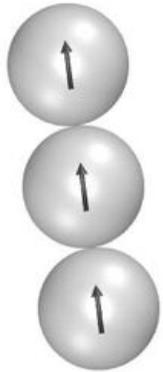
Two-particle ground states





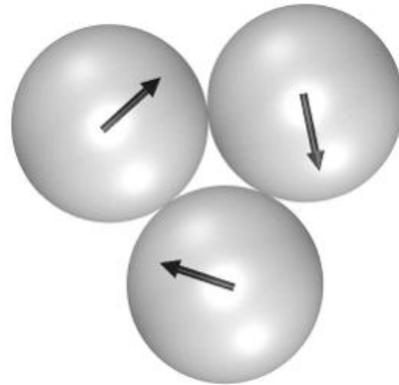
3-Particle Clusters

C3-I



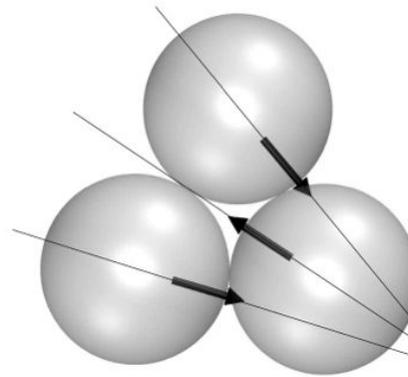
$$\alpha = 0$$
$$0 < \alpha < 0.258$$

C3-II



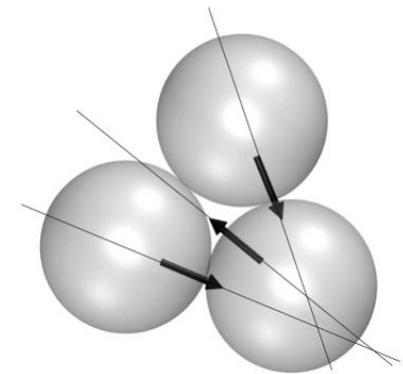
$$\alpha = 0.3$$
$$0.258 < \alpha < 0.799$$

C3-III

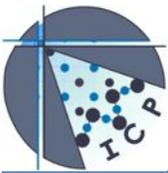


$$\alpha = 0.81$$
$$0.799 < \alpha < 0.83$$

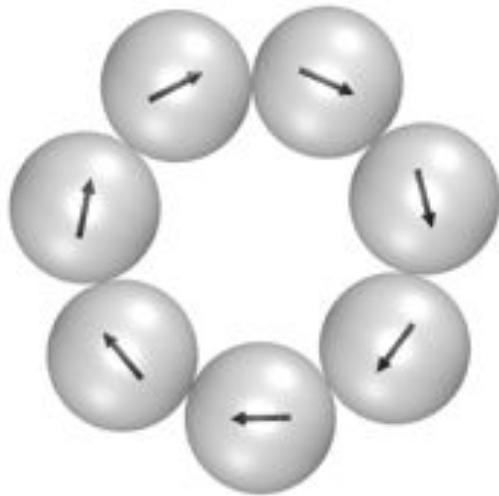
C3-IV



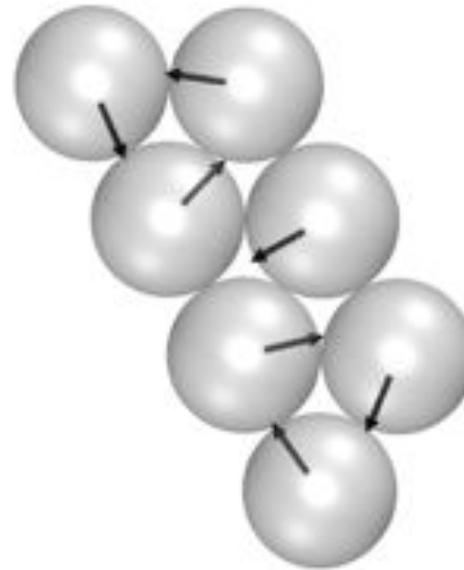
$$\alpha = 0.85$$
$$0.83 < \alpha < 1$$



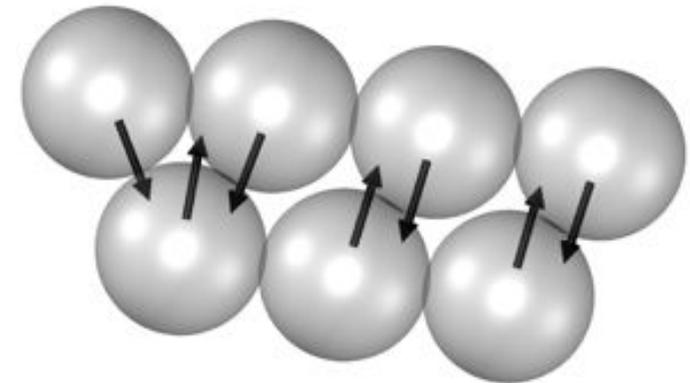
Higher Order Clusters



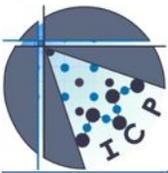
$\alpha = 0.0$



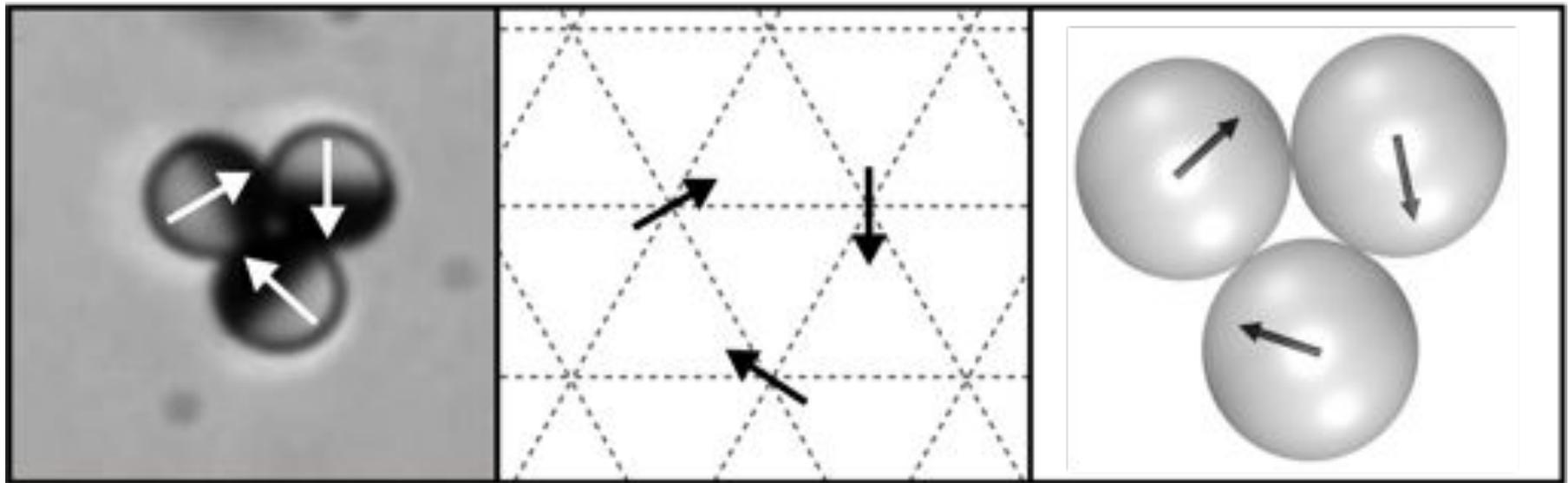
$\alpha = 0.67$



$\alpha = 0.85$

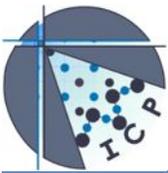


Baraban 3-Particle Cluster

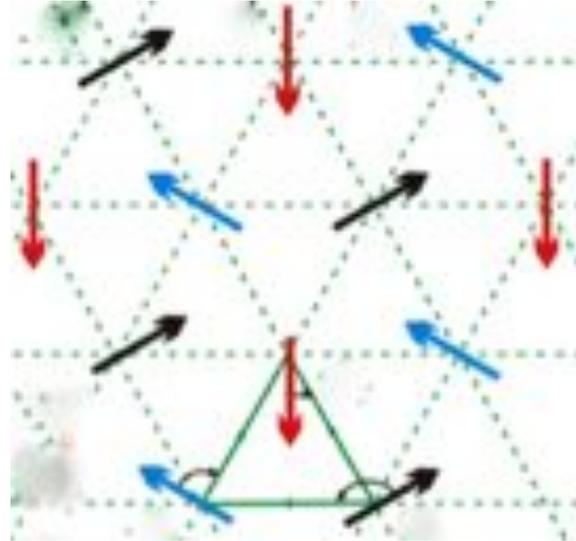
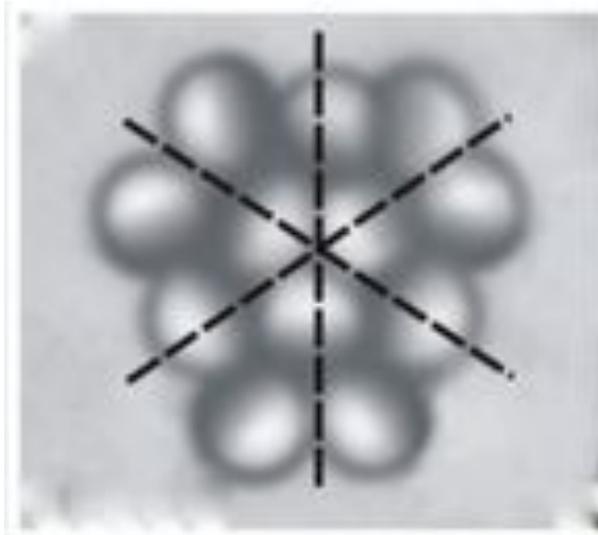


$$\alpha \approx 0.5$$

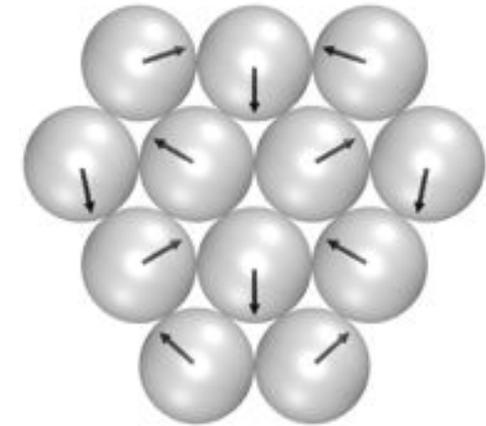
Triangular configuration observed for wide range of $0.258 < \alpha < 0.799$



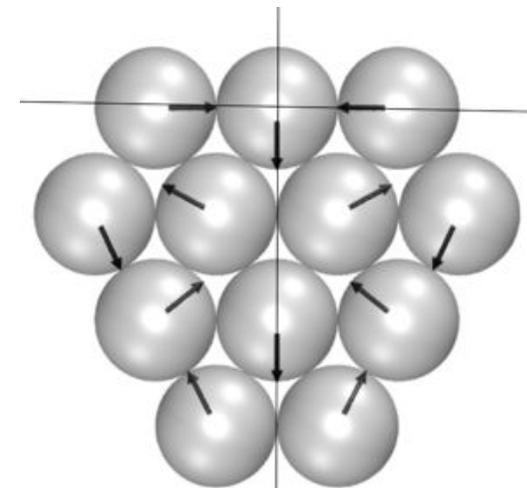
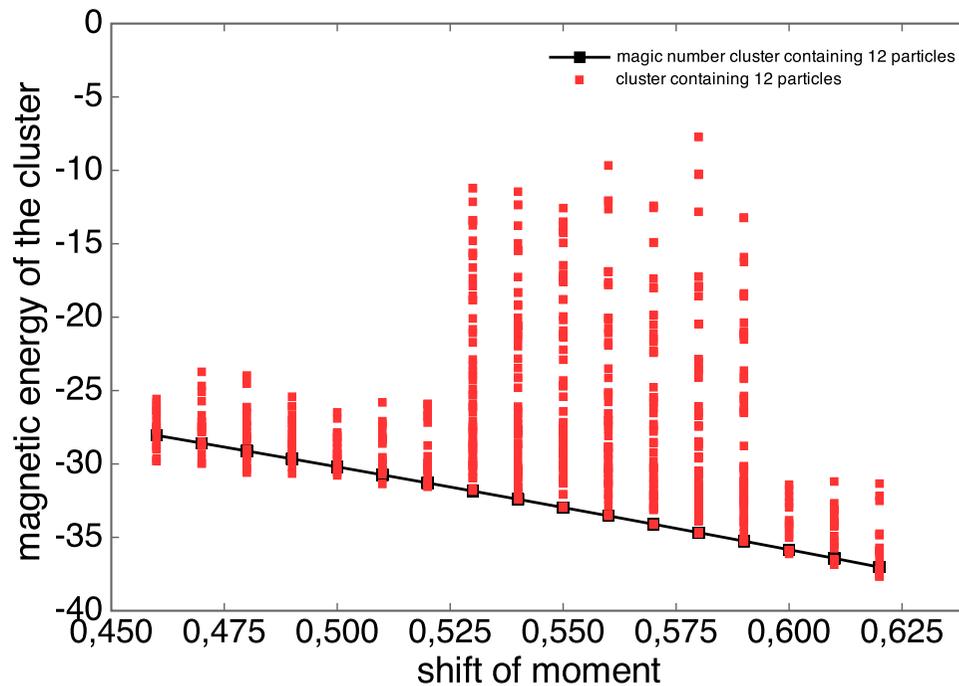
12-Particle „Magic Cluster“



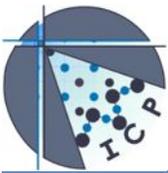
Best „match“



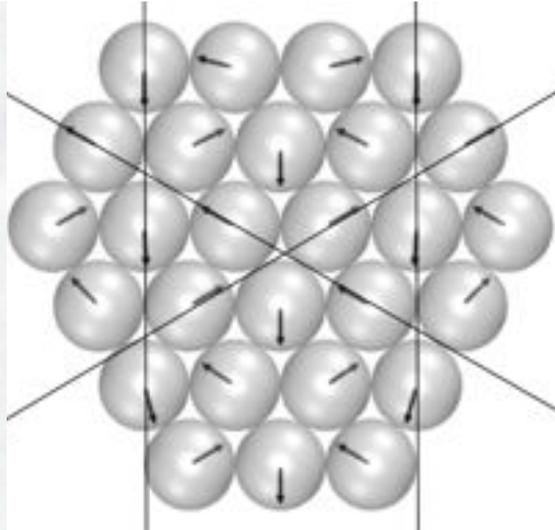
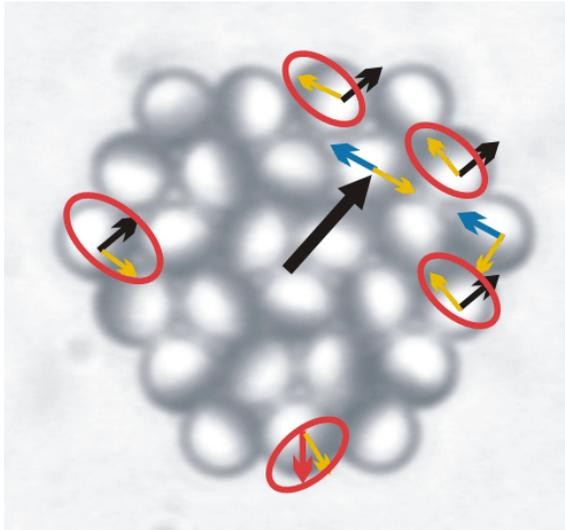
$$\alpha = 0.47$$



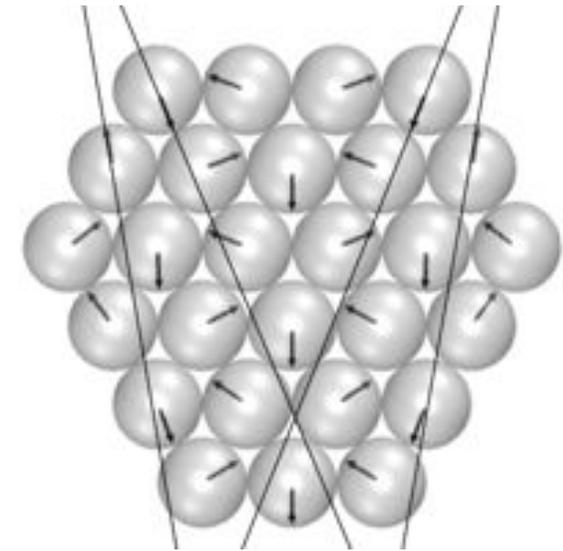
$$\alpha = 0.62$$



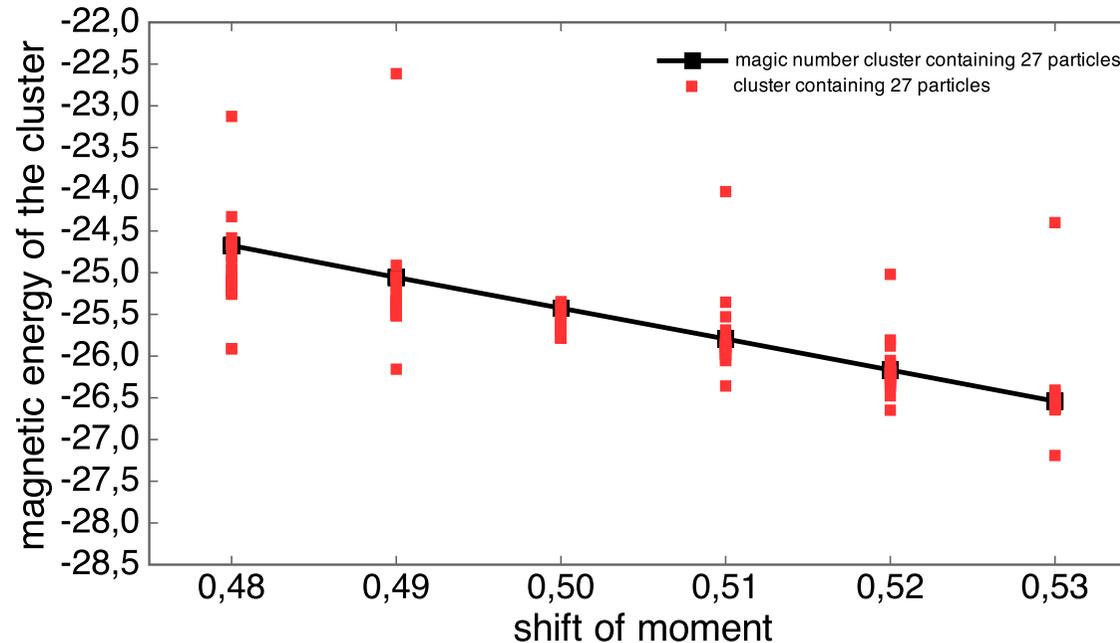
27-Particle „Magic Cluster“



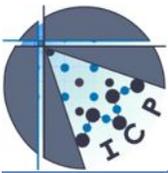
$$\alpha = 0.68$$



$$\alpha = 0.53$$



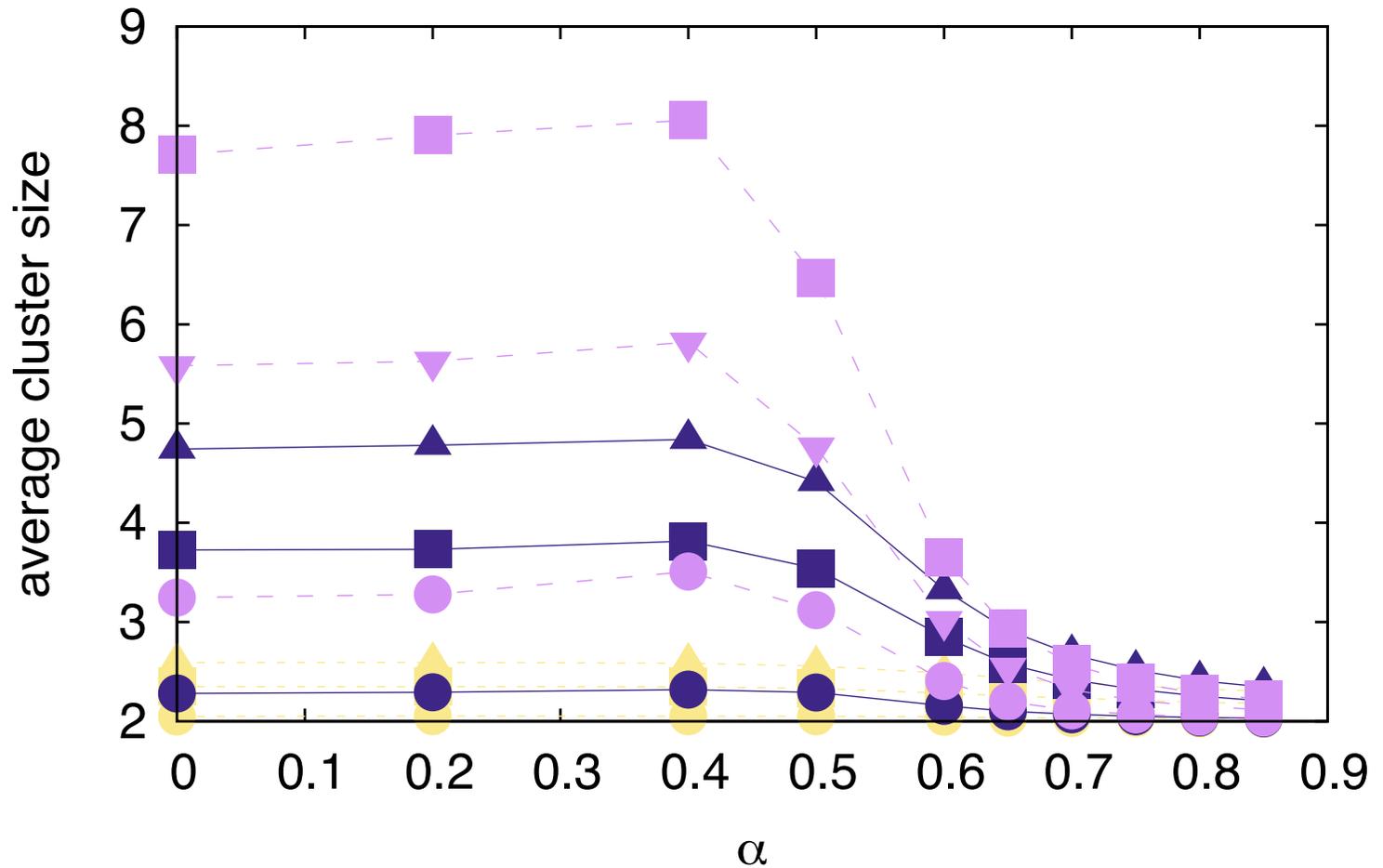
Magic cluster does not correspond to the ground state

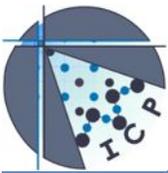


Cluster Size at Room Temperature

$\lambda^* = \gamma(\alpha) \cdot \lambda$

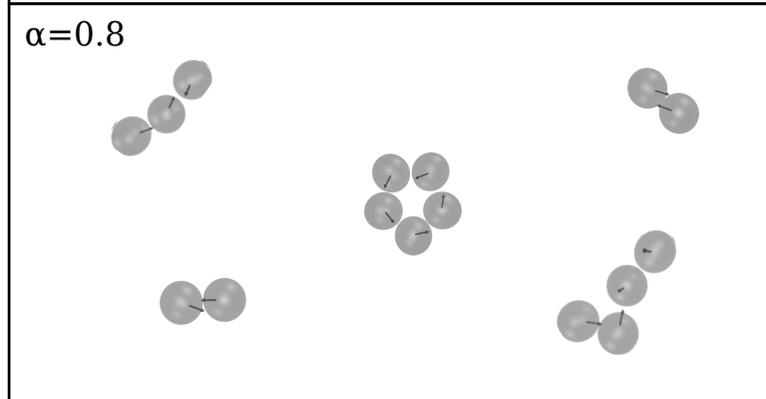
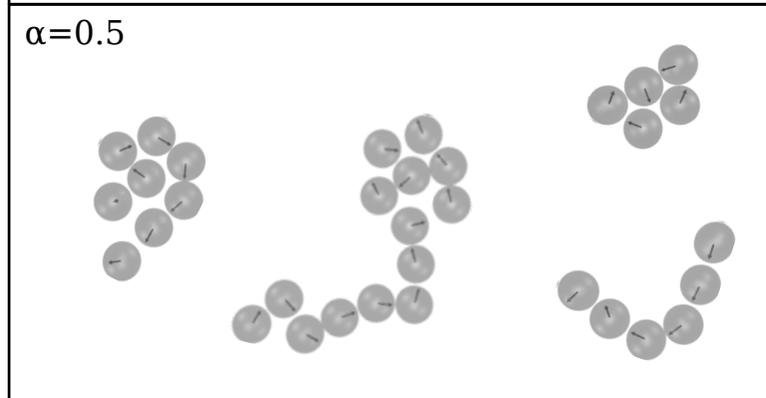
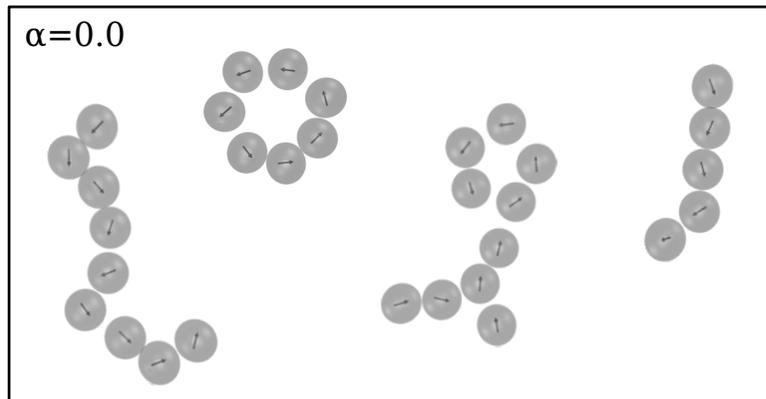
$\lambda^*=1$ $\phi=0.03$ ●	$\lambda^*=3$ $\phi=0.03$ ●	$\lambda^*=4$ $\phi=0.03$ ●
$\lambda^*=1$ $\phi=0.15$ ■	$\lambda^*=3$ $\phi=0.15$ ■	$\lambda^*=4$ $\phi=0.09$ ▼
$\lambda^*=1$ $\phi=0.21$ ▲	$\lambda^*=3$ $\phi=0.21$ ▲	$\lambda^*=4$ $\phi=0.15$ ■



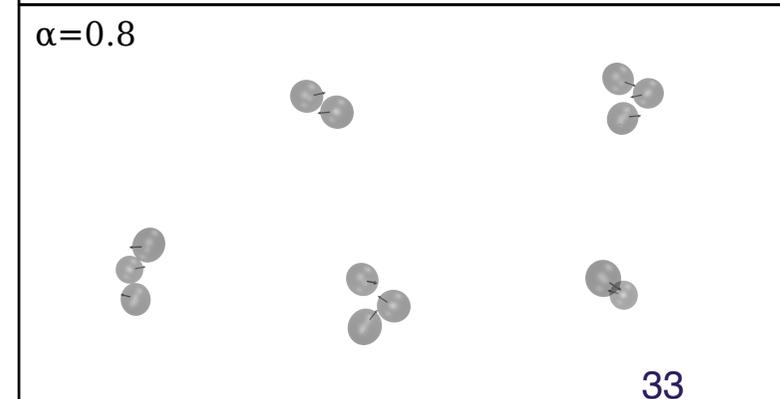
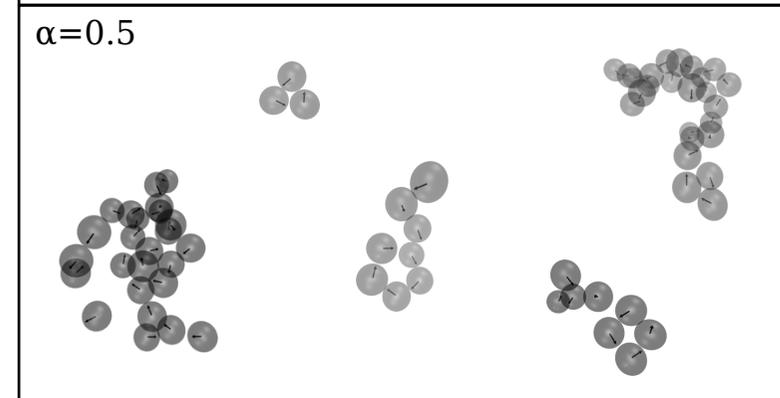
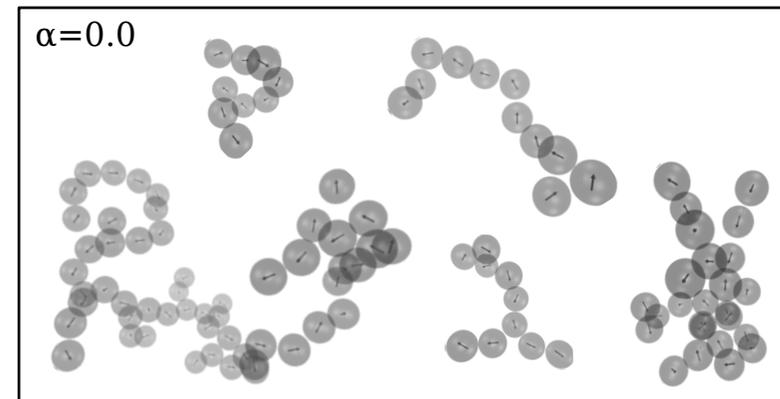


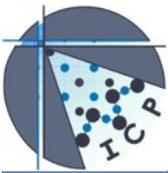
Cluster at finite Temperature

Q2D

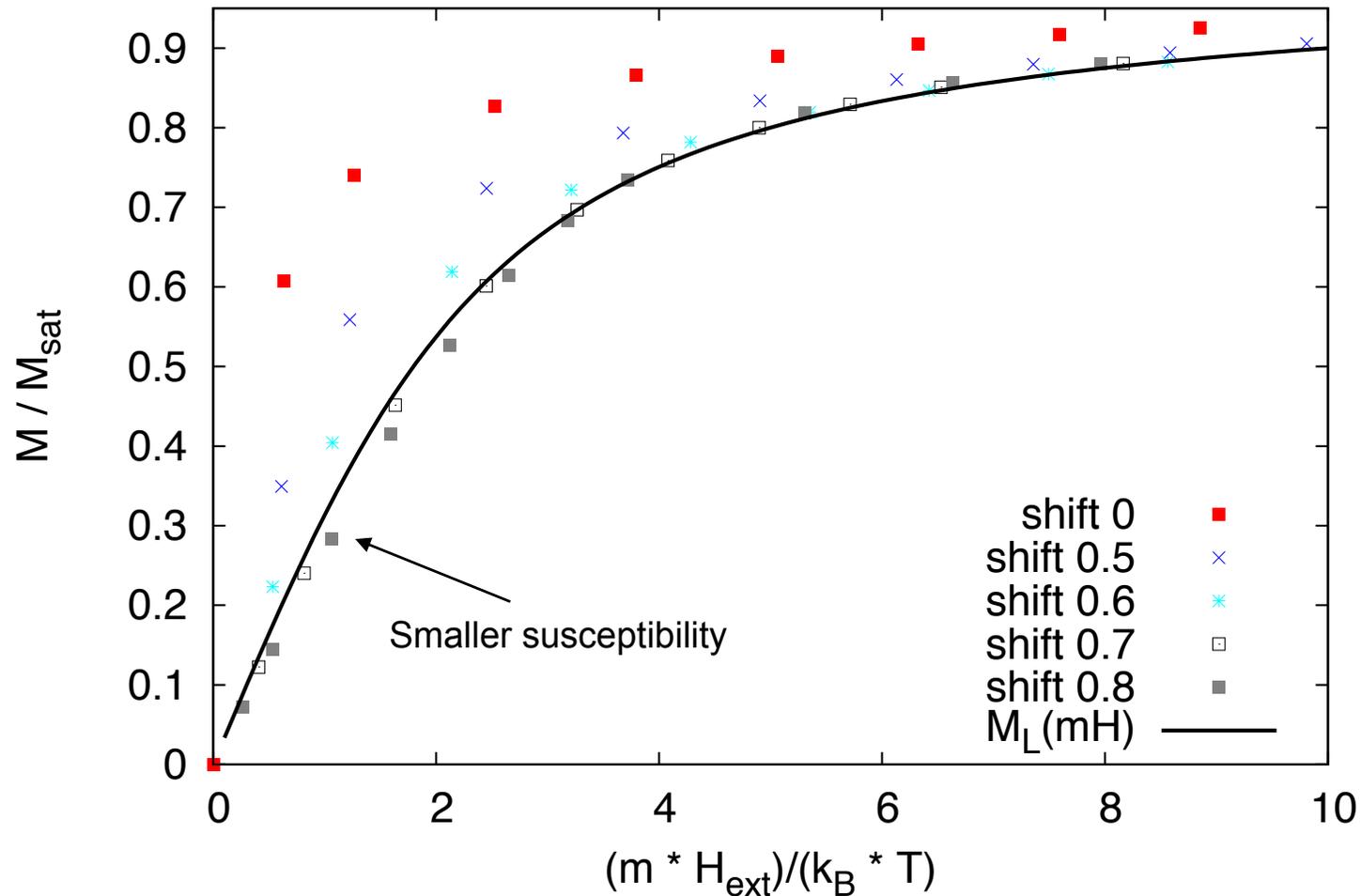


3D

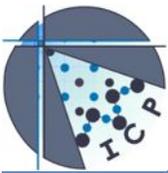




Magnetization Behavior of SD

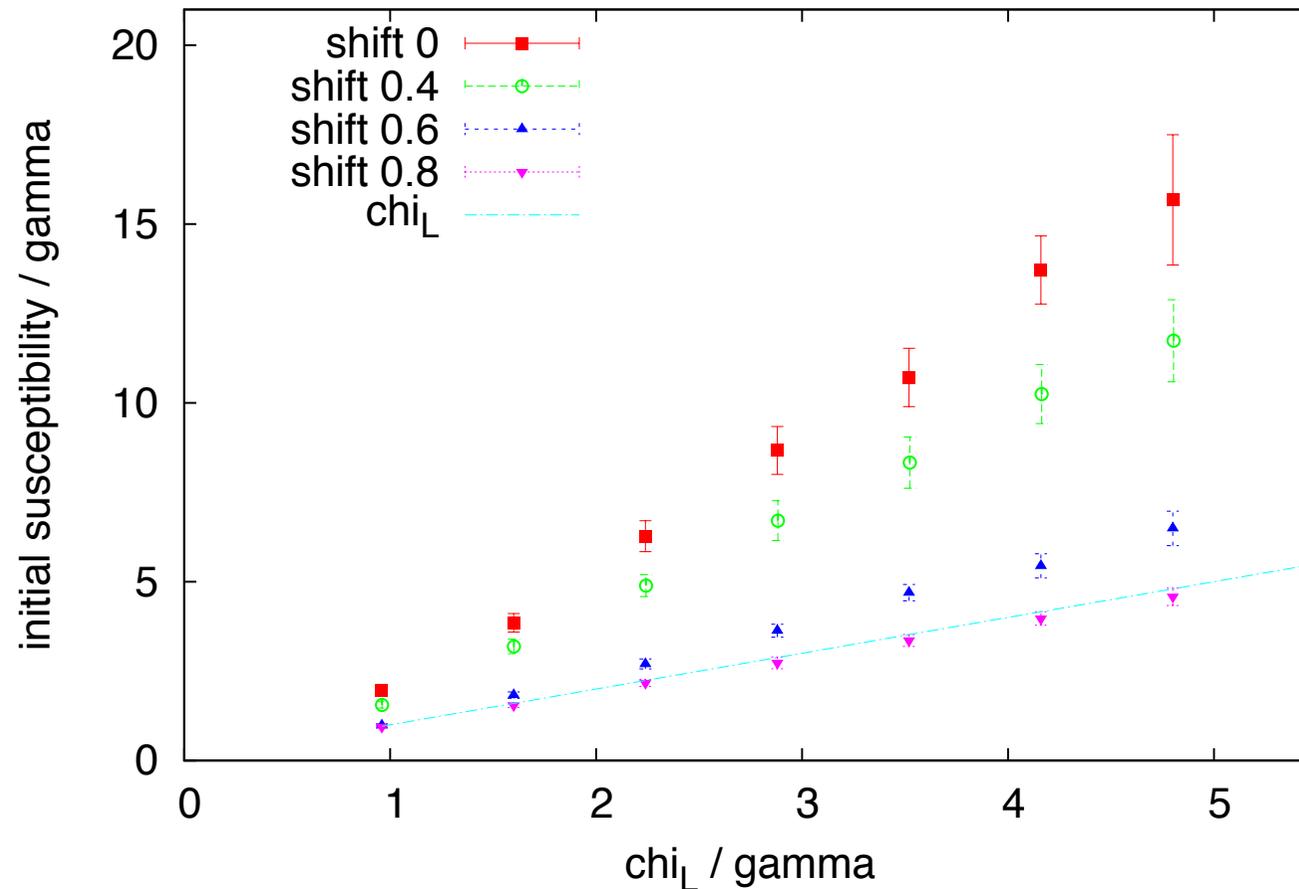


At large field values and large shifts, the clusters of anti-parallel dipoles break up under the influence of strong fields=> **reversible self-assembly** !

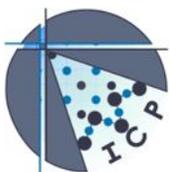


Susceptibility for $\lambda^*=4$

$$\chi_L = \rho \frac{m^2}{3\mu_0 kT}$$

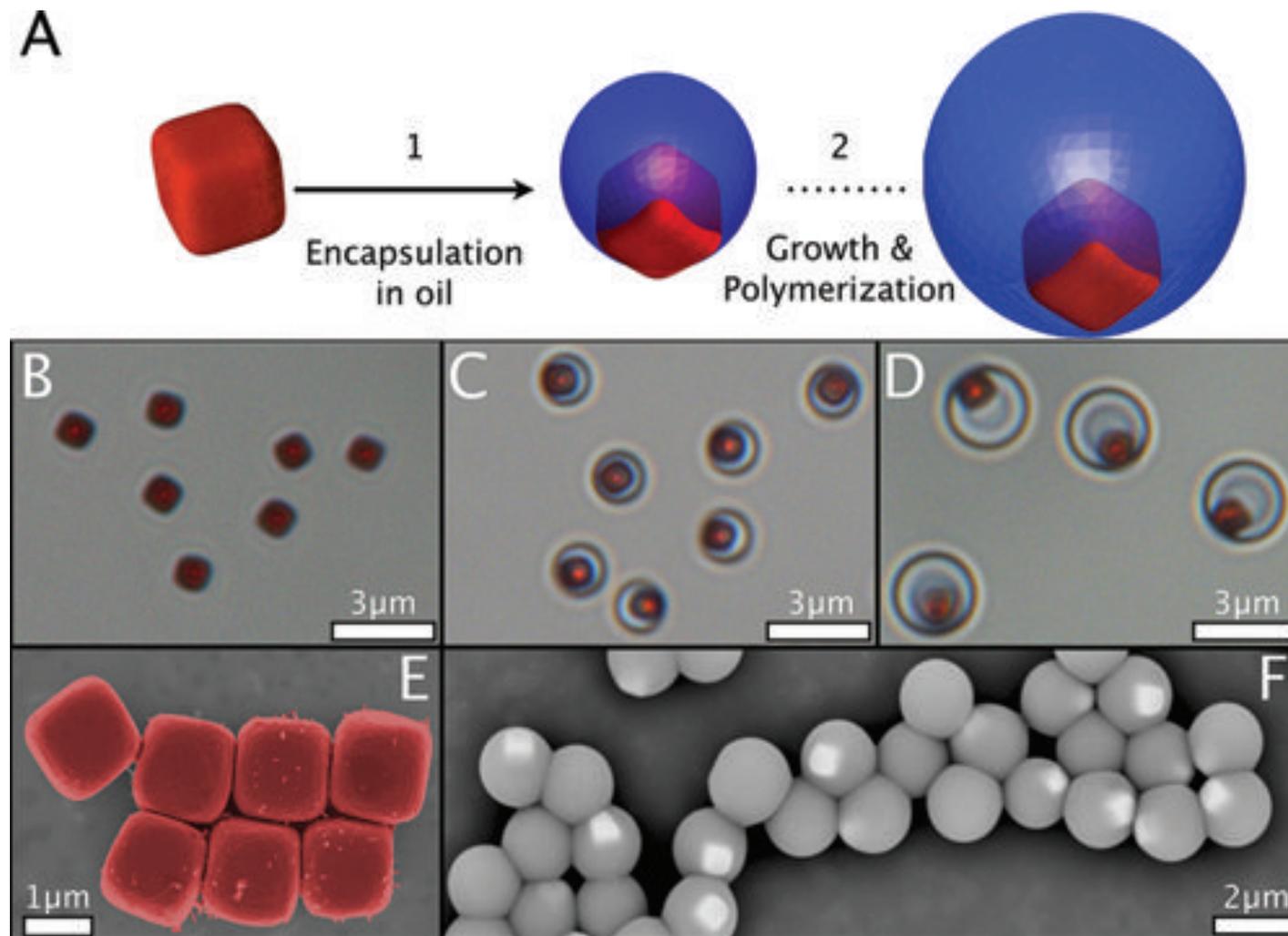


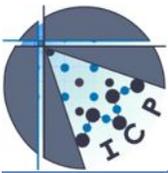
Initial susceptibility can be smaller than Langevin law!
Due to occurrence of many clusters with zero magnetic moment



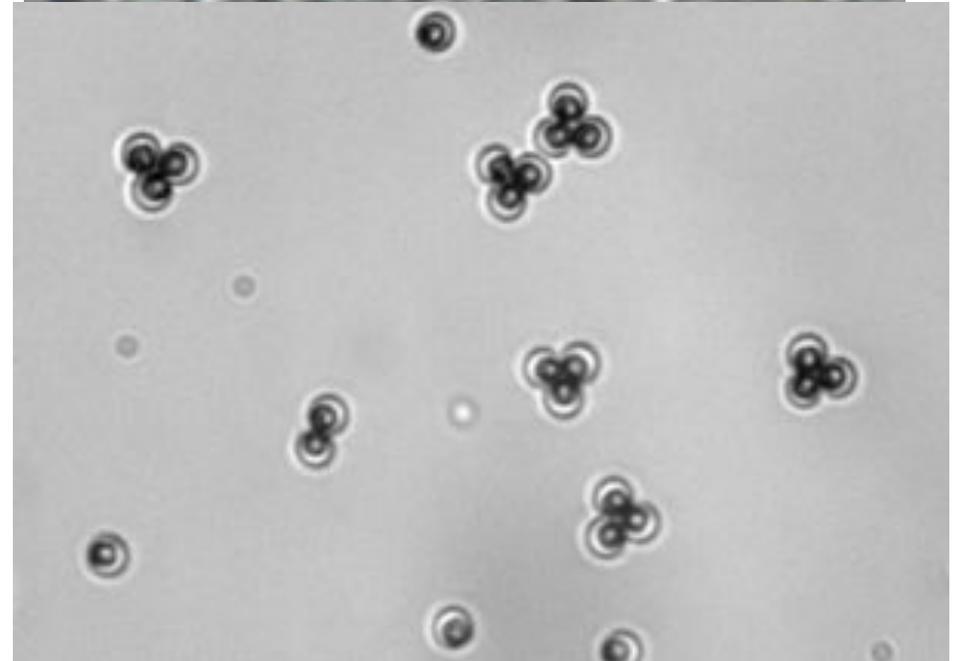
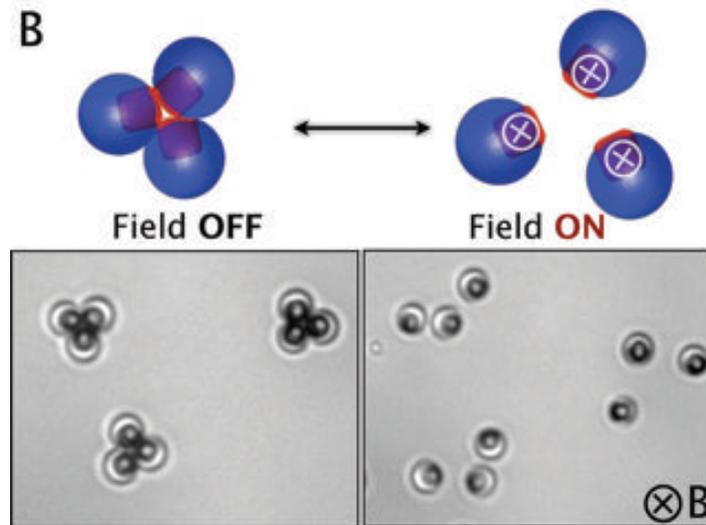
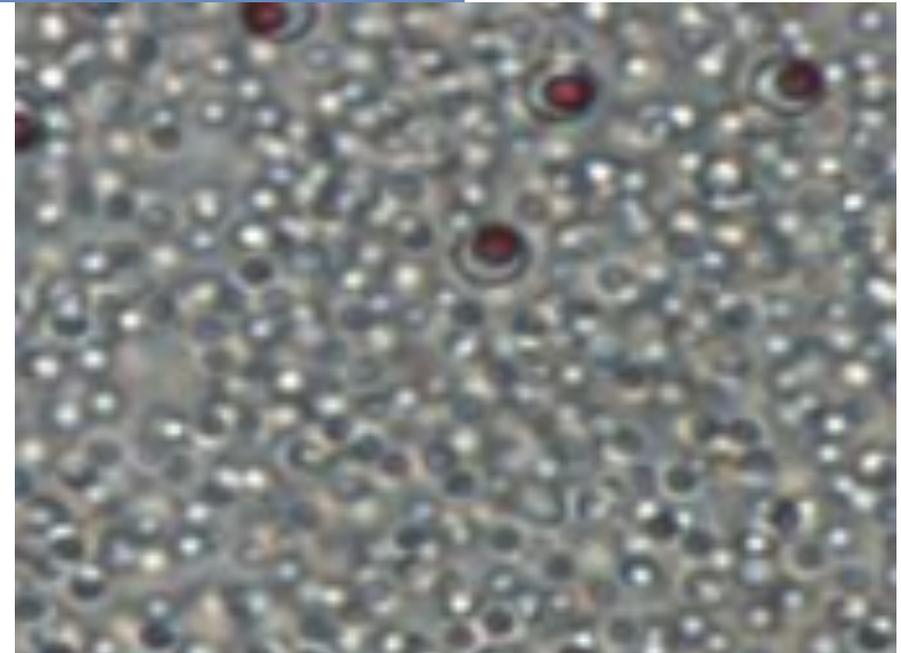
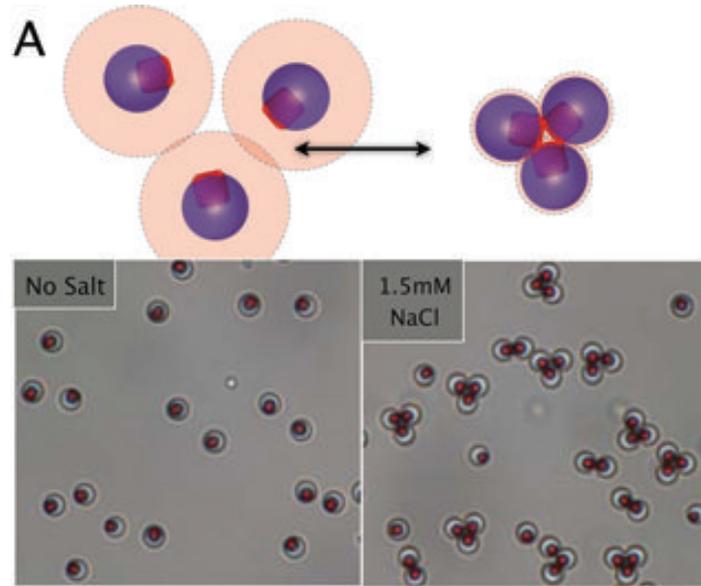
New Experimental Realisation

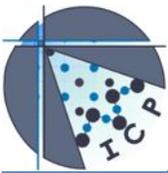
D. Pine group, *Magnetic Click Colloidal Assembly* J. Am. Chem. Soc. **134**, 6112-6115 (2012)





Pine's Patchy Colloids





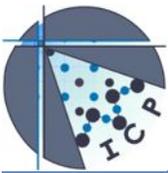
Summary Part 2

- the form of ground state clusters changes from chains and rings over triangles to structures with antiparallel orientation of magnetic moments with increasing shift α
- the size of clusters is controlled by α , λ^* , and ϕ , whereas its structure is dominated by α
- for large shifts initial susceptibility is lower than the initial susceptibility of a Langevin ideal superparamagnetic gas
- A strong applied field at high shifts can reversibly unbind anti-parallel pairs

S. Kantorovich, R. Weeber, J.J. Cerdà, C. H., "Ferrofluids with shifted dipoles: ground state structures" *Soft Matter* **7**, 5217, (2011).

S. Kantorovich, R. Weeber, J.J. Cerdà, C. H., "Magnetic particles with shifted dipoles", *JMMM* **323**, 1269 (2011),

M. Klinkigt, R. Weeber, S. Kantorovich, C. Holm, in preparation (2012).



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Y. Raikher (Perm)

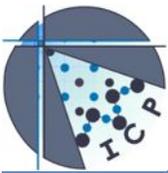
R. Perzynski (Paris)



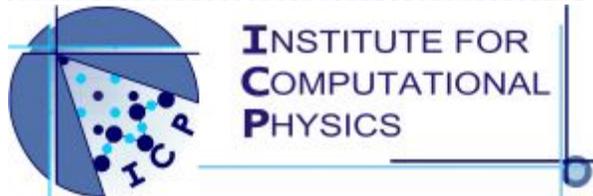
<http://www.espressomd.com>

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