



Rare event sampling with



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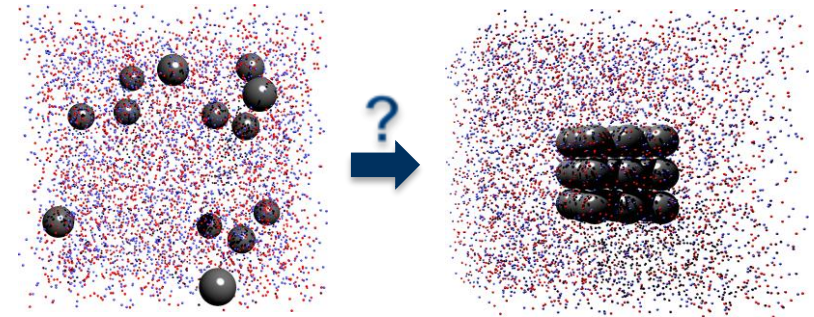
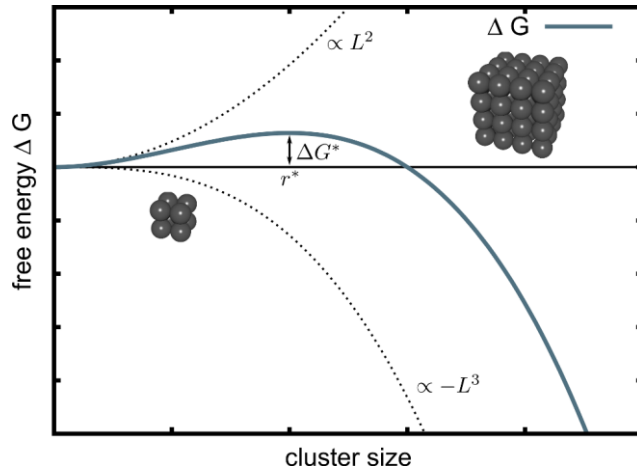
Outline

- Intro: Rare events & sampling methods overview
- Forward flux sampling (FFS)
- Stochastic process rare event sampling (S-PRES)
- Harness System (FRESHS)
- Conclusion



Rare Events: Examples

■ Crystallization of charged macromolecules



Clusters smaller than a critical nucleus size are more likely dissolved than they continue to grow!

$$\Delta G = -\Delta G_V + \Delta G_S = -\mu\rho\frac{4}{3}\pi L^3 + 4\pi\sigma L^2$$

CNT: bulk term and surface term

→ **Long time scales, many particles:** Does not crystallize in available computation time

→ Computationally very expensive task, only few, if any, events are observed in a conventional simulation run

→ Rare event

- Macroscopic: Earthquakes, financial crashes, telecommunication failures
- Microscopic: Activated chemical reactions, protein folding, translocation of DNA through nanopores



Simulating rare events – methods overview

- Many rare event sampling methods have been developed recently [1], e.g.
 - Bennet-Chandler/reactive flux methods based on the transition state theory (TST)
 - Transition path sampling (TPS) and transition interface sampling (TIS)
 - Milestoning
 - The weighted ensemble method
 - The finite temperature string method (FTS)

equilibrium

...

equilibrium and
nonequilibrium

- Forward flux sampling (FFS)
- Stochastic process rare event sampling (S-PRES) [2]

[1] R. J. Allen, Ch. Valeriani, P. R. ten Wolde, J. Phys: Condens. Matter **21** 463102 (2009)

[2] J. T. Berryman and T. Schilling, J. Chem. Phys. **133**, 244,101 (2010)



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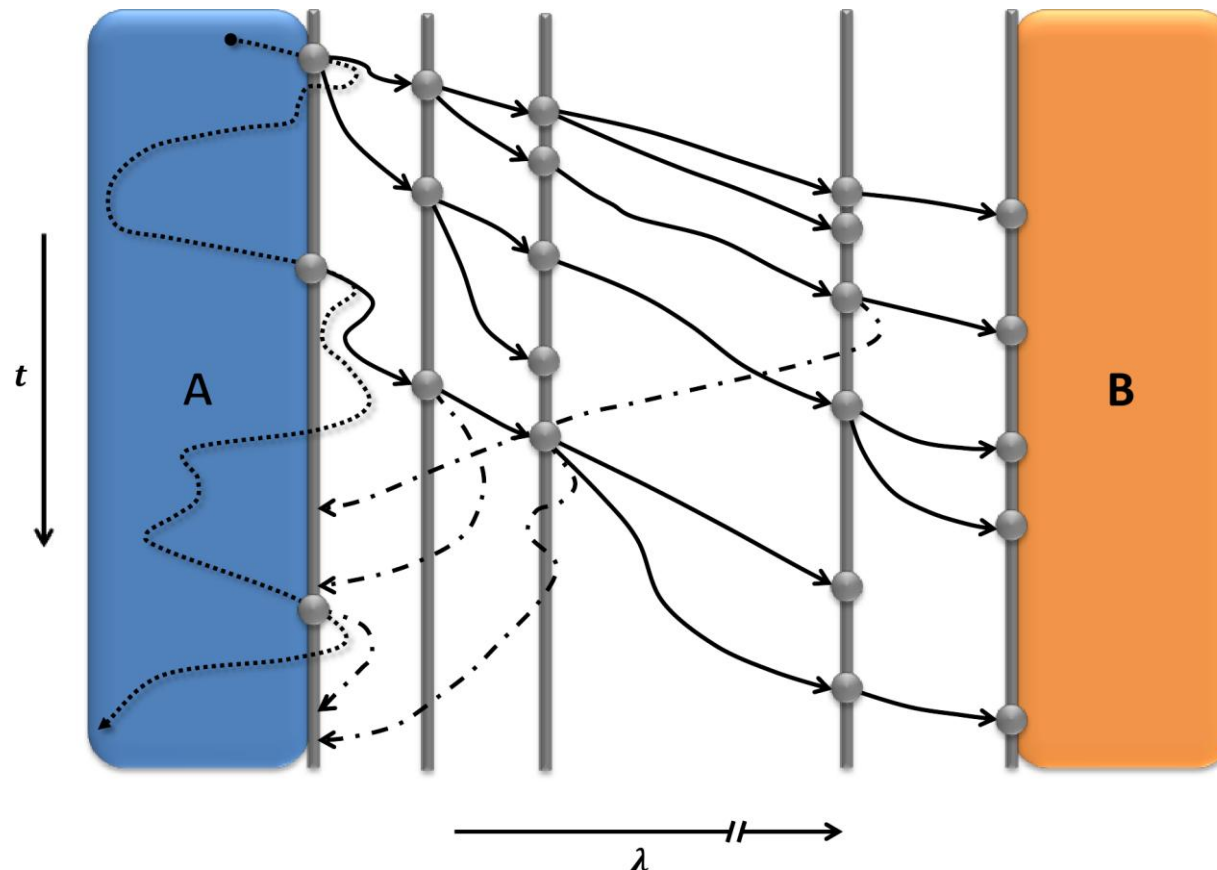
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Forward Flux Sampling (FFS)

R. J. Allen, Ch. Valeriani, P. R. ten Wolde, J. Phys: Condens. Matter **21** 463102 (2009)

■ Rare event: **Spontaneous, fluctuation-driven** transition



- Transition rate
 $k_{AB} = \Gamma e^{-\beta \Delta G^*}$
- Arrhenius equation
- kinetic pre-factor Γ
- $\beta = 1/k_B T$



Forward Flux Sampling

- Escape flux:
$$\frac{\bar{\Phi}_{A,0}}{\bar{h}_A} = \frac{\text{number of configurations at } \lambda_0}{\text{total simulation time}}$$
- Conditional probabilities:
$$P(\lambda_n|\lambda_0) = \prod_{i=0}^{n-1} P(\lambda_{i+1}|\lambda_i)$$
- Transition rate:
$$k_{AB} = \frac{\bar{\Phi}_{A,n}}{\bar{h}_A} = \frac{\bar{\Phi}_{A,0}}{\bar{h}_A} P(\lambda_n|\lambda_0)$$
- Advantage:
$$P(\lambda_{i+1}|\lambda_i) \gg P(\lambda_n|\lambda_0)$$

→ Much easier to sample than the whole process!
- FFS:
Equilibrium and **nonequilibrium** systems with stochastic dynamics, **quasistatic**



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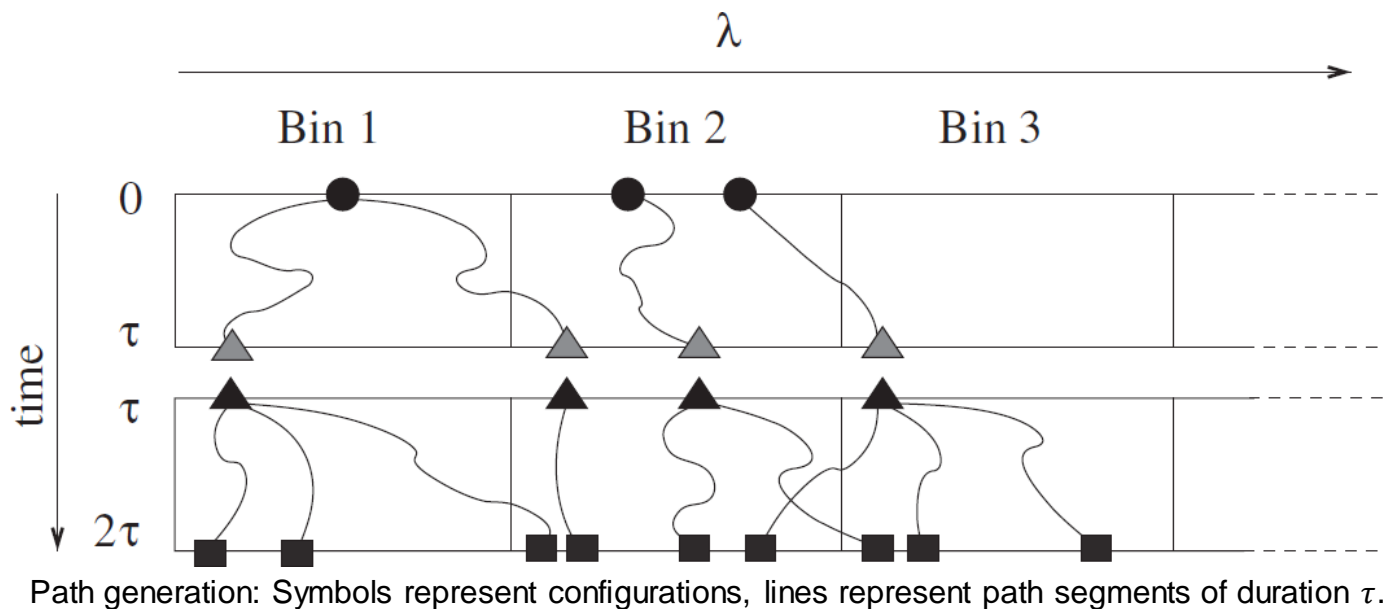
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Stochastic Process Rare Event Sampling (S-PRES)

J. T. Berryman and Tanja Schilling, J. Chem. Phys. **133**,244101 (2010)

- Focus on calculating the **time-series** of the probability of a rare event
- Phase space binning instead of hypersurfaces
- Reaction coordinate λ , trajectory paths similar to FFS
- Now: Each trajectory fragment (shot) has a fixed duration for tracking the time evolution



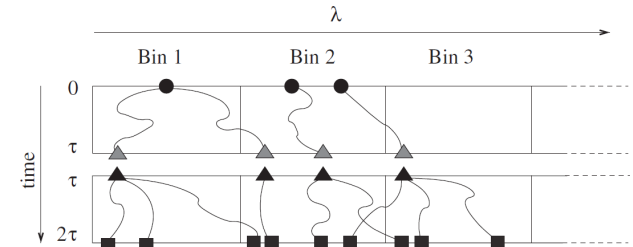


Stochastic Process Rare Event Sampling (S-PRES)

- Rosenbluth sampling is used to ensure dynamically adaptive sampling rates in the bins

- Fixed bins

- ➔ Time-dependent matrix of transition frequencies
- ➔ Extraction of observables and statistics



- S-PRES:

Nonequilibrium and **nonstationary** systems with macroscopically **irreversible dynamics** and away from both stationary and metastable states

- Examples of events: quenching, aging, ignition, impact

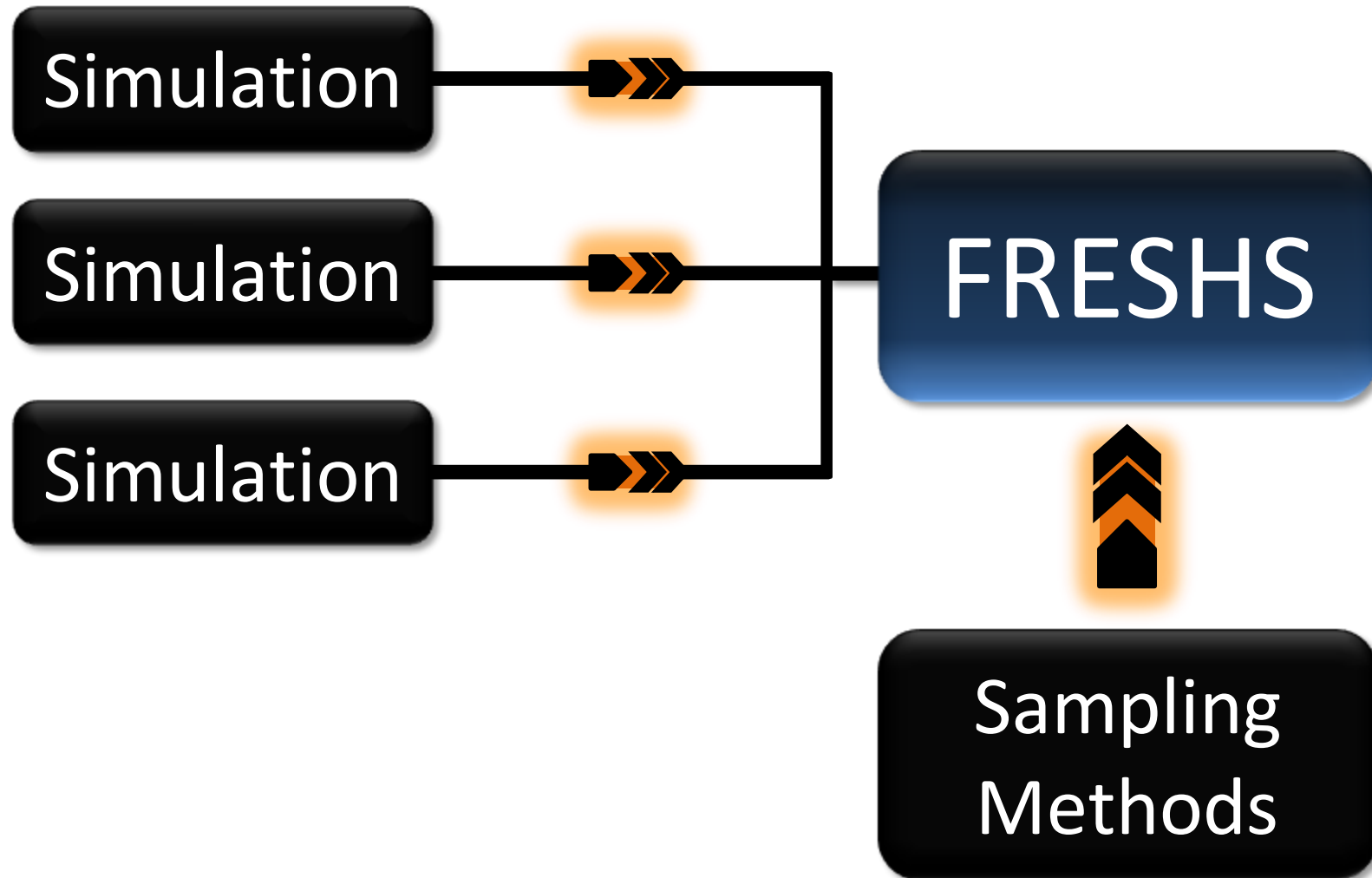


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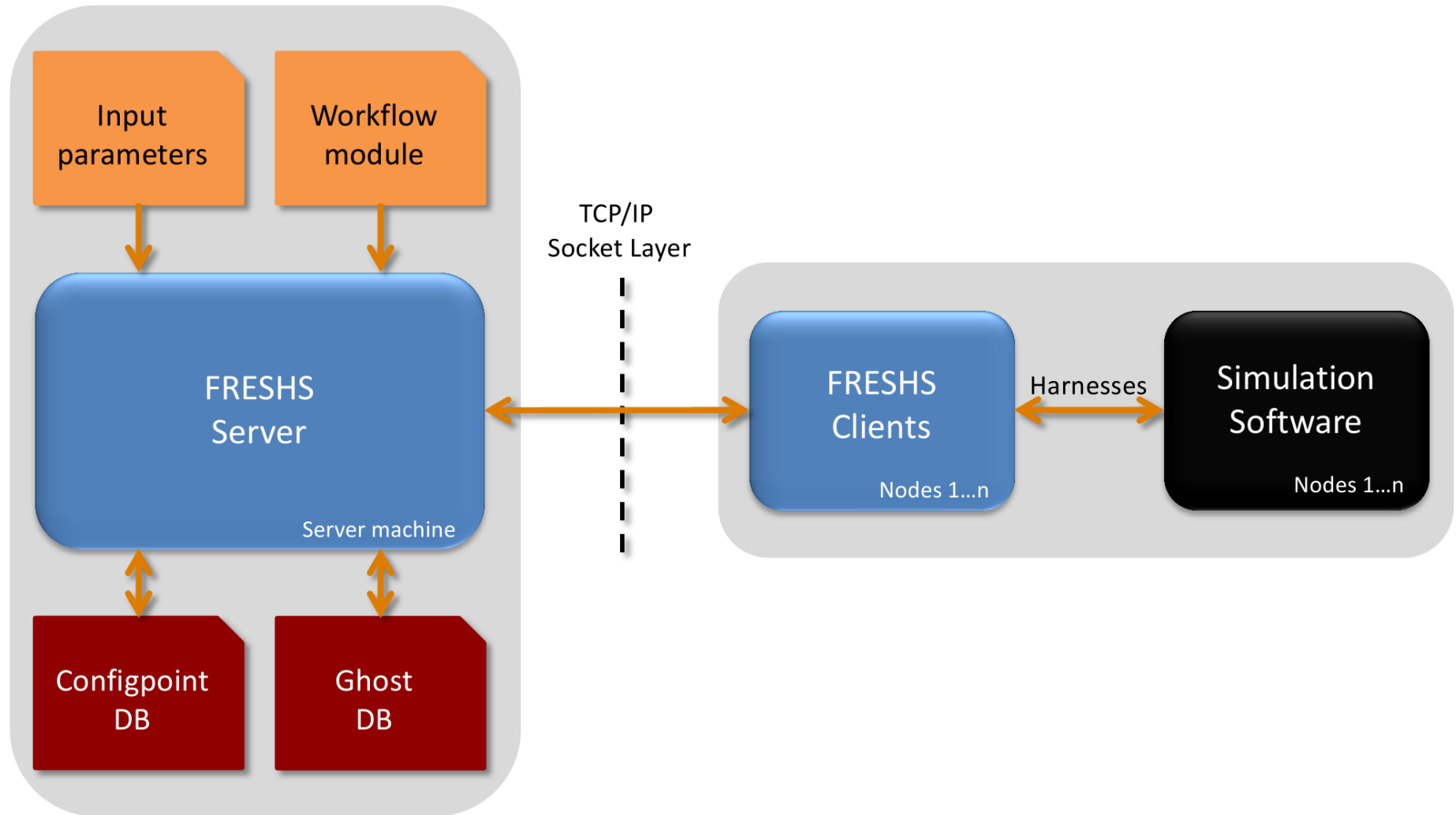


The Flexible Rare Event Sampling Harness System





The Flexible Rare Event Sampling Harness System





The Flexible Rare Event Sampling Harness System



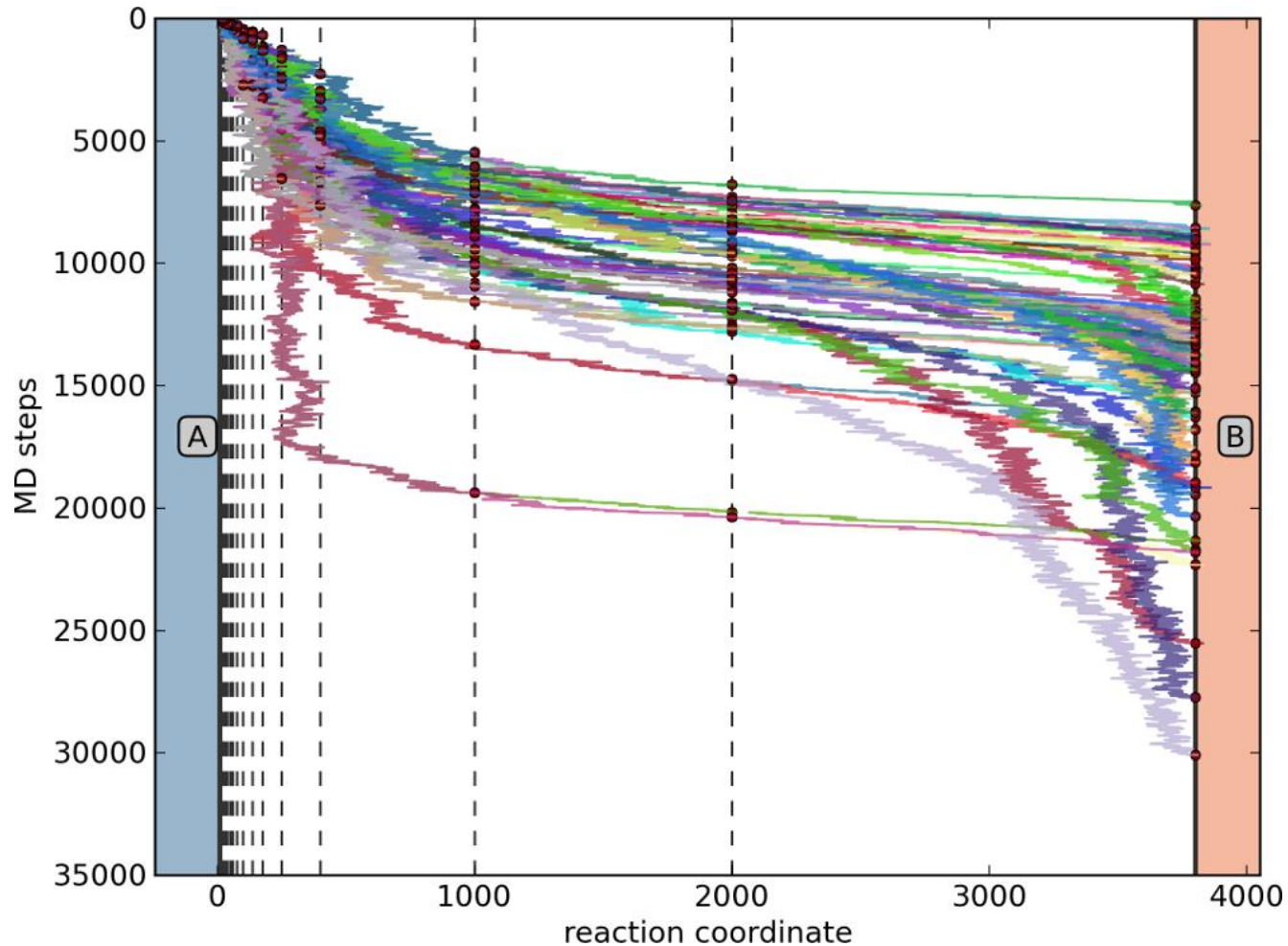
- Asynchronous parallelization
 - ➔ each path can be calculated by a different client
- Calculation of the physics can still be parallelized using OpenMP or MPI
 - E.g. each client 1 node and 8 CPUs, 100 clients connected
 - ➔ 800 CPUs working for us
- Ghost runs to bridge the waiting time on interface change

Spin-off projects:

- A. Taudt: Gromacs & biological Systems, ICP / ITB
- J. Zeman: Kinetic Monte Carlo, Fe/Cu nucleation, ICP / IMWF
- S. Kesselheim: Translocation of DNA through nanopore, ICP



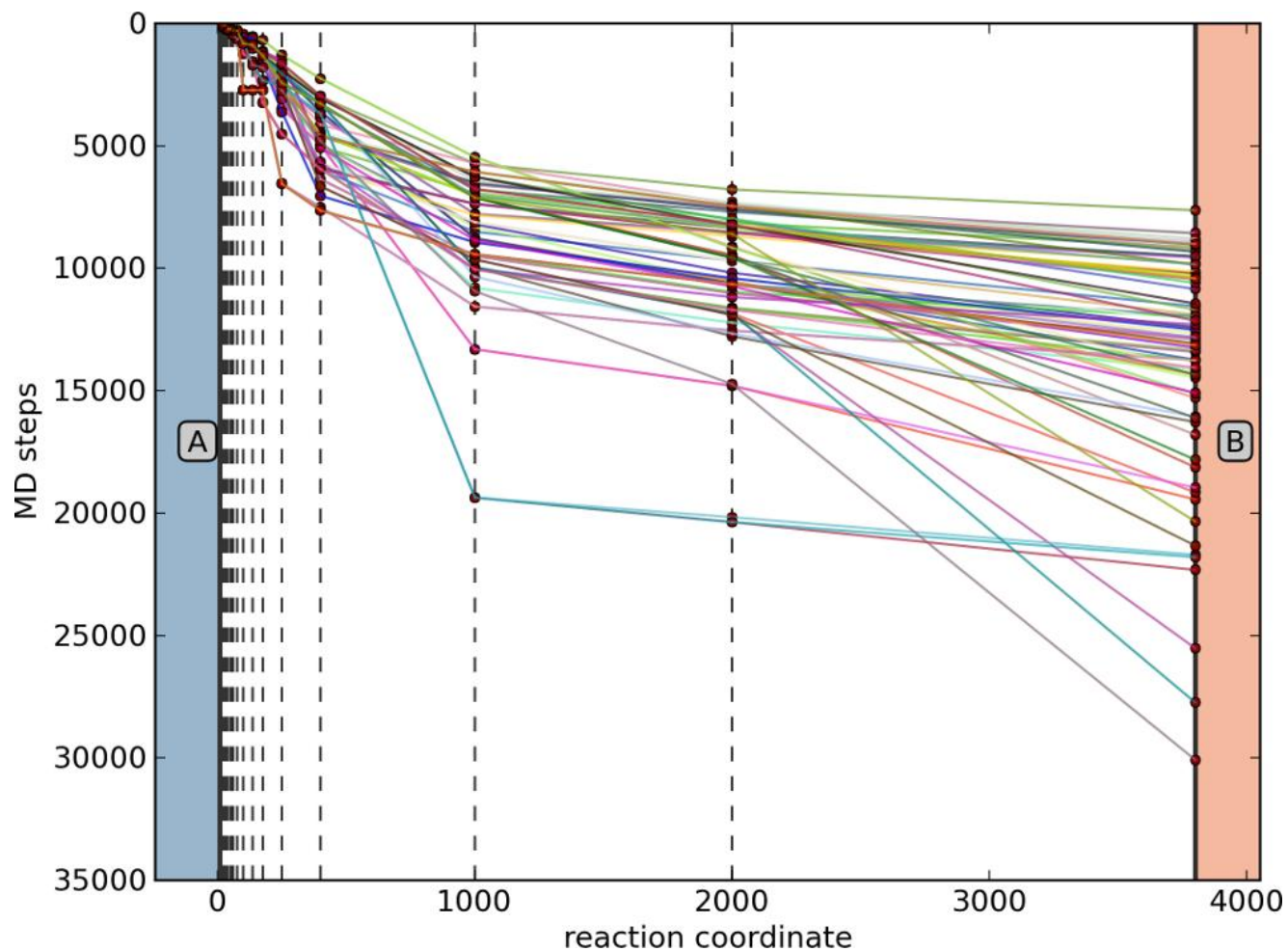
Results of a crystallization simulation - pathways



Successful pathways of the nucleation process: Fluctuations of the order parameter.



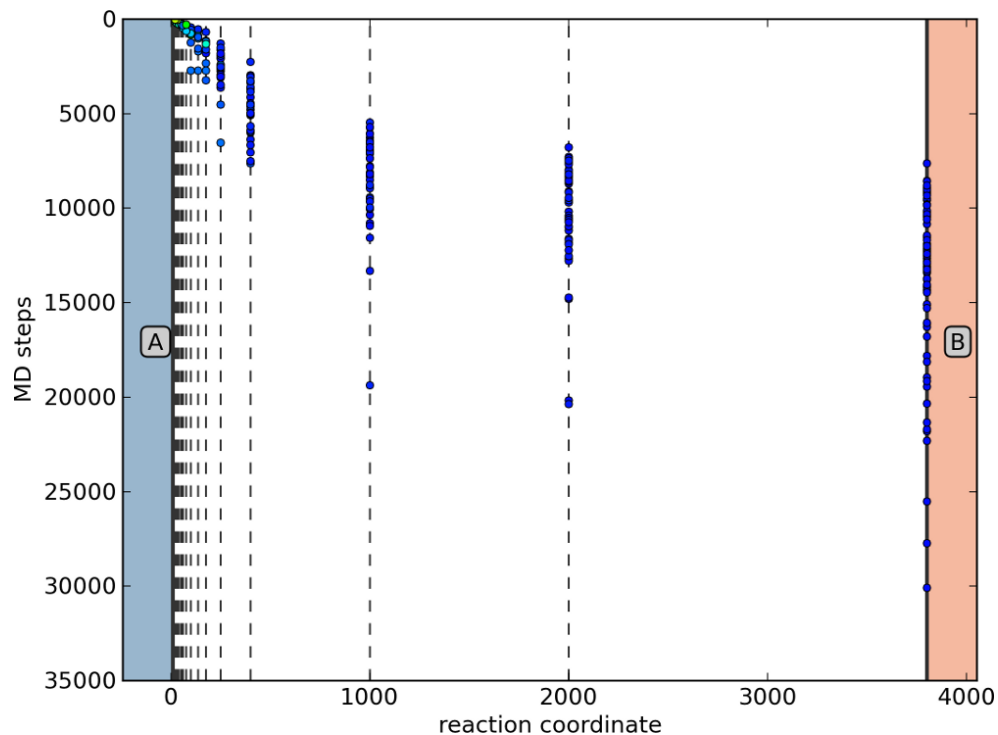
Results - backtracing



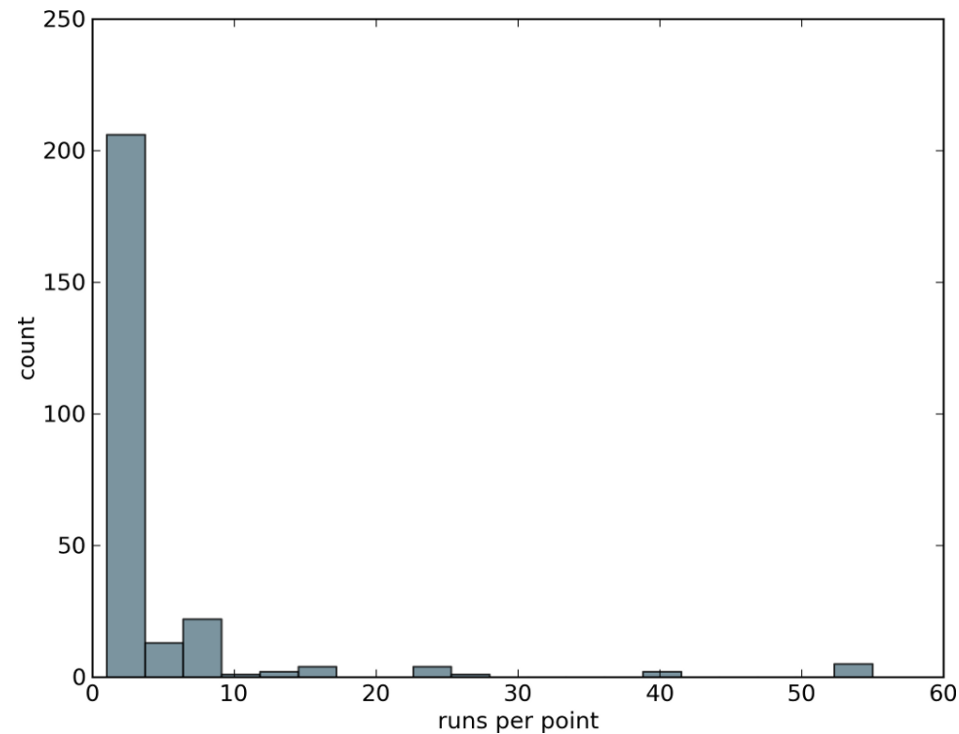
Backtrace of the successful runs. As many backtraces as points on border of state B.



Results - check of statistics



(a) BLUE = 1 run, RED = all runs.

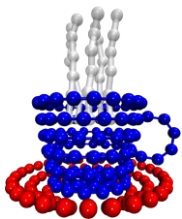


(b) Histogram of the runs per point.



Conclusions

- Developed flexible framework for simulating rare events
 - ➔ Simulating quasistatic and dynamic systems in equilibrium and non-equilibrium
 - ➔ Farming on HPC hardware
 - ➔ Tested with ESPResSo, Gromacs, LAMMPS and various self-written simulation codes
 - ➔ Will be put open source soon



<http://www.espressomd.org>



FRESHS + ESPResSo

Now:

Hands-on Tutorial



Requirements for the hands-on session

- FRESHS & Tutorial: http://www.icp.uni-stuttgart.de/~kratzer/freshs_tut.tar.bz2
- ESPResSo: <http://espressomd.org>
- Python

Optional:

- Gnuplot
- A sqlite DB viewer, e.g. firefox sql browser plugin
- VMD



Getting started

- Unpack the tutorial package
- Open the lj_spres_tut.pdf
- Follow instructions in the pdf

E.g.

- Run the server:

```
python "$FRESHHS"/server/main_server.py "$CONF"
```

- Start a client:

```
python "$FRESHHS"/client/main_client.py "$ESPRESSO" "$HARNESS"
```

- If things are working, start more clients ☺